

Computational Methods for Kinetic Processes in Plasma Physics



Ken Nishikawa

Department of Physics/UAH



Main program 4

June 4, 2015

Main program (continued)

```
c *****
  subroutine Smooth_Current(dex,dey,dez,mFx,mFy,mFz,sm,
&                          FBDLx,FBDLy,FBDLz,FBDRx,FBDRy,FBDRz)

  integer FBDRx,FBDRy,FBDRz
  integer FBDLx,FBDLy,FBDLz

  dimension dex(mFx,mFy,mFz),dey(mFx,mFy,mFz),dez(mFx,mFy,mFz)
  dimension dextemp(mFx,mFy,mFz),deytemp(mFx,mFy,mFz)
  dimension deztemp(mFx,mFy,mFz)
  dimension sm(-1:1,-1:1,-1:1)

c must zero these arrays - if not severe errors appear!!!
  do k = 1,mFz
    do j = 1,mFy
      do i = 1,mFx
        dextemp(i,j,k) = 0.0
        deytemp(i,j,k) = 0.0
        deztemp(i,j,k) = 0.0
      end do
    end do
  end do
```

```
end do
end do
```

c filtering operates on cells in the "particle core" only

```
do k = FBDLz,FBDRz
do j = FBDLy,FBDRy
do i = FBDLx,FBDRx
do nz = -1,1
do ny = -1,1
do nx = -1,1
dextemp(i+nx,j+ny,k+nz) = dextemp(i+nx,j+ny,k+nz)
& +sm(nx,ny,nz)*dex(i,j,k)
deytemp(i+nx,j+ny,k+nz) = deytemp(i+nx,j+ny,k+nz)
& +sm(nx,ny,nz)*dey(i,j,k)
deztemp(i+nx,j+ny,k+nz) = deztemp(i+nx,j+ny,k+nz)
& +sm(nx,ny,nz)*dez(i,j,k)
end do
end do
end do
end do
```

```
end do
end do
```

```
c ** because of using temporary arrays "dextemp..." guard cells in "dex..." **
c ** contain contributions from the above applied filtering only - **
c ** contributions from current deposition which have been already passed **
c ** are automatically erased **
do k = 1,mFz
do j = 1,mFy
do i = 1,mFx
dex(i,j,k) = dextemp(i,j,k)
dey(i,j,k) = deytemp(i,j,k)
dez(i,j,k) = deztemp(i,j,k)
end do
end do
end do

return
end
```

```
c *****
```

```
  subroutine E_field_update(ex,ey,ez,dex,dey,dez,mFx,mFy,mFz,  
&      FBDLx,FBDLy,FBDLz,FBDRx,FBDRy,FBDRz)
```

```
  integer FBDRx,FBDRy,FBDRz  
  integer FBDLx,FBDLy,FBDLz
```

```
  dimension ex(mFx,mFy,mFz),ey(mFx,mFy,mFz),ez(mFx,mFy,mFz)  
  dimension dex(mFx,mFy,mFz),dey(mFx,mFy,mFz),dez(mFx,mFy,mFz)
```

```
c ** indices range for cells in the "particle core" only - other elements **  
c ** provided by "Field_passing" subroutine; only i-index range is extended to**  
c ** properly update fields in the guard cells of the Left and Right domains **  
  do k = FBDLz,FBDRz  
    do j = FBDLy,FBDRy  
      do i = FBDLx-1,FBDRx+1  
        ex(i,j,k) = ex(i,j,k) + dex(i,j,k)  
        ey(i,j,k) = ey(i,j,k) + dey(i,j,k)  
        ez(i,j,k) = ez(i,j,k) + dez(i,j,k)  
      end do  
    end do  
  end do
```

```
c clear "current" arrays
  do k = 1,mFz
    do j = 1,mFy
      do i = 1,mFx
        dex(i,j,k) = 0.0
        dey(i,j,k) = 0.0
        dez(i,j,k) = 0.0
      end do
    end do
  end do

return
end
```

```
c *****
```

```
c random number generator
```

```
c ** this is ran2 routine from Numerical Recipes (name changed to ran1) **
```

```
  real*8 FUNCTION ran1(idum)
```

```
  INTEGER idum,IM1,IM2,IMM1,IA1,IA2,IQ1,IQ2,IR1,IR2,NTAB,NDIV
```

```
c   REAL ran2,AM,EPS,RNMX
```

```
  REAL AM,EPS,RNMX
```

```
  PARAMETER (IM1=2147483563,IM2=2147483399,AM=1./IM1,IMM1=IM1-1,
```

```
&      IA1=40014,IA2=40692,IQ1=53668,IQ2=52774,IR1=12211,
```

```
&      IR2=3791,NTAB=32,NDIV=1+IMM1/NTAB,EPS=1.2e-7,RNMX=1.-EPS)
```

```
  INTEGER idum2,j,k,iv(NTAB),iy
```

```
  SAVE iv,iy,idum2
```

```
  DATA idum2/123456789/, iv/NTAB*0/, iy/0/
```

```
  if (idum.le.0) then
```

```
    idum=max(-idum,1)
```

```
    idum2=idum
```

```
do j=NTAB+8,1,-1
k=idum/IQ1
idum=IA1*(idum-k*IQ1)-k*IR1
if (idum.lt.0) idum=idum+IM1
if (j.le.NTAB) iv(j)=idum
enddo
iy=iv(1)
endif
```

```
k=idum/IQ1
idum=IA1*(idum-k*IQ1)-k*IR1
if (idum.lt.0) idum=idum+IM1
k=idum2/IQ2
idum2=IA2*(idum2-k*IQ2)-k*IR2
if (idum2.lt.0) idum2=idum2+IM2
j=1+iy/NDIV
iy=iv(j)-idum2
iv(j)=idum
if(iy.lt.1)iy=iy+IMM1
```

```
c   ran2=min(AM*iy,RNMX)
   ran1=min(AM*iy,RNMX)
   return
END
```



```
C *****
C
C      PARTICLE SORTING SUBROUTINES
C *****
```

```
      subroutine Sort_particles(ipar,x,y,z,u,v,w,mh,nFy,nFz,
&                                DHDx,DHDy,DHDz)
```

```
      integer isortZ(3:nFz+2),isortZY(3:nFz+2,3:nFy+2)
```

```
      dimension x(mh),y(mh),z(mh)
      dimension u(mh),v(mh),w(mh)
      dimension temp(mh)
```

```
      dimension indx(mh),indx1(mh),indx2(mh)
```

```
      do j=1,ipar
        indx2(j)=j
        indx1(j)=j
        indx(j)=j
      end do
```

```
do i = 3,nFz+2
  isortZ(i)=0
  do j = 3,nFy+2
    isortZY(i,j)=0
  end do
end do
```

c first sort in "k"

```
call indexx(1,ipar,ipar,DHDz,z,indx2,indx2,indx)
```

c how many elements has each $k=\text{int}(z(\text{indx}(i)))$ of the sorted array?

c e.g., $k=3$ has 10, $k=4$ has 2 etc. elements with j,i still to be sorted

c array "isortZ" records: $\text{isortZ}(3)=10, \text{isortZ}(4)=12$ etc.

```
inz=3
```

```
ismax=0
```

```
do i=1,ipar
```

```
  if (int(z(indx(i)))-DHDz) .eq. inz) then
```

```
    isortZ(inz)=isortZ(inz)+1
```

```
    ismax=max(isortZ(inz),0)
```

```

else
  do j = inz,nFz+1
    inz = inz+1
    if (int(z(indx(i))-DHDz) .eq. inz) then
      isortZ(inz)=ismax+1
      ismax=max(isortZ(inz),0)
      goto 24
    end if
  end do
end if
24  Continue
end do

c then, for given "k" sort in "j"
  ismax=0
  do i = 3,nFz+2
    if ((isortZ(i)-ismax) .gt. 0) then
      call indexx(ismax+1,isortZ(i),ipar,DHDy,y,indx2,indx,indx1)
    end if
    ismax=max(isortZ(i),ismax)
  end do
end do

```

```

inz=3
iny=3
ismax=0
do i=1,ipar
  if (int(z(indx(indx1(i))))-DHDz) .eq. inz) then
    if (int(y(indx(indx1(i))))-DHDy) .eq. iny) then
      isortZY(inz,iny)=isortZY(inz,iny)+1
      ismax=max(isortZY(inz,iny),0)
    else
      do j = iny,nFy+1
        iny = iny+1
        if (int(y(indx(indx1(i))))-DHDy) .eq. iny) then
          isortZY(inz,iny)=isortZY(inz,iny)+1
          ismax=max(isortZY(inz,iny),0)
        go to 25
      end if
    end do
  end if
end if

```

```

else
  iny=3
  do j = inz,nFz+1
    inz = inz+1
    if (int(z(indx(indx1(i))))-DHDz) .eq. inz) then
      if (int(y(indx(indx1(i))))-DHDy) .eq. iny) then
        isortZY(inz,iny)=ismax+1
        ismax=max(isortZY(inz,iny),0)
        go to 25
      else
        do k = iny,nFy+1
          iny = iny+1
          if (int(y(indx(indx1(i))))-DHDy) .eq. iny) then
            isortZY(inz,iny)=ismax+1
            ismax=max(isortZY(inz,iny),0)
            go to 25
          end if
        end do
      end if
    end do
  end if
end do

```

```
    end if
25  Continue
    end do
```

```
c finally, for given "k" and "j" sort in "i"
  ismax=0
  do i = 3,nFz+2
    do j = 3,nFy+2
      if ((isortZY(i,j)-ismax) .gt. 0) then
        call indexx(ismax+1,isortZY(i,j),ipar,DHDx,x,
&                                indx,indx1,indx2)
      end if
      ismax=max(isortZY(i,j),ismax)
    end do
  end do
```

```
c now, rearrange each array using index arrays (requires temporary array)
  do i = 1,ipar
    temp(i) = x(i)
  end do
```

```
do i = 1,ipar
  x(i) = temp(indx(indx1(indx2(i))))
end do
do i = 1,ipar
  temp(i) = y(i)
end do
do i = 1,ipar
  y(i) = temp(indx(indx1(indx2(i))))
end do
do i = 1,ipar
  temp(i) = z(i)
end do
do i = 1,ipar
  z(i) = temp(indx(indx1(indx2(i))))
end do
do i = 1,ipar
  temp(i) = u(i)
end do
do i = 1,ipar
  u(i) = temp(indx(indx1(indx2(i))))
end do
```

```
do i = 1,ipar
  temp(i) = v(i)
end do
do i = 1,ipar
  v(i) = temp(indx(indx1(indx2(i))))
end do
do i = 1,ipar
  temp(i) = w(i)
end do
do i = 1,ipar
  w(i) = temp(indx(indx1(indx2(i))))
end do

return
end
```


c *****

c subroutine from Num. Recipes (Sec. 8.4) constructing index table for array
c being sorted. Changes include: a) sorting in int(arr), b) additional index
c arrays for sorting in k, j, i separately in a way to produce specific
c order the arrays were at the start of simulation --> see "Particle_init"

SUBROUTINE indexx(n1,n2,n,DHD,arr,indx0,indx1,indx)

INTEGER n1,n2,n,indx(n),indx0(n),indx1(n),M,NSTACK

cPIC REAL arr(n)

dimension arr(n)

PARAMETER (M=7,NSTACK=500)

c Indexes an array arr(1:n), i.e., outputs the array indx(1:n) such that

c arr(indx(j)) is in ascending order for $j = 1, 2, \dots, N$. The input

c quantities n and arr are not changed.

INTEGER i,indx0,ir,itemp,j,jstack,k,l,istack(NSTACK)

cPIC REAL a

integer a

```

cPIC      do j=1,n
           do j=n1,n2
             indx(j)=j
           end do
           jstack=0
cPIC      l=1
cPIC      ir=n
           l=n1
           ir=n2
1          if(ir-l.lt.M)then
             do j=l+1,ir
               indxt=indx(j)
cPIC      a=arr(indxt)
             a=arr(indx0(indx1(indxt)))-DHD
             do i=j-1,1,-1
cPIC      if(arr(indx(i)).le.a)goto 2
             if((arr(indx0(indx1(indx(i))))-DHD).le.a)goto 2
             indx(i+1)=indx(i)
             end do
             i=l-1

```

```

2      indx(i+1)=indxt
      end do
      if(jstack.eq.0)return
      ir=istack(jstack)
      l=istack(jstack-1)
      jstack=jstack-2
      else
      k=(1+ir)/2
      itemp=indx(k)
      indx(k)=indx(l+1)
      indx(l+1)=itemp
cPIC   if(arr(indx(l)).gt.arr(indx(ir)))then
      &   if(int(arr(indx0(indx1(indx(l))))-DHD).gt.
      &     int(arr(indx0(indx1(indx(ir))))-DHD))then
      itemp=indx(l)
      indx(l)=indx(ir)
      indx(ir)=itemp
      endif
cPIC   if(arr(indx(l+1)).gt.arr(indx(ir)))then
      &   if(int(arr(indx0(indx1(indx(l+1))))-DHD).gt.
      &     int(arr(indx0(indx1(indx(ir))))-DHD))then

```

```

        itemp=indx(l+1)
        indx(l+1)=indx(ir)
        indx(ir)=itemp
    endif
cPIC    if(arr(indx(l)).gt.arr(indx(l+1)))then
        if(int(arr(indx0(indx1(indx(l))))-DHD).gt.
&      int(arr(indx0(indx1(indx(l+1))))-DHD))then
            itemp=indx(l)
            indx(l)=indx(l+1)
            indx(l+1)=itemp
        endif
        i=l+1
        j=ir
        indxt=indx(l+1)
cPIC    a=arr(indxt)
        a=arr(indx0(indx1(indxt)))-DHD
3      continue
    i=i+1
cPIC    if(arr(indx(i)).lt.a)goto 3
        if((arr(indx0(indx1(indx(i))))-DHD).lt.a)goto 3

```

```

4          continue
      j=j-1
cPIC      if(arr(indx(j)).gt.a)goto 4
          if(int(arr(indx0(indx1(indx(j))))-DHD).gt.a)goto 4
          if(j.lt.i)goto 5
          itemp=indx(i)
          indx(i)=indx(j)
          indx(j)=itemp

          goto 3
5          indx(l+1)=indx(j)
indx(j)=indxl
      jstack=jstack+2
      if(jstack.gt.NSTACK)pause 'NSTACK too small in indexx'
      if(ir-i+1.ge.j-1)then
          istack(jstack)=ir
          istack(jstack-1)=i
      ir=j-1

```

```
else  
  istack(jstack)=j-1  
  istack(jstack-1)=1  
  l=i  
endif  
endif  
goto 1  
END
```

```
C *****
```

```
C      COMMUNICATION SUBROUTINES
```

```
C *****
```

```
      subroutine Field_passing(fx,fy,fz,mFx,mFy,mFz,mc,mrl,mrh,  
&          dims,coords,FBDLx,FBDLy,FBDLz,FBDRx,FBDRy,FBDRz,  
&          nleft,nright,nfront,nrear,nbottom,ntop)  
      include 'mpif.h'
```

```
c      integer myid,Nproc
```

```
      integer lgrp,comm3d,ierror,Tag,istatus(MPI_STATUS_SIZE)
```

```
      integer dims(3),coords(3)
```

```
      integer FBDRx,FBDRy,FBDRz
```

```
      integer FBDLx,FBDLy,FBDLz
```

```
      integer requestx,requesty,requestz
```

```
      integer requestx1,requesty1,requestz1
```

```
      dimension fx(mFx,mFy,mFz),fy(mFx,mFy,mFz),fz(mFx,mFy,mFz)
```

```
      dimension fxs(2:mc,mrl:mrh),fys(2:mc,mrl:mrh),fzs(2:mc,mrl:mrh)
```

```
      dimension fxr(2:mc,mrl:mrh),fyr(2:mc,mrl:mrh),fzr(2:mc,mrl:mrh)
```

common /pparms/ lgrp,comm3d

Tag = 100

c communication is done separately for each dimension, so that number of
c buffer zones is minimal; contributions from edge and corner cells are
c automatically properly passed after the three loops

c attention !!!

c the present version allows for non-cubic domains - the domain sizes in
c y and z-direction must be the same, x-size may vary

c ** to keep minimal number of buffer arrays and minimize communication (pass **
c ** only actual surface points) we change buffer counts in each dimension **
c ** (for non-cubic domains); also data packing (and unpacking) to buffers **
c ** is handled in a way to account for row-wise passing of arrays in MPI **
c !! useful to check if array passing is row-wise when using different MPI !!
c !! implementation !!


```

c periodic boundary conditions for B-fields, that were imposed in 1D version
c in "copylayr" subroutine are now automatically embedded here by making
c grid topology periodic
  do n = 1,3

c send fields to the Right (or Rear or Top)
c pack fields to buffers
  if (n.eq.1) then
    mcount=FBDRy*FBDRz

c ** cell indices passed between domains range from 2 to nFi+3 (nFi=nFx,nFy,..)**
c ** however for leftmost and rightmost domains limits are changed in x-direct.**
c ** because this direction is not periodic: i=1,nFx+3 in leftmost domains and **
c ** i=2,nFx+5 in rightmost domains; because of that "mrl" and "mrh" in buffer **
c ** arrays change depending on position along x-dir.; this works well for **
c ** communication in y and z-dir (loop n=2,3), but problem arises for leftmost**
c ** domains in communication with right neighbors, because buffer arrays **
c ** indexing differs between them and rows are sent starting from k=1 but **
c ** but received from k=2; that's why sent buffers for leftmost domains below **

```

```

c ** copy field arrays with a shift in "k", then they are unpacked properly **
c ** from the receive buffers on the right; this method also ensures proper **
c ** counts for passing!! **
    if (coords(1).eq.0) then
        do k = FBDLz-1,FBDRz+1
            do j = FBDLy-1,FBDRy+1
                fxs(j,k-1) = fx(FBDRx,j,k)
                fys(j,k-1) = fy(FBDRx,j,k)
                fzs(j,k-1) = fz(FBDRx,j,k)
            end do
        end do
    else
        do k = FBDLz-1,FBDRz+1
            do j = FBDLy-1,FBDRy+1
                fxs(j,k) = fx(FBDRx,j,k)
                fys(j,k) = fy(FBDRx,j,k)
                fzs(j,k) = fz(FBDRx,j,k)
            end do
        end do
    end if

```

```
    neighr = nright  
    neighl = nleft  
else if (n.eq.2) then  
    mcount=FBDRz*(FBDRx-FBDLx+3)
```

```
        do i = FBDLx-1,FBDRx+1  
        do k = FBDLz-1,FBDRz+1  
            fxs(k,i) = fx(i,FBDRy,k)  
            fys(k,i) = fy(i,FBDRy,k)  
            fzs(k,i) = fz(i,FBDRy,k)  
        end do  
    end do  
    neighr = nrear  
    neighl = nfront  
else if (n.eq.3) then  
    mcount=FBDRy*(FBDRx-FBDLx+3)
```

```
        do i = FBDLx-1,FBDRx+1  
        do j = FBDLy-1,FBDRy+1
```

```
    fxs(j,i) = fx(i,j,FBDRz)
    fys(j,i) = fy(i,j,FBDRz)
    fzs(j,i) = fz(i,j,FBDRz)
end do
end do
    neighr = ntop
    neighl = nbottom
end if
```

```
call MPI_Irecv(fxr,mcount,MPI_DOUBLE_PRECISION,neighl,Tag+1,
&             comm3d,requestx,ierror)
call MPI_Irecv(fyr,mcount,MPI_DOUBLE_PRECISION,neighl,Tag+2,
&             comm3d,requesty,ierror)
call MPI_Irecv(fzr,mcount,MPI_DOUBLE_PRECISION,neighl,Tag+3,
&             comm3d,requestz,ierror)
```

```
call MPI_Send(fxs,mcount,MPI_DOUBLE_PRECISION,neighr,Tag+1,
&            comm3d,ierror)
call MPI_Send(fys,mcount,MPI_DOUBLE_PRECISION,neighr,Tag+2,
&            comm3d,ierror)
```

```
call MPI_SEND(fzs,mcount,MPI_DOUBLE_PRECISION,neighr,Tag+3,  
&comm3d,ierror)
```

```
call MPI_WAIT(requestx,istatus,ierror)
```

```
call MPI_WAIT(requesty,istatus,ierror)
```

```
call MPI_WAIT(requestz,istatus,ierror)
```

```
c unpack buffers
```

```
  if (n.eq.1 .and. coords(1).ne.0) then
```

```
c !!! do the same for other directions if they are non-periodic !!!
```

```
c ** because boundary conditions in x-direction are non-periodic, processes **
```

```
c ** without neighbors send or receive information to (from) MPI_PROC_NULL **
```

```
c ** upon which receive buffers are not changed; DON'T UNPACK THESE
```

```
c   BUFFERS **
```

```
c ** (buffers from right shift to processes on the left are zeroed arrays **
```

```
c ** and buffers in the left shift to processes on the right are the same **
```

```
c ** as for the right shift) **
```

```
  do k = FBDLz-1,FBDRz+1
```

```
    do j = FBDLy-1,FBDRy+1
```

```
      fx(FBDLx-1,j,k) = fxr(j,k)
```

```
      fy(FBDLx-1,j,k) = fyr(j,k)
```

```
        fz(FBDLx-1,j,k) = fzs(j,k)
    end do
end do
```

```
else if (n.eq.2) then
    do i = FBDLx-1,FBDRx+1
    do k = FBDLz-1,FBDRz+1
        fx(i,FBDLy-1,k) = fxs(k,i)
        fy(i,FBDLy-1,k) = fys(k,i)
        fz(i,FBDLy-1,k) = fzs(k,i)
    end do
end do
```

```
else if (n.eq.3) then
    do i = FBDLx-1,FBDRx+1
    do j = FBDLy-1,FBDRy+1
        fx(i,j,FBDLz-1) = fxs(j,i)
        fy(i,j,FBDLz-1) = fys(j,i)
        fz(i,j,FBDLz-1) = fzs(j,i)
    end do
end do
```

end if

c send fields to the Left (or Front or Bottom)

c pack fields to buffers

if (n.eq.1) then

mcount=FBDRy*FBDRz

do k = FBDLz-1,FBDRz+1

do j = FBDLy-1,FBDRy+1

fxs(j,k) = fx(FBDLx,j,k)

fys(j,k) = fy(FBDLx,j,k)

fzs(j,k) = fz(FBDLx,j,k)

end do

end do

neighr = nright

neighl = nleft

else if (n.eq.2) then

mcount=FBDRz*(FBDRx-FBDLx+3)


```

        do i = FBDLx-1,FBDRx+1
do k = FBDLz-1,FBDRz+1
    fxs(k,i) = fx(i,FBDLy,k)
    fys(k,i) = fy(i,FBDLy,k)
    fzs(k,i) = fz(i,FBDLy,k)
end do
end do
neighr = nrear
    neighl = nfront
else if (n.eq.3) then
    mcount=FBDRy*(FBDRx-FBDLx+3)

        do i = FBDLx-1,FBDRx+1
do j = FBDLy-1,FBDRy+1
    fxs(j,i) = fx(i,j,FBDLz)
    fys(j,i) = fy(i,j,FBDLz)
    fzs(j,i) = fz(i,j,FBDLz)
end do
end do

```



```
    neighr = ntop  
    neighl = nbottom  
end if
```

```
call MPI_Irecv(fxr,mcount,MPI_DOUBLE_PRECISION,neighr,Tag+4,  
& comm3d,requestx1,ierror)  
call MPI_Irecv(fyr,mcount,MPI_DOUBLE_PRECISION,neighr,Tag+5,  
& comm3d,requesty1,ierror)  
call MPI_Irecv(fzr,mcount,MPI_DOUBLE_PRECISION,neighr,Tag+6,  
& comm3d,requestz1,ierror)
```

```
call MPI_Send(fxs,mcount,MPI_DOUBLE_PRECISION,neighl,Tag+4,  
& comm3d,ierror)  
call MPI_Send(fys,mcount,MPI_DOUBLE_PRECISION,neighl,Tag+5,  
& comm3d,ierror)  
call MPI_Send(fzs,mcount,MPI_DOUBLE_PRECISION,neighl,Tag+6,  
& comm3d,ierror)
```

```
call MPI_Wait(requestx1,istatus,ierror)  
call MPI_Wait(requesty1,istatus,ierror)  
call MPI_Wait(requestz1,istatus,ierror)
```

```

c unpack buffers
  if (n.eq.1 .and. coords(1).ne.(dims(1)-1)) then
c ** situation analogous to the right send: field elements sent to leftmost **
c ** processes starting from k=2 are received from k=1 **
    if (coords(1).eq.0) then
      do k = FBDLz-1,FBDRz+1
        do j = FBDLy-1,FBDRy+1
          fx(FBDRx+1,j,k) = fxr(j,k-1)
          fy(FBDRx+1,j,k) = fyr(j,k-1)
          fz(FBDRx+1,j,k) = fzs(j,k-1)
        end do
      end do
    else
      do k = FBDLz-1,FBDRz+1
        do j = FBDLy-1,FBDRy+1
          fx(FBDRx+1,j,k) = fxr(j,k)
          fy(FBDRx+1,j,k) = fyr(j,k)
          fz(FBDRx+1,j,k) = fzs(j,k)
        end do
      end do
    end do
  end do

```

end if

else if (n.eq.2) then

do i = FBDLx-1,FBDRx+1

do k = FBDLz-1,FBDRz+1

fx(i,FBDRy+1,k) = fxr(k,i)

fy(i,FBDRy+1,k) = fyr(k,i)

fz(i,FBDRy+1,k) = fzs(k,i)

end do

end do

else if (n.eq.3) then

do i = FBDLx-1,FBDRx+1

do j = FBDLy-1,FBDRy+1

fx(i,j,FBDRz+1) = fxr(j,i)

fy(i,j,FBDRz+1) = fyr(j,i)

fz(i,j,FBDRz+1) = fzs(j,i)

end do

end do

end if

end do

return

end