

Theory of STM on Unconventional Superconductors

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Copenhagen, Denmark

UNIVERSITÄT LEIPZIG



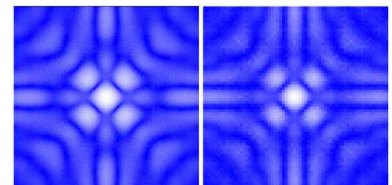
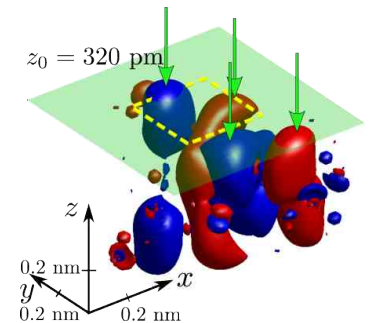
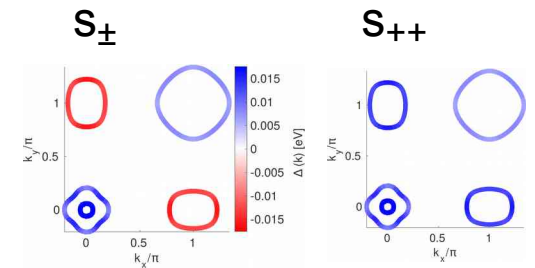
KØBENHAVNS
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UF UNIVERSITY of
FLORIDA
The Foundation for The Gator Nation

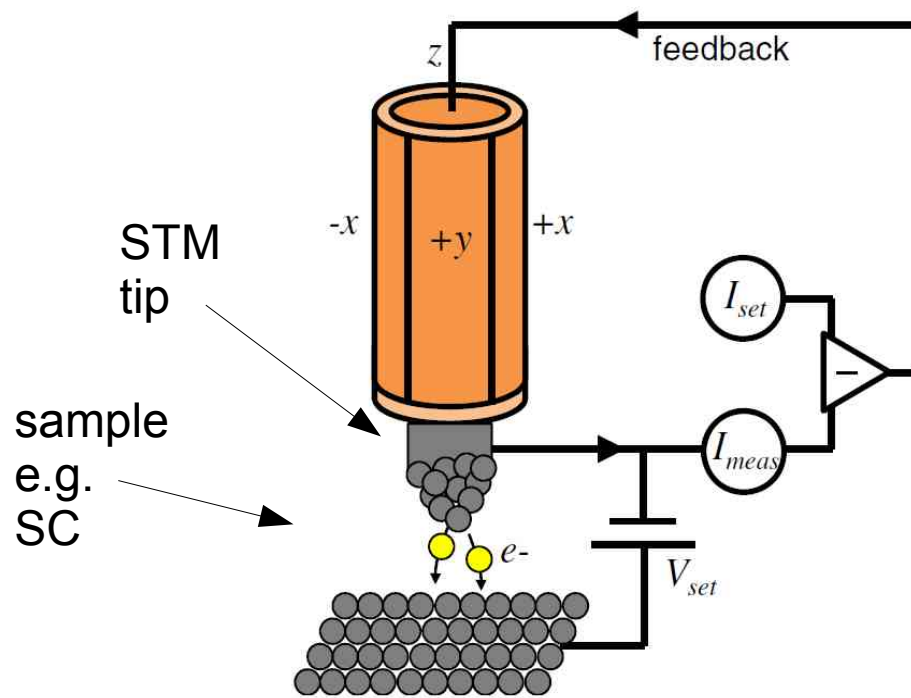
P. Choubey, *et al.*, Phys. Rev. B **90**, 134520 (2014)
A. Kreisel, *et al.*, Phys. Rev. Lett. **114**, 217002 (2015)
A. Kreisel, *et al.*, Phys. Rev. B **94**, 224518 (2016)
P. Choubey, *et al.*, Phys. Rev. B **96**, 174523 (2017)

Outline

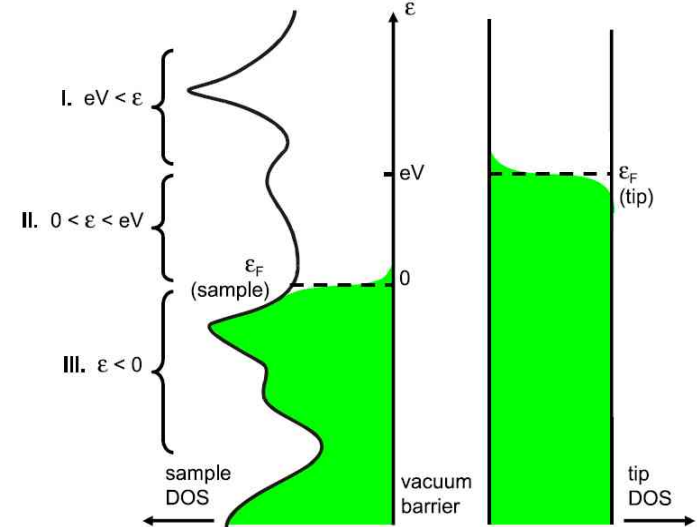
- Motivation
 - STM: impurities as probe for electronic structure, order parameter and more
 - layered superconductors, complications
- Theoretical methods to investigate impurity physics in superconductors
 - using wavefunction information in layered superconductors: Wannier method
 - Applications
 - LiFeAs (multiband, s-wave)
 - Cuprates: $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$, $\text{Ca}_2\text{CuO}_2\text{Cl}_2$
- Inelastic tunneling



Scanning tunneling microscopy



J. Hoffman Rep. Prog. Phys. **74** 124513 (2011)

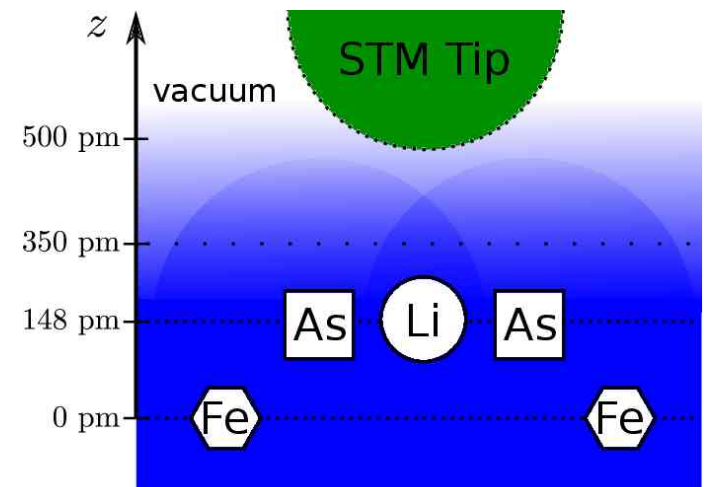


Tunneling current:

$$I(V, x, y, z) = -\frac{4\pi e}{\hbar} \rho_t(0) |M|^2 \int_0^{eV} \rho(x, y, z, \epsilon) d\epsilon$$

Local Density Of States (LDOS)
of sample at given energy **at the tip position**

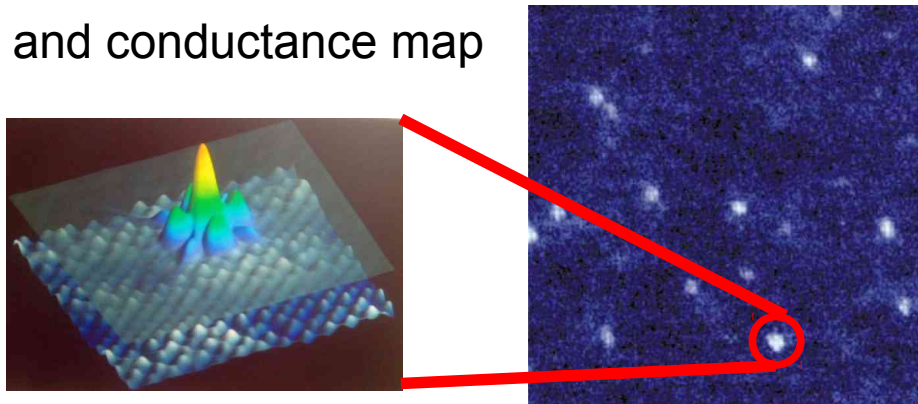
J. Tersoff and D. R. Hamann, PRB **31**, 805 (1985)



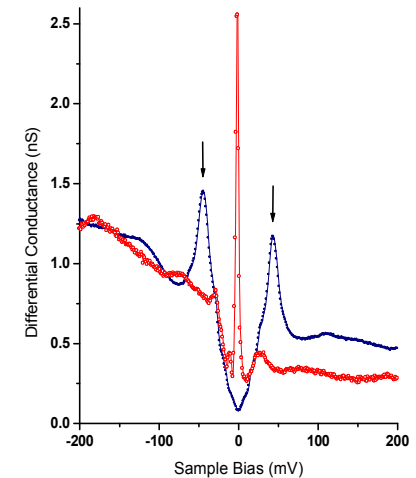
STM: examples

- Cuprates: Zn impurity in BSCCO

spectra and conductance map

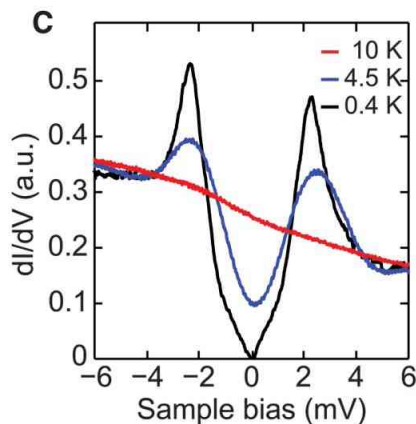


Pan et al., Nature **403**, 746 (2000)

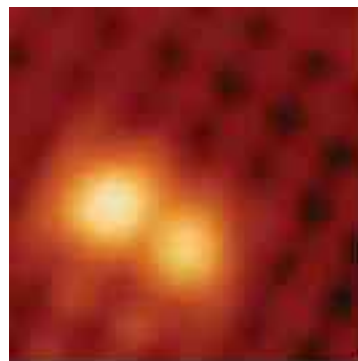


- Fe-SC

FeSe: topograph of Fe centered impurity

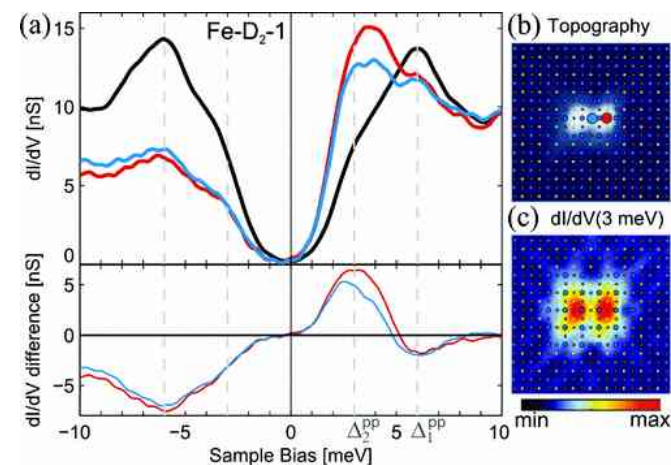


Song et al., Science **332**, 1410 (2011)



Can-Li Song, et al. PRL **109**, 137004 (2012)

LiFeAs: Fe centered impurity



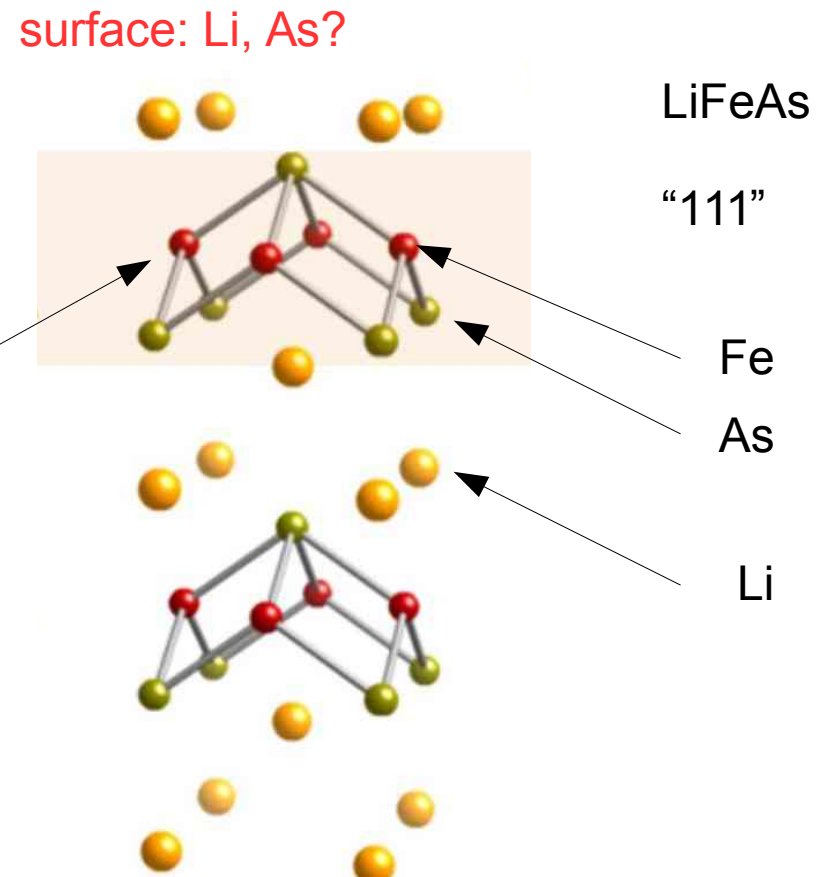
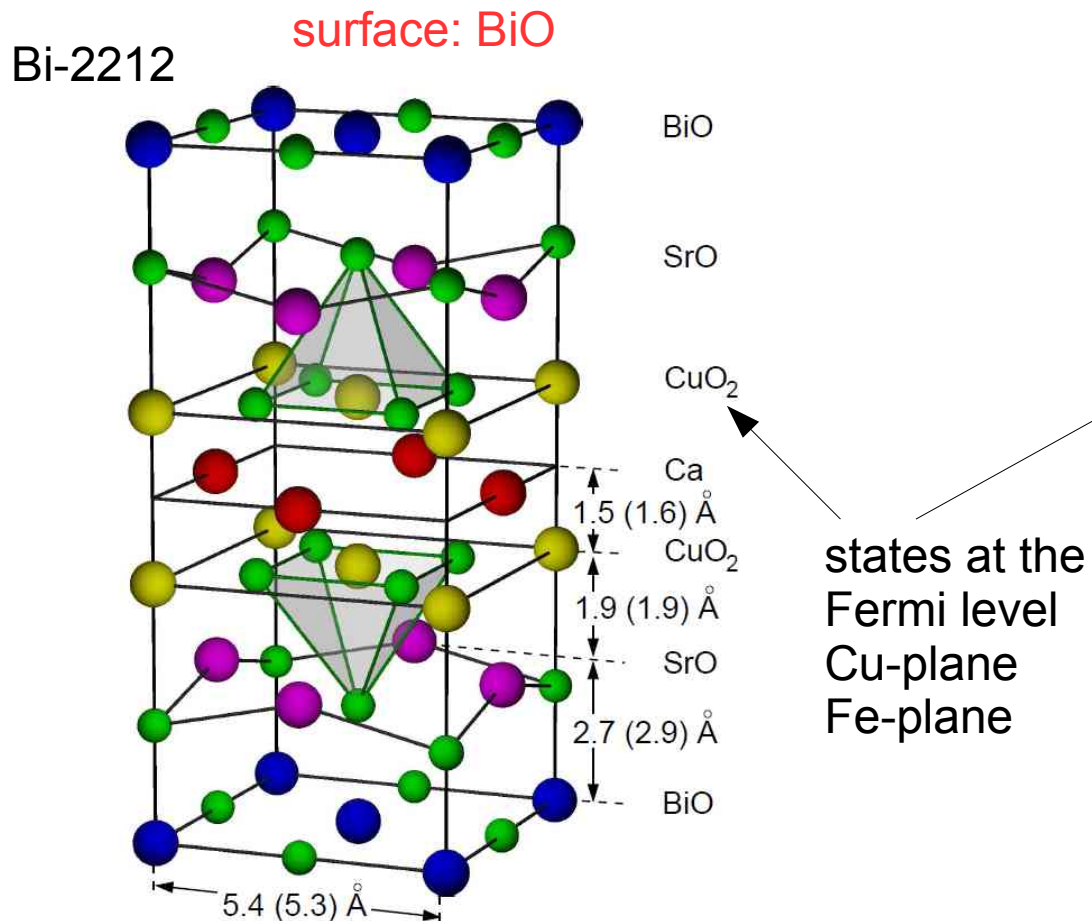
S. Grothe, et al., PRB **86**, 174503 (2012)

Layered superconductors

- 2 examples: surface atoms $\neq$ superconducting layer

Cuprates

Iron based superconductors



Theoretical approaches: Cuprates

- LDOS: impurity in d-wave superconductor
 - local LDOS: 4 fold pattern
 - low energy bound state

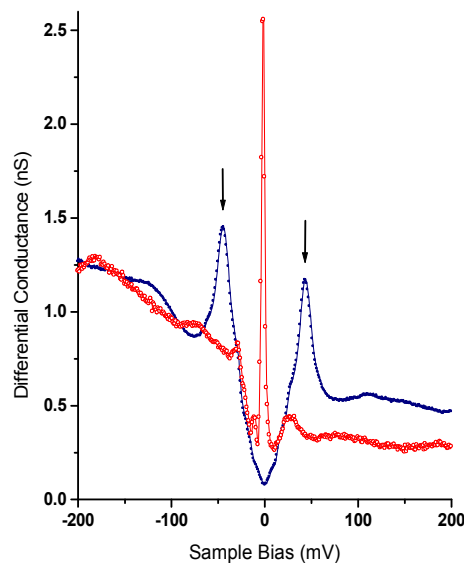
$$\Omega \equiv \Omega' + i\Omega'' = \Delta_0 \frac{\pi c/2}{\ln(8/\pi c)} \left[1 + \frac{i\pi}{2} \frac{1}{\ln(8/\pi c)} \right]$$

J. M. Byers, M. E. Flatté, and D. J. Scalapino Phys. Rev. Lett. **71**, 3363 (1993)

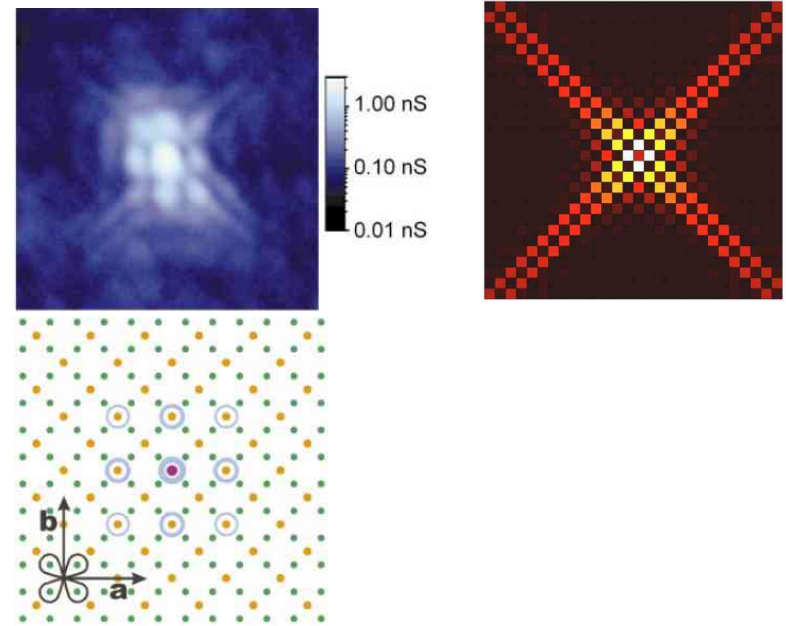
A. V. Balatsky, M. I. Salkola, and A. Rosengren Phys. Rev. B **51**, 15547 (1995)

Stamp, Journal of Magnetism and Magnetic Materials, **63**, 429 - 431 (1987) (p-wave)

- Comparison to experiment



Pan et al., Nature **403**, 746 (2000)



Theoretical approaches: Cuprates

- LDOS: impurity in d-wave superconductor
 - local LDOS: 4 fold pattern
 - low energy bound state

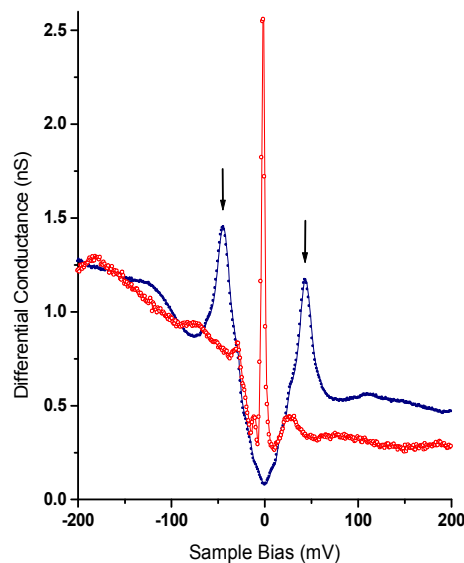
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J. M. Byers, M. E. Flatté, and D. J. Scalapino Phys. Rev. Lett. **71**, 3363 (1993)

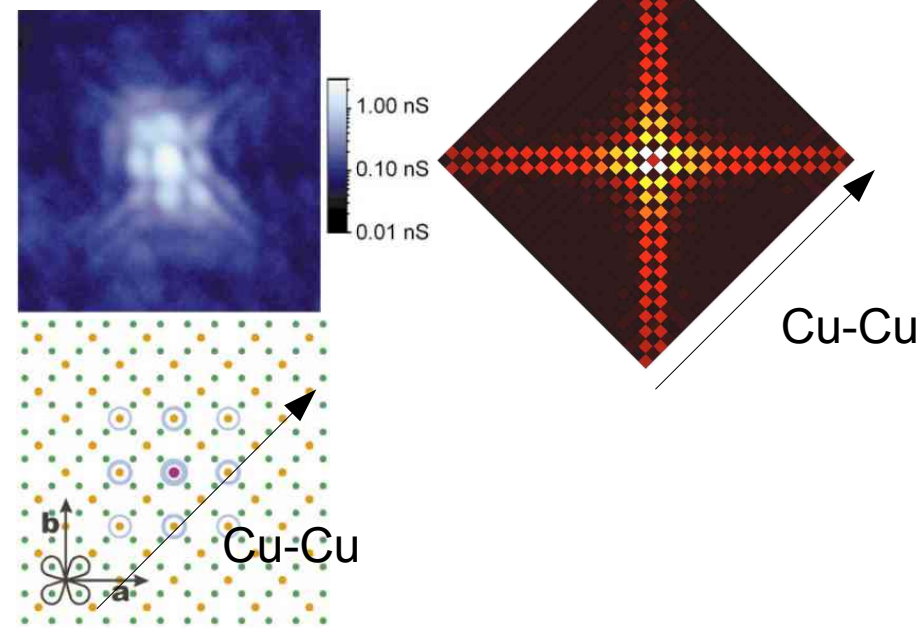
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Pan et al., Nature **403**, 746 (2000)

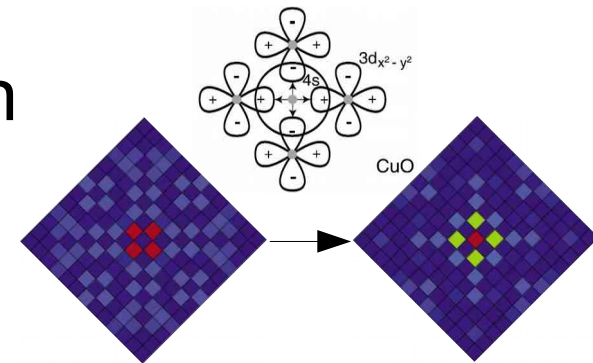


Theoretical approaches: Cuprates

- extended impurity potentials (magnetic Ni impurity) Jian-Ming Tang and Michael E. Flatté PRB **66**, 060504(R) (2002)

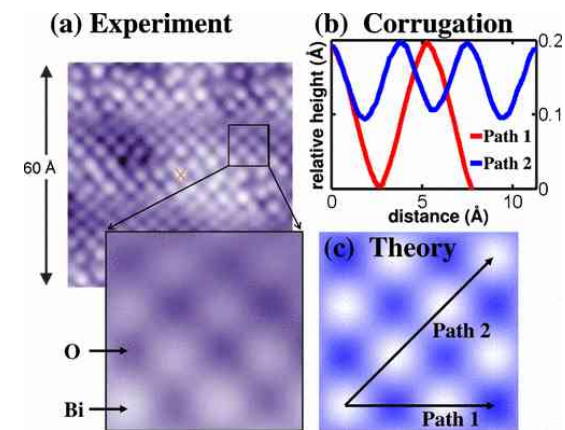
- Correlations: “Kondo screening” (magnetic impurity) Anatoli Polkovnikov PRB **65**, 064503 (2002)

- “Filter function”: STM tip probes states in the superconducting layer by tunneling matrix elements Martin *et al.*, PRL **88**, 097003 (2002)



- Large tight binding basis set of orbitals + Greens function method to calculate tunneling matrix elements

J. Nieminen, *et al.*, PRB **80**, 134509 (2009)



Theoretical approaches: Fe-SC

- Identification of nature of impurities in FeSe monolayer (non-SC) by ab-initio calculations

Dennis Huang et al., Nano Lett., **16** (7), 4224 (2016)

- Inelastic tunneling

- coupling to bosonic mode
- signatures of spin fluctuations (real space)

S. Chi, et al., Nat. Commun. **8**, 15996 (2017)

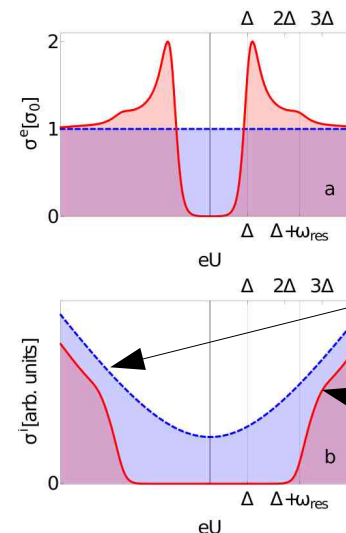
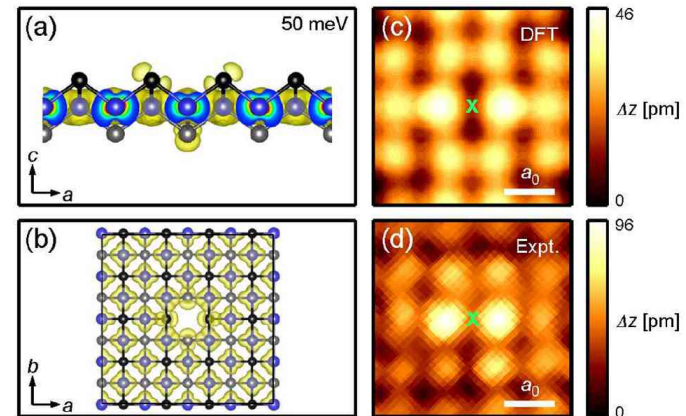
- Wannier method (this talk)

See also: “holographic maps”

Dalla Torre, He, Demler
Nat. Phys., **12**, 1052 (2016)

$$h_G(q, V) = g(q, V)g^*(q + G, V)$$

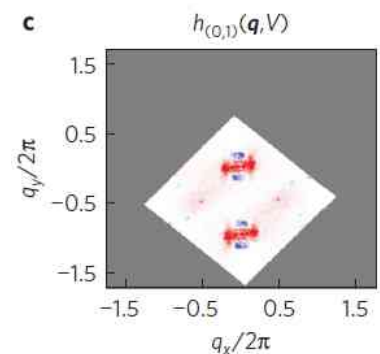
unravel intra-unitcell
information



J. R. Kirtley and D. J. Scalapino, PRL **65**, 798 (1990); J. R. Kirtley, PRB **47**, 11379 (1993)
P. Hlobil, et al., Phys. Rev. Lett. **118**, 167001 (2017)

normal state

superconducting state



Wannier method: example LiFeAs

- Ab-initio calculation

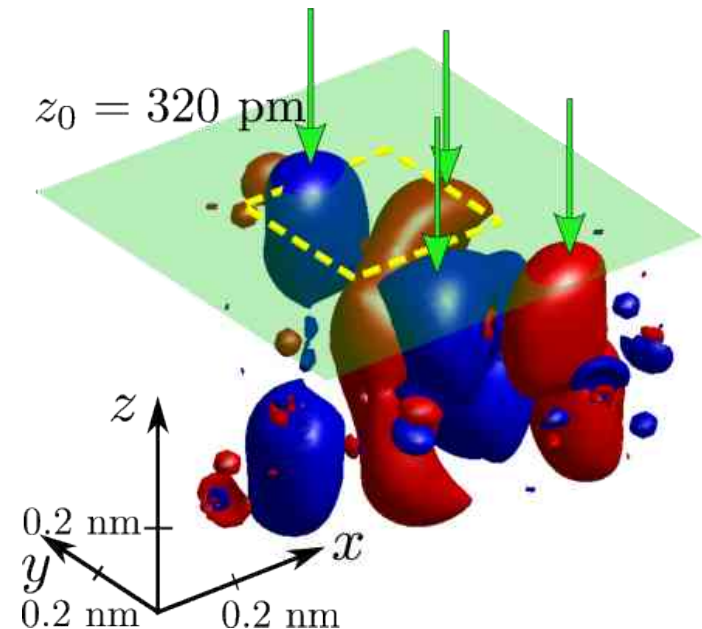
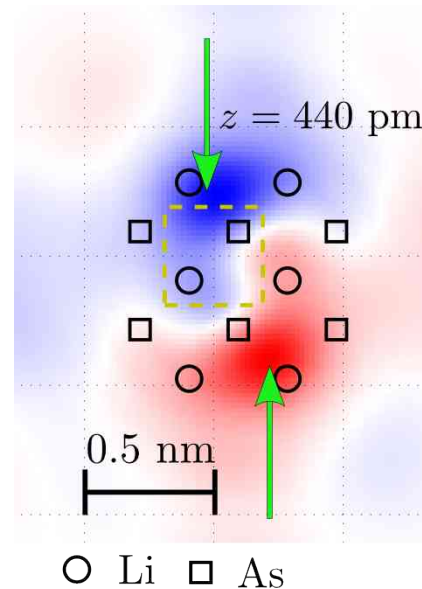
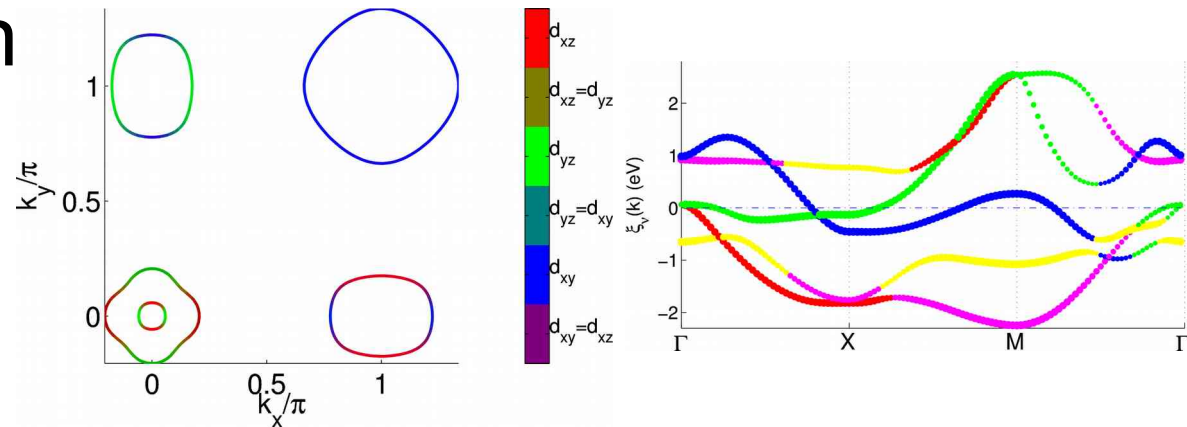
- band structure

5 band model

$$H_0 = \sum_{\mathbf{R}\mathbf{R}',\sigma} t_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\sigma}^\dagger c_{\mathbf{R}'\sigma}$$

$$- \mu_0 \sum_{\mathbf{R},\sigma} c_{\mathbf{R}\sigma}^\dagger c_{\mathbf{R}\sigma}$$

- Wannier functions (including glide plane symmetry)



Superconductivity

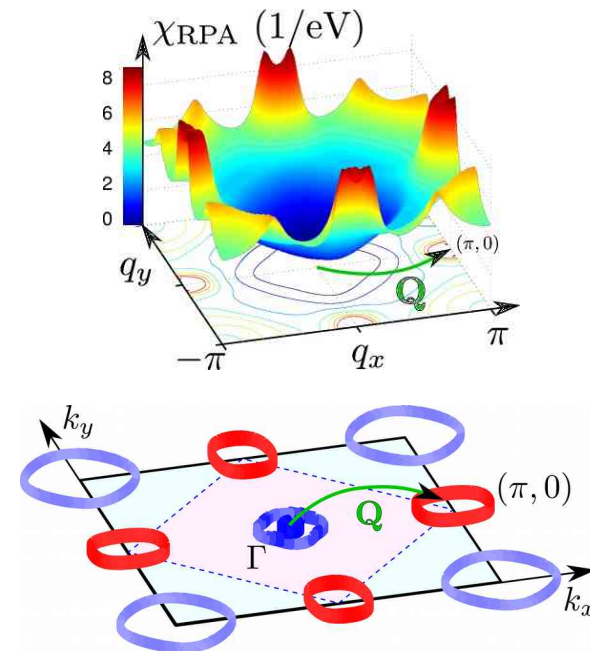
- superconducting order parameter from spin- fluctuation theory

$$H_{\text{BCS}} = - \sum_{\mathbf{R}, \mathbf{R}'} \Delta_{\mathbf{R}\mathbf{R}'} c_{\mathbf{R}\uparrow}^{\dagger} c_{\mathbf{R}'\downarrow}^{\dagger} + H.c.,$$

- calculate Green's function in superconducting state

$$H_{\text{Nambu}} = \begin{pmatrix} H_k & \Delta_k \\ \Delta_k^{\dagger} & -H_{-k} \end{pmatrix}$$

$$G_0(\mathbf{k}, \omega) = [\omega - H_{\text{Nambu}} + i0^+]^{-1}$$



Real space Greens function by Fourier transform

Impurity $\rightarrow$ engineered

- ab-initio calculation of impurity potential for Co, Ni, Mn in LiFeAs (engineered impurity)

$$H = H_0 + H_{\text{BCS}} + H_{\text{imp}}$$

$$H_{\text{imp}} = \sum_{\sigma} V_{\text{imp}} c_{\mathbf{R}^* \sigma}^{\dagger} c_{\mathbf{R}^* \sigma}$$

- T-matrix approach to obtain Green's function other methods also possible
 - BdG
 - Gutzwiller mean field

Kreisel et al., Phys. Rev. Lett. **114**, 217002 (2015)
Choubey et al., New J. Phys. **19**, 013028 (2017)

$$\underline{\hat{G}}_{\mathbf{R}, \mathbf{R}'}(\omega) = \underline{\hat{G}}_{\mathbf{R}-\mathbf{R}'}^0(\omega) + \underline{\hat{G}}_{\mathbf{R}}^0(\omega) \underline{\hat{T}}(\omega) \underline{\hat{G}}_{-\mathbf{R}'}^0(\omega)$$

$$\underline{\hat{T}}(\omega) = [1 - \underline{\hat{V}}_{\text{imp}} \underline{\hat{G}}(\omega)]^{-1} \underline{\hat{V}}_{\text{imp}}$$

lattice Green function
(state of the art)

cLDOS

- Basis transformation $\psi_\sigma(\mathbf{r}) = \sum_{\mathbf{R}\mu} c_{\mathbf{R}\mu\sigma} w_{\mathbf{R}\mu}(\mathbf{r})$

$$\underline{\hat{G}}_{\mathbf{R},\mathbf{R}'}(\omega) = \underline{\hat{G}}_{\mathbf{R}-\mathbf{R}'}^0(\omega) + \underline{\hat{G}}_{\mathbf{R}}^0(\omega) \underline{\hat{T}}(\omega) \underline{\hat{G}}_{-\mathbf{R}'}^0(\omega)$$

surface Wannier
function with phases

$$\underline{G}(\mathbf{r}, \mathbf{r}'; \omega) = \sum_{\mathbf{R}, \mathbf{R}', \mu\nu} \underline{\hat{G}}_{\mathbf{R}, \mathbf{R}'}^{\mu, \nu}(\omega) w_{\mathbf{R}\mu}(\mathbf{r}) w_{\mathbf{R}'\nu}(\mathbf{r}')$$

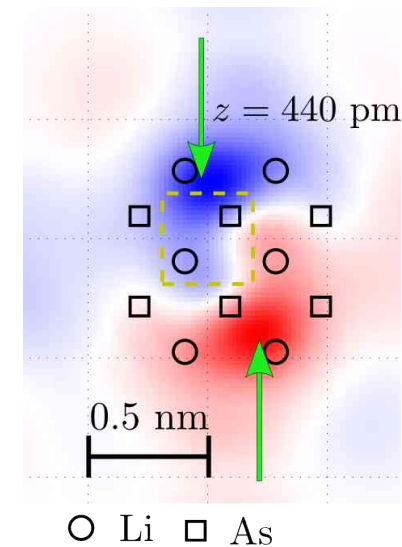
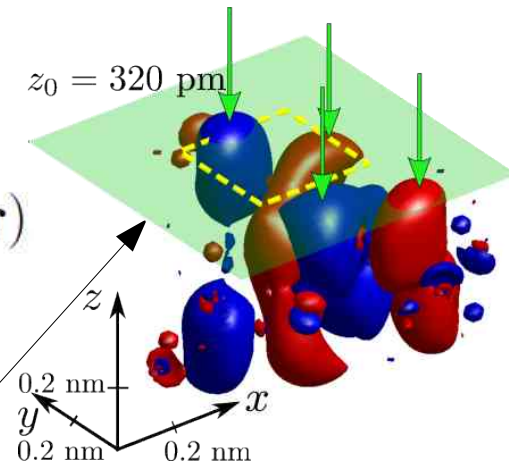
continuum position

nonlocal contributions

lattice Green function

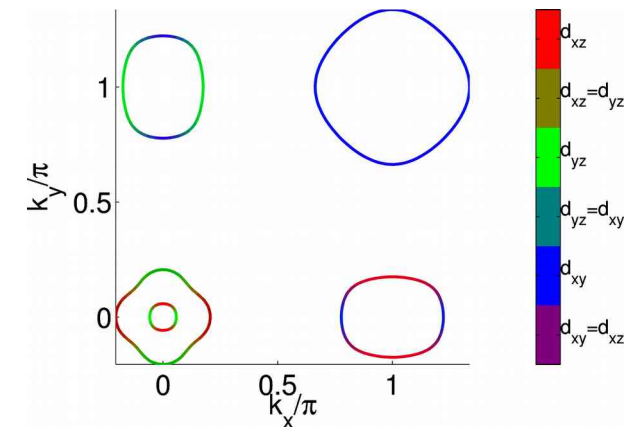
continuum Local Density Of States (cLDOS)
of sample at given energy **at the tip position**

$$\rho(r, \omega) \equiv -\frac{1}{\pi} \text{Im } G(\mathbf{r}, \mathbf{r}; \omega)$$



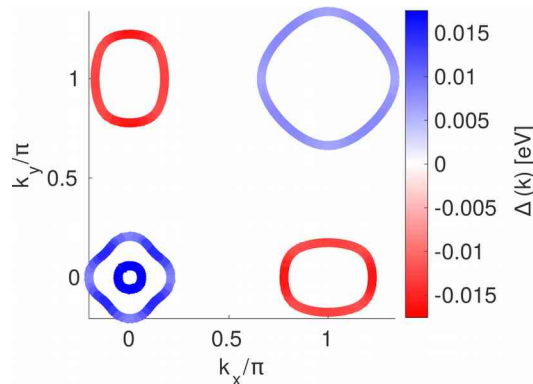
LiFeAs: Questions

- Properties of the order parameter (sign-change)



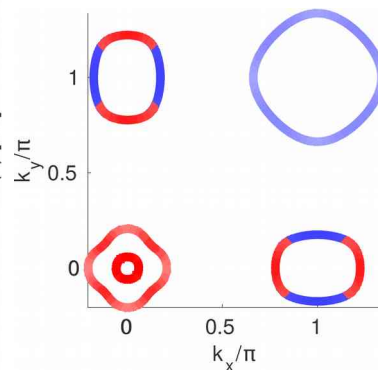
conventional $s_{\pm}$

Y. Wang, A. Kreisel, et al.,
Phys. Rev. B **88**, 174516 (2013)
A. Kreisel, et al., Phys. Rev. B **95**,
174504 (2017)



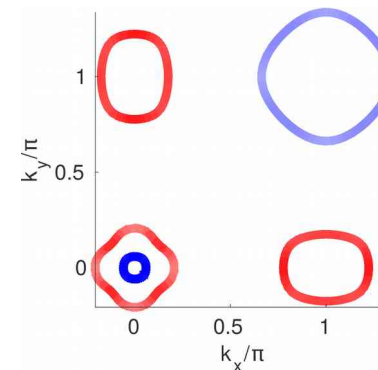
antiphase $s_{\pm}$

Z. P. Yin, K. Haule, G. Kotliar
Nature Physics **10**, 845 (2014)



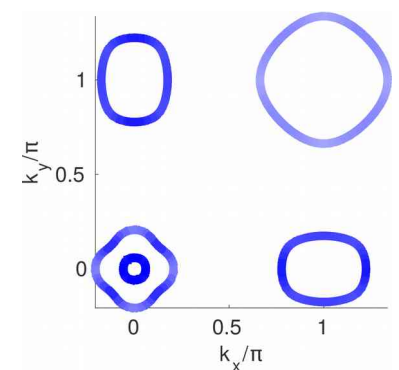
novel $s_{\pm}$

F. Ahn, et al., Phys. Rev. B **89**, 144513
(2014)



conventional s_{++}

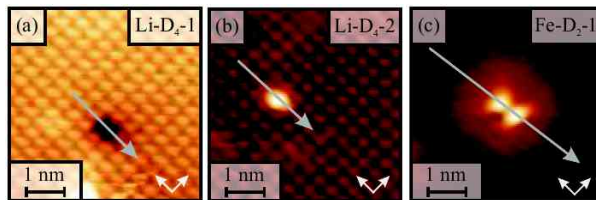
T. Saito, et al. Phys. Rev. B **90**,
035104 (2014)



LiFeAs: Questions

- Interpretation of
 - impurity shapes

R. Schlegel, et al., Phys. Status Solidi B, **254**: 1600159 (2017)

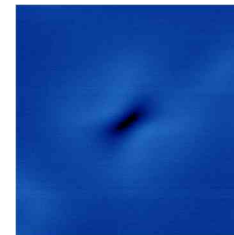


Hanaguri, unpublished (KITP 2011)

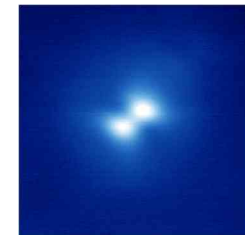
“Dot”



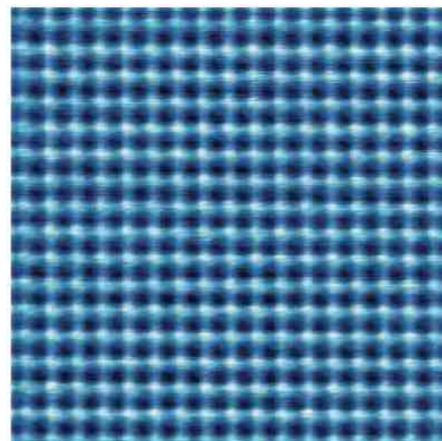
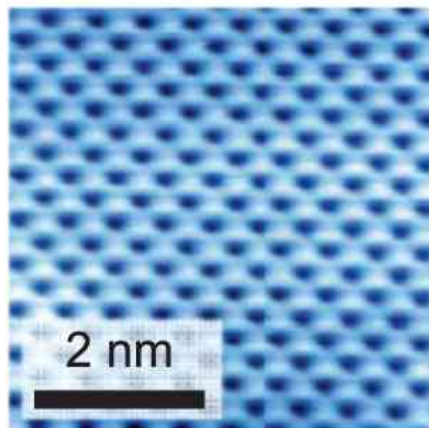
“Trench”



“Dumbbell”

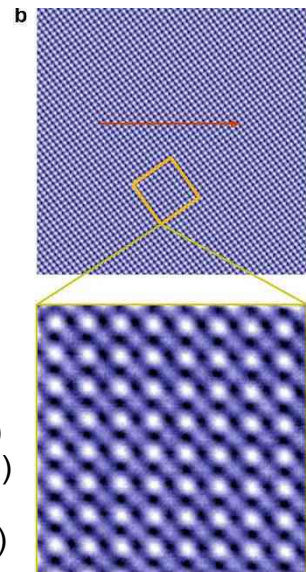


- registered “surface lattice” in STM



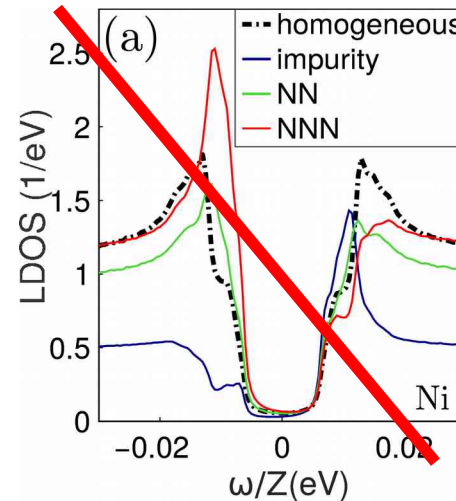
LiFeAs: Li or As lattice?

Shun Chi, et al., PRL **109**, 087002 (2012)
 T. Hanaguri, et al. PRB **85**, 214505 (2012)
 S. Grothe, et al., PRB **86**, 174503 (2012)
 J. -X. Yin, et al., arXiv, 1602.04949 (2016)

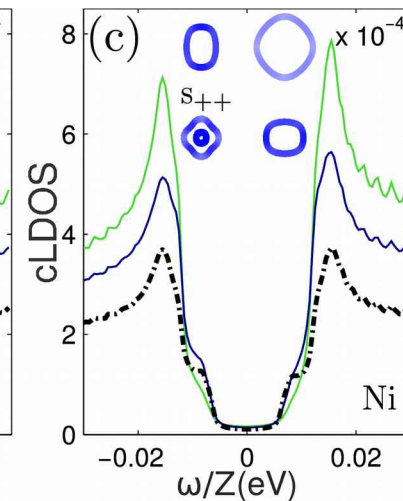
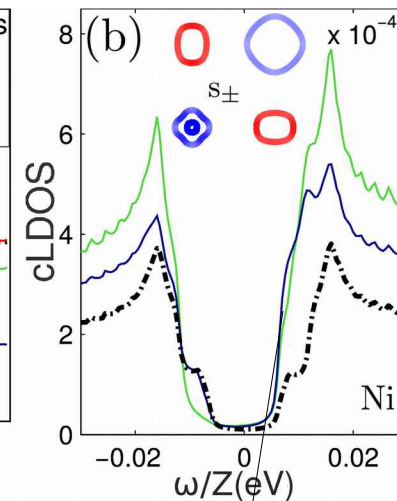


LiFeAs: spectra

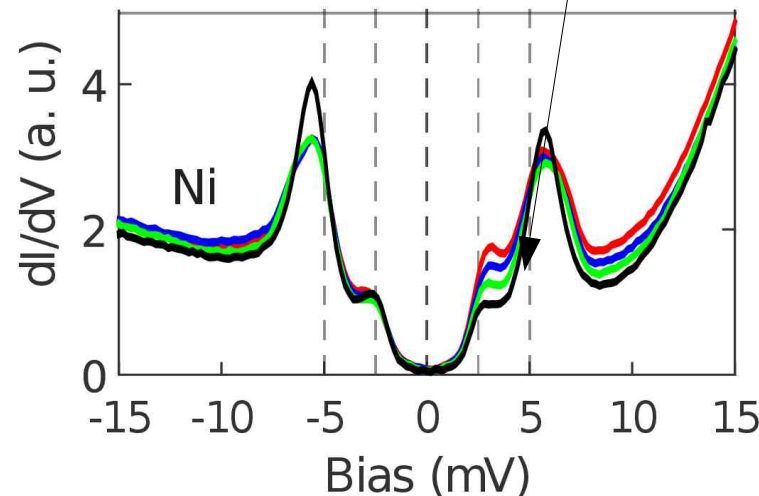
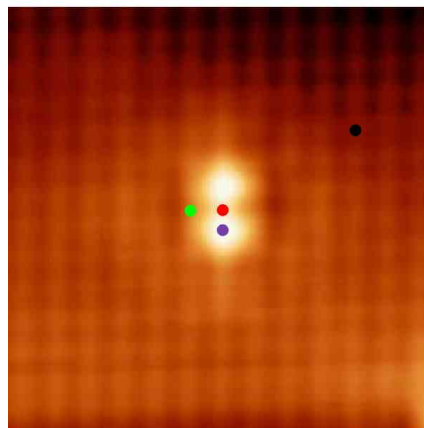
- evidence for sign-changing order parameter by in-gap state with engineered impurity



conventional calculation:
lattice LDOS: strong
response at negative bias



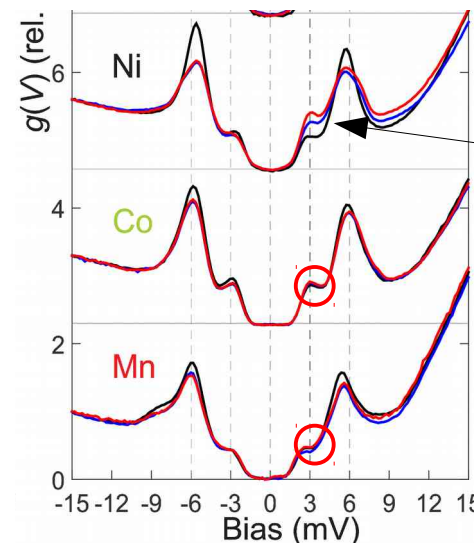
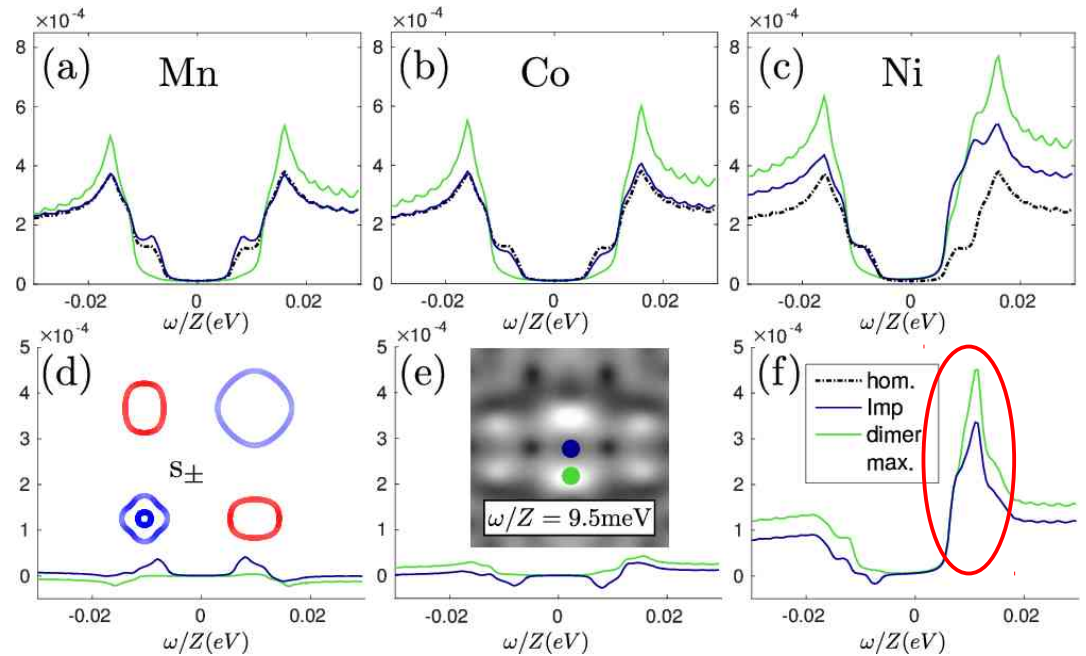
$$0 \approx 1 - V_{\text{imp}}^{\mu\mu} G_{\mathbf{R}=0}^0(\omega)^{\mu\mu}$$



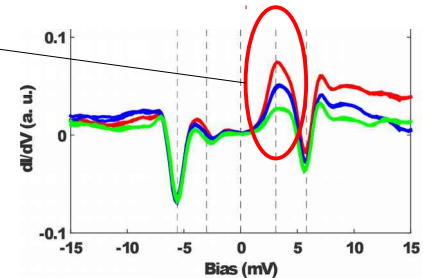
S. Chi, (...), **A. Kreisel**,
et al. Phys. Rev. B **94**,
134515 (2016)

LiFeAs: spectra

- sequence of impurity potentials from ab-initio calculation correct, but overall renormalization downwards required [correlation effects]



relative spectra
Ni impurity



P. O. Sprau, ..., A. Kreisel, et al., Science, **357**, 75 (2017)

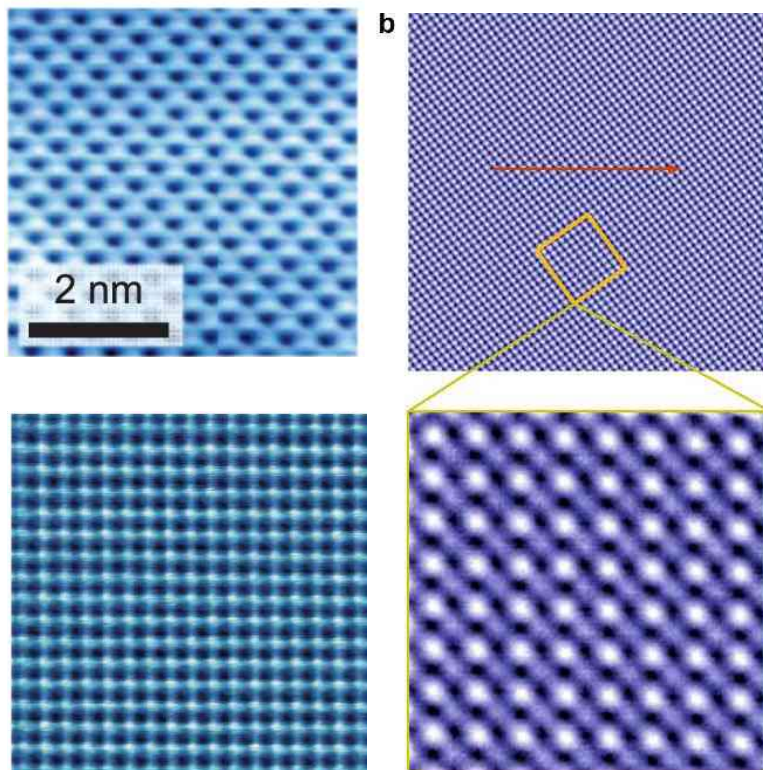
A. Kreisel, et al., Phys. Rev. B **95**, 174504 (2017)

A. Kostin, et al., arXiv:1802.02266

S. Chi, (...) , A. Kreisel, et al.
Phys. Rev. B **94**, 134515 (2016)

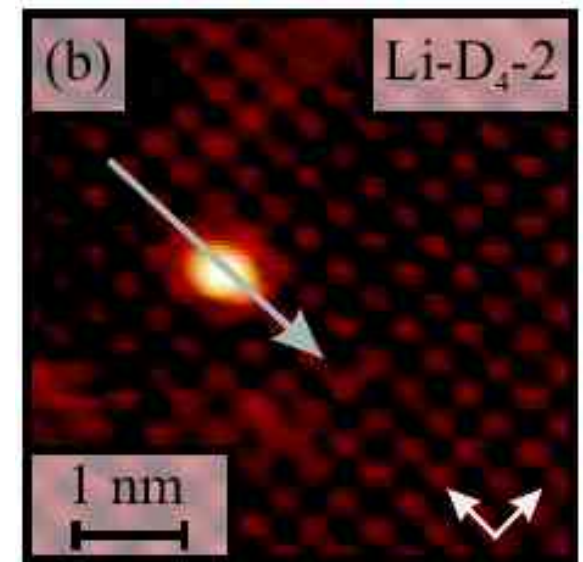
Height and current dependence of topographs

- experiment: Li or As lattice?



Shun Chi, et al., PRL 109, 087002 (2012)
T. Hanaguri, et al. PRB 85, 214505 (2012)
S. Grothe, et al., PRB 86, 174503 (2012)
J. -X. Yin, et al., arXiv, 1602.04949 (2016)

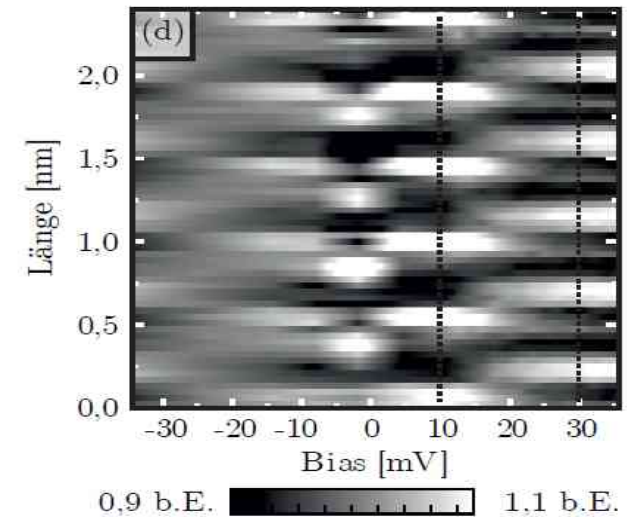
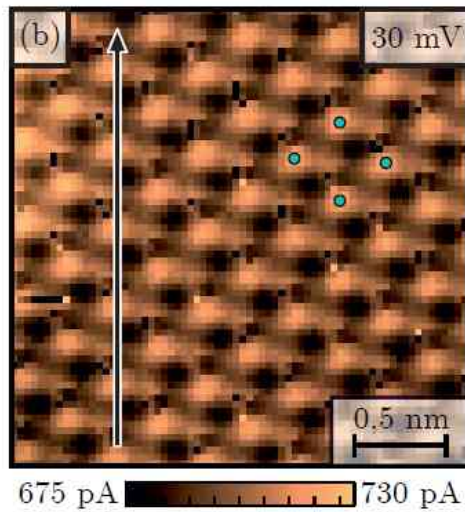
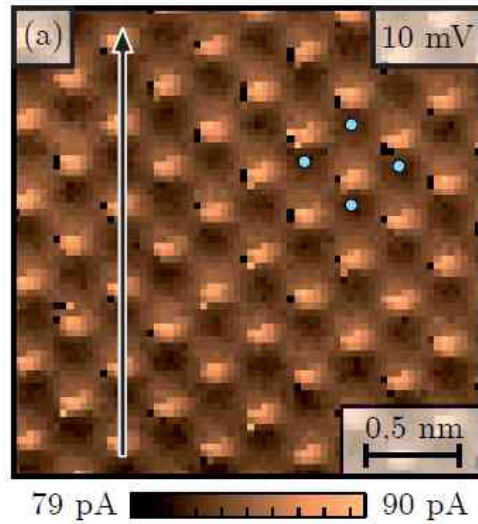
height maxima at Li
positions!?
counter-intuitive from
chemistry point of view



R. Schlegel, et al., Phys. Status
Solidi B, **254**: 1600159 (2017)

Further experimental evidences?

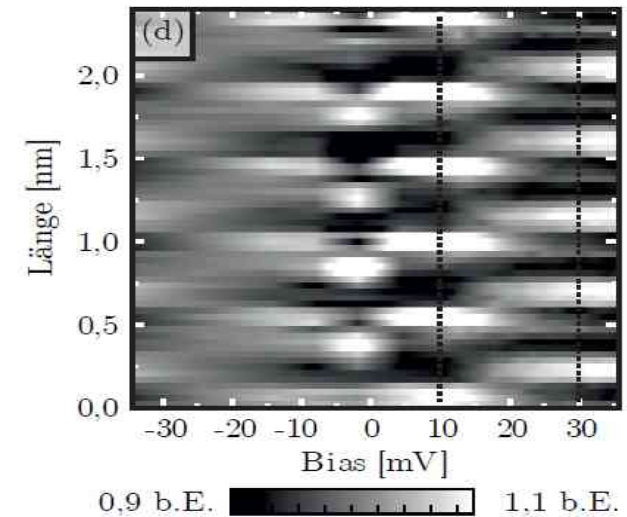
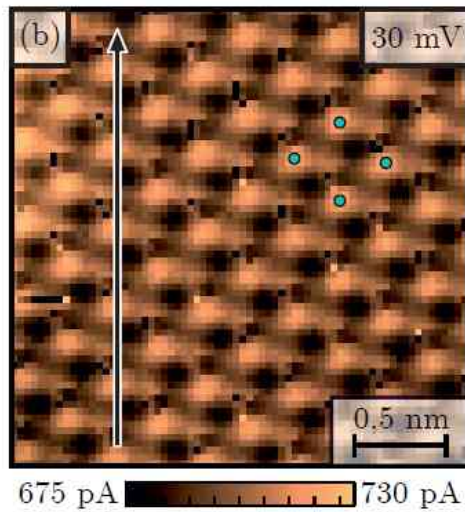
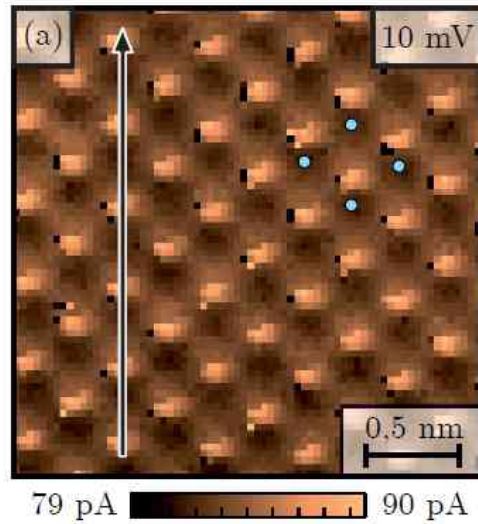
experiment (current maps)



Ronny Schlegel, Dissertation, TU Dresden
(thanks to C. Hess)

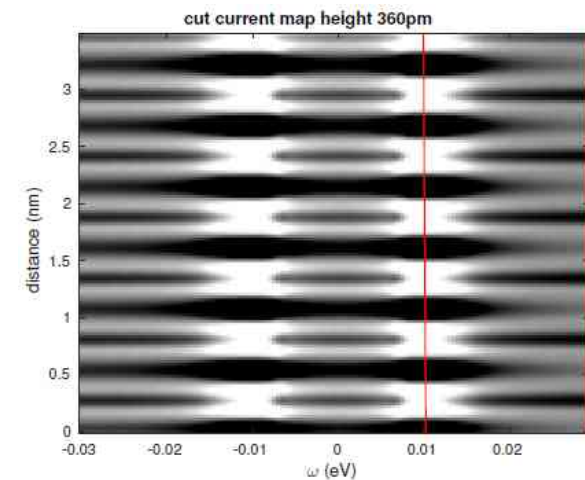
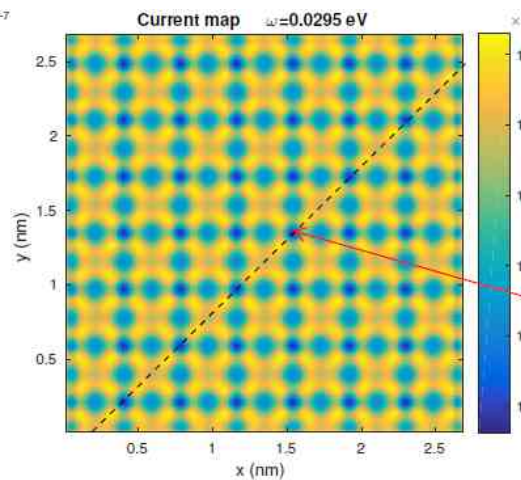
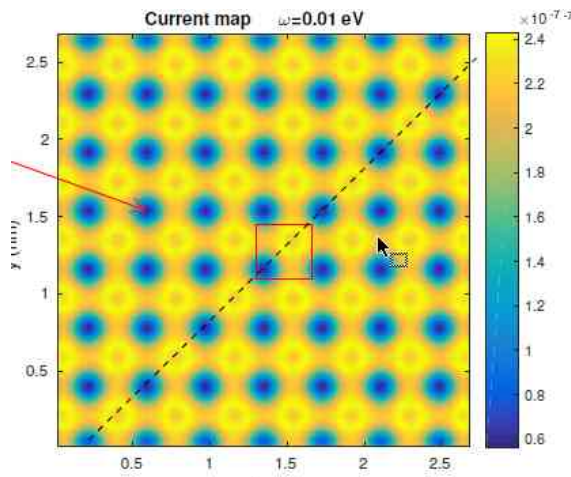
Further experimental evidences?

experiment (current maps)



Ronny Schlegel, Dissertation, TU Dresden
(thanks to C. Hess)

theory

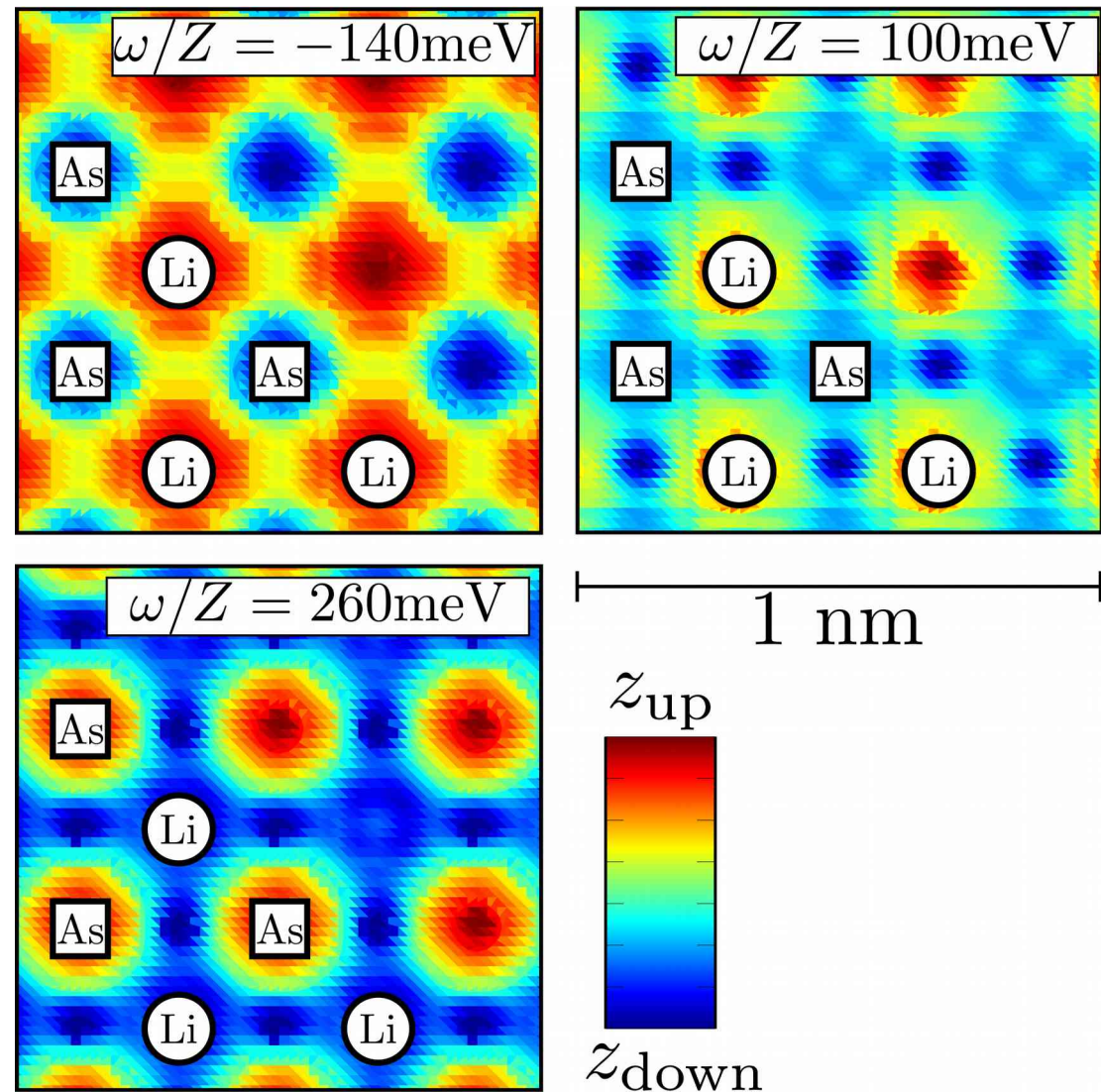


Simulation of topographs

- solve for $z(x, y)$

$$I_0 = \frac{4\pi e}{\hbar} \rho_t(0) |M|^2 \int_0^{eV} d\omega \rho(x, y, z(x, y), \omega)$$

- switching of height maxima as a function of bias voltage



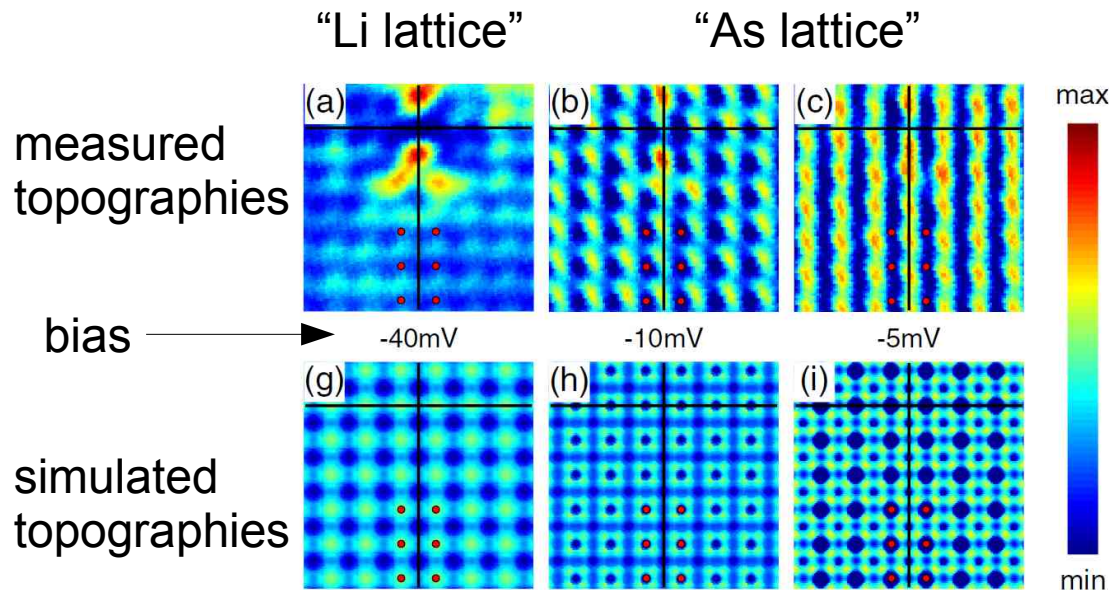
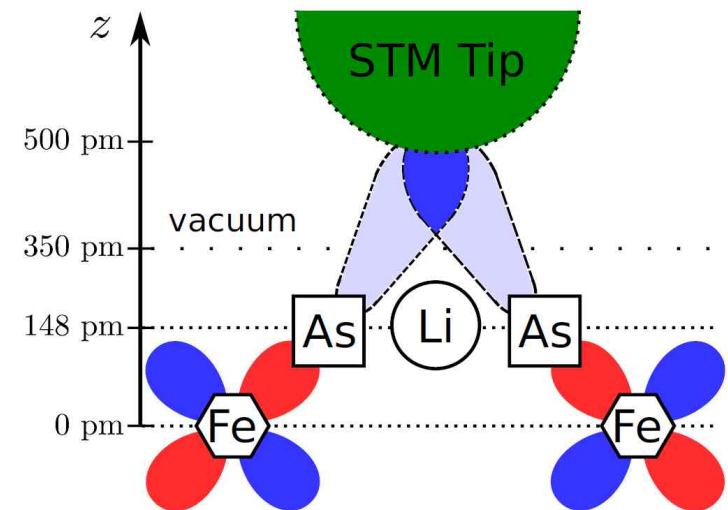
Results

registered surface lattice in STM

- tunneling into states described by Wannier functions

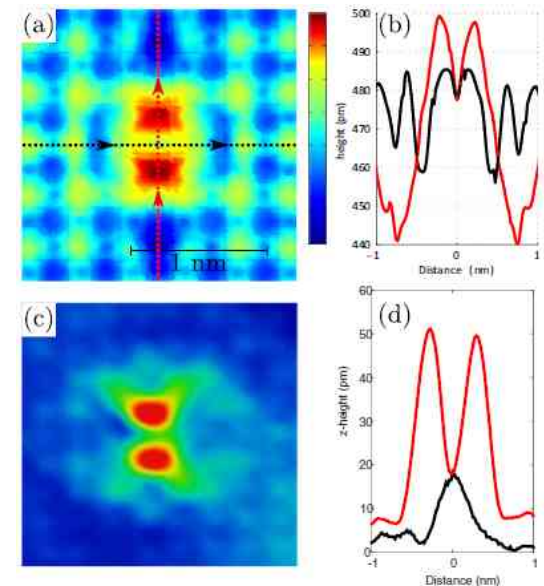
$$G(\mathbf{r}, \mathbf{r}'; \omega) = \sum_{\mu, \nu, \mathbf{R}, \mathbf{R}'} G(\mathbf{R}, \mu, \mathbf{R}', \nu; \omega) w_{\mathbf{R}, \mu}(\mathbf{r}) w_{\mathbf{R}', \nu}^*(\mathbf{r}')$$

- registered lattice switches as function of bias and current



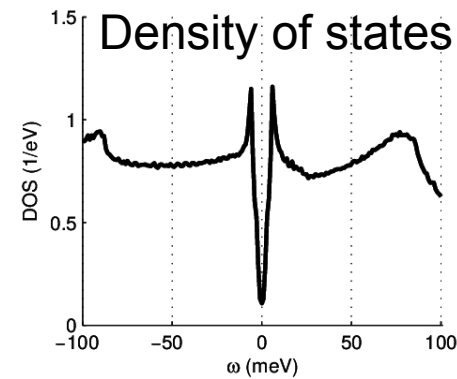
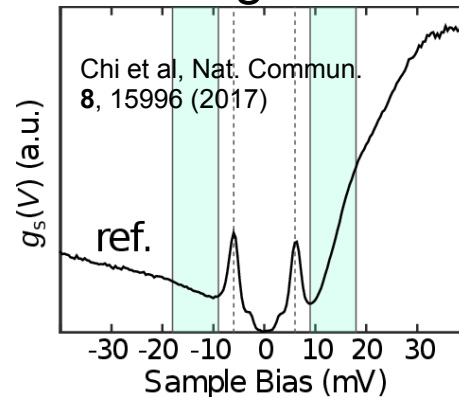
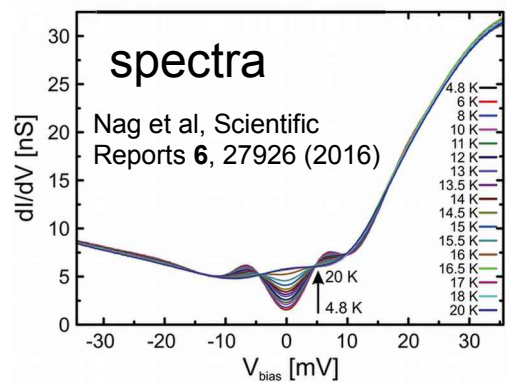
simulated topography close to strong imp.

measured topography close to Ni



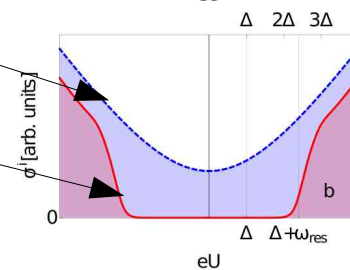
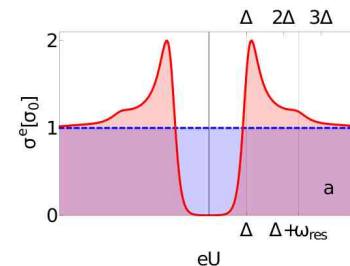
Inelastic tunneling

- well known property
increasing conductance at large bias



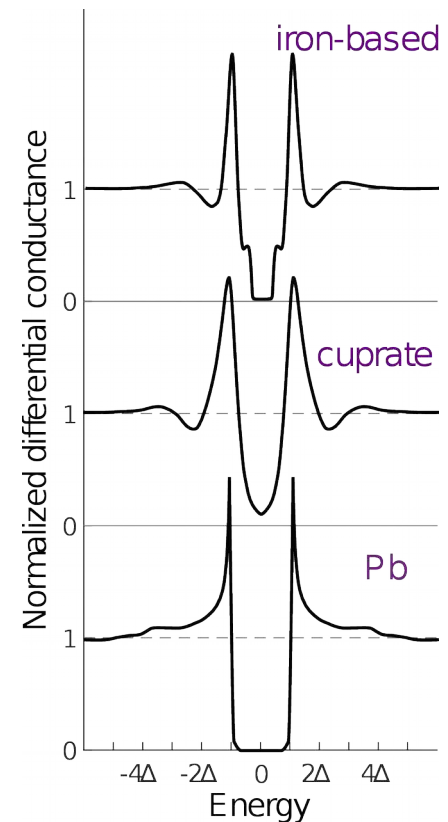
- deduction of collective modes?

$$g_{\text{tot}}(\omega) = g_{\text{el}}(\omega) + g_{\text{inel}}(\omega)$$



normal state

superconducting state



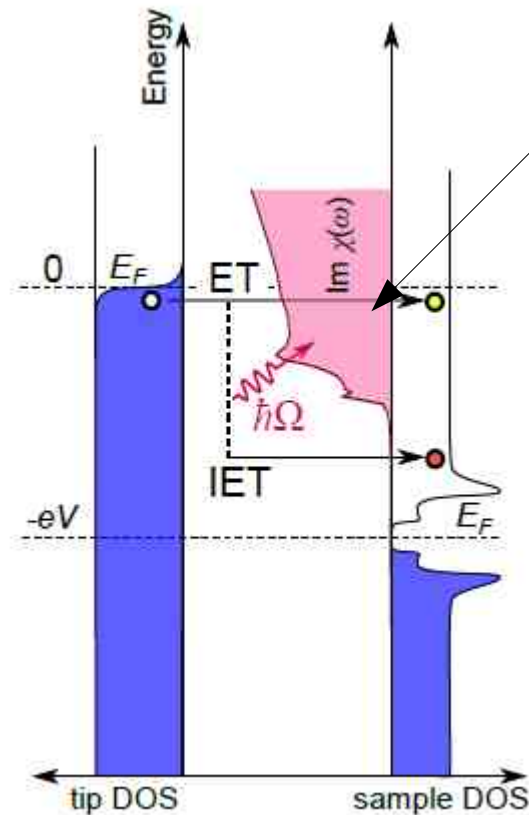
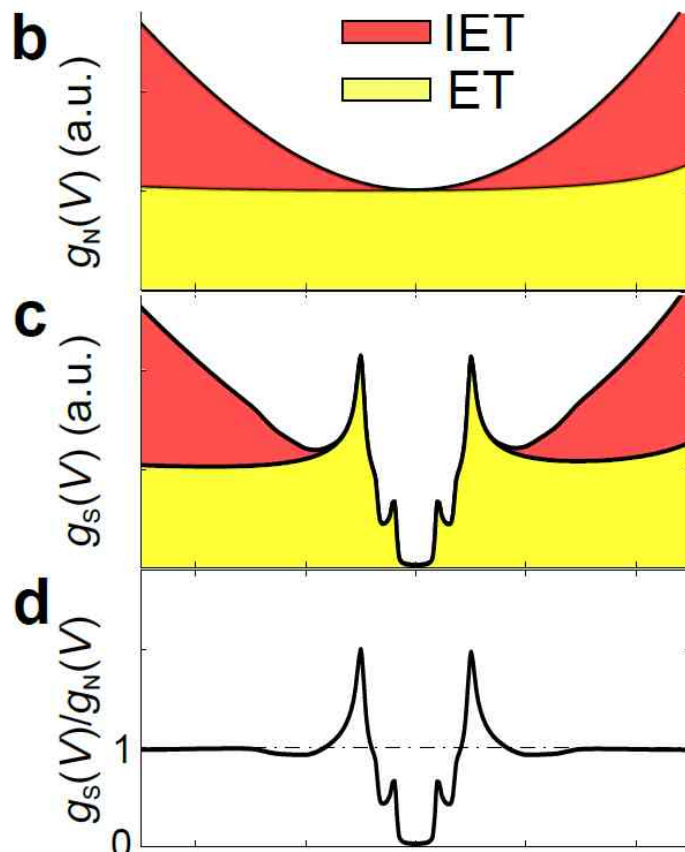
J. R. Kirtley and D. J. Scalapino, PRL **65**, 798 (1990); J. R. Kirtley, PRB **47**, 11379 (1993)
P. Hlobil, et al., Phys. Rev. Lett. **118**, 167001 (2017)

Inelastic tunneling in FeSC: coupling to spin fluctuations

- Inelastic contribution

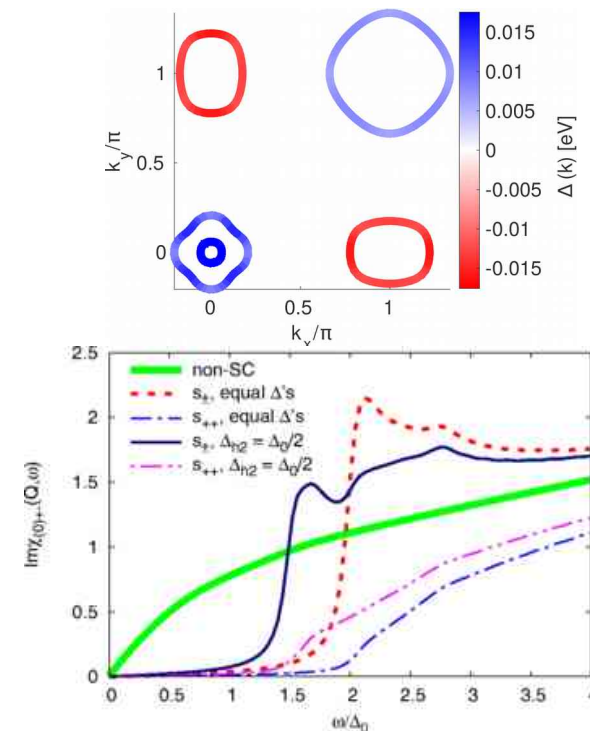
$$g_{\text{inel}}(V) \propto \int_0^{eV} \chi(\omega) \rho(eV - \omega) d\omega$$

- Dip-hump feature



J. R. Kirtley and D. J. Scalapino, PRL **65**, 798 (1990); J. R. Kirtley, PRB **47**, 11379 (1993)
P. Hlobil, et al., Phys. Rev. Lett. **118**, 167001 (2017)

Spin fluctuations:
two gap
superconductor
(LiFeAs), double
resonance



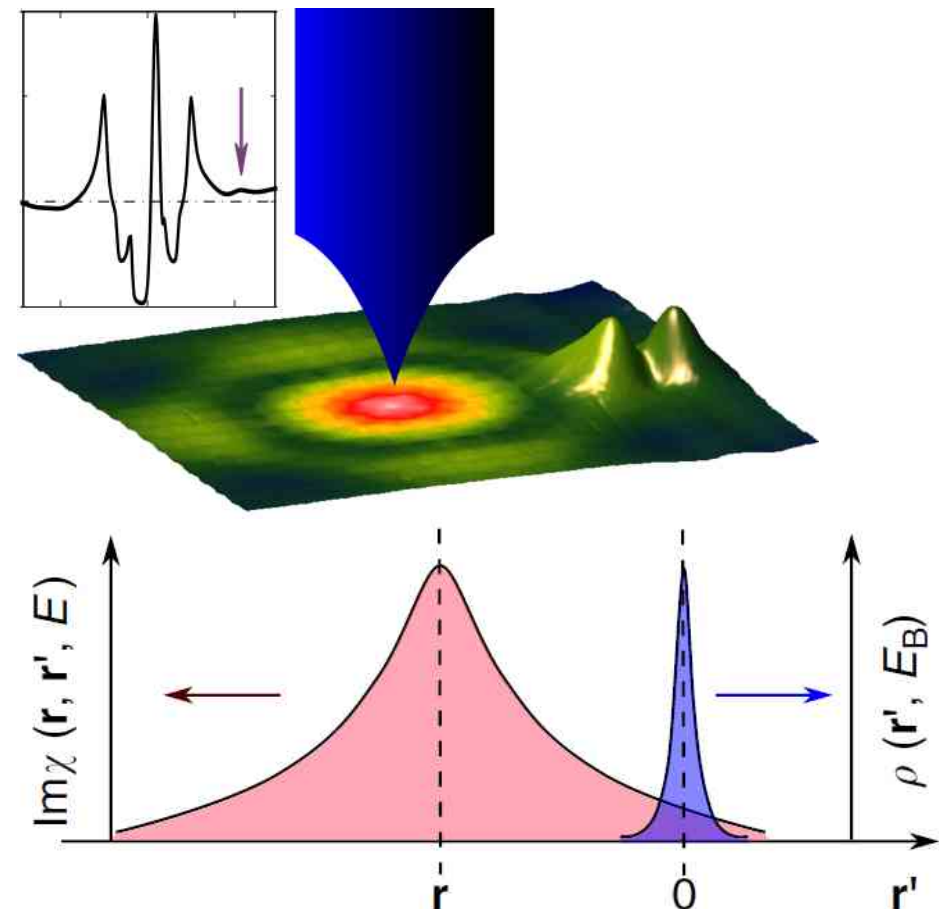
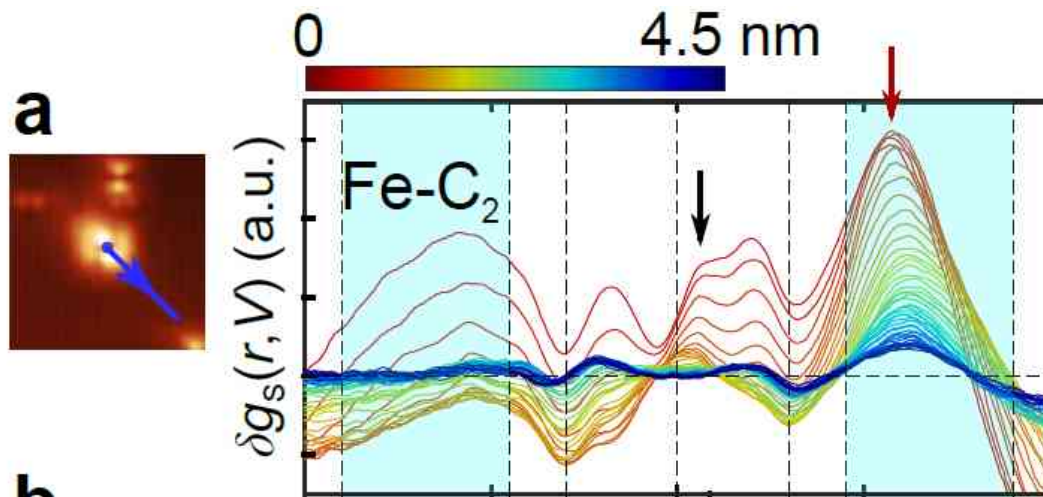
M. M. Korshunov, et al., Phys. Rev. B **94**, 094517 (2016)

Imaging spin fluctuations in real space

- real space structure $g_{\text{inel}}(\mathbf{r}, V) \propto \int_0^{eV} \int \rho(\mathbf{r}', eV - \omega) \chi(\mathbf{r}, \mathbf{r}', \omega) d\mathbf{r}' d\omega$

S. Chi, (...) AK, et al., Nat. Commun. **8**, 15996 (2017)

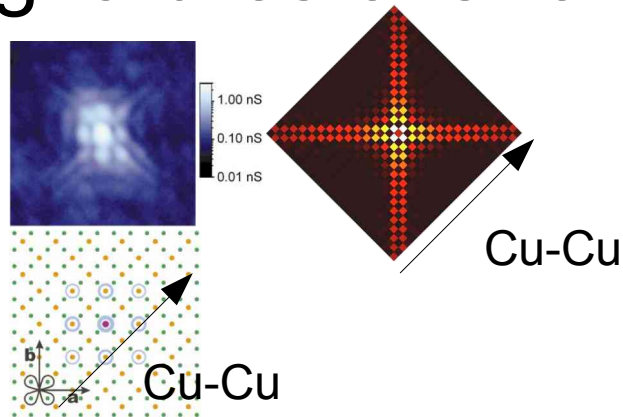
- in presence of impurity



Fast spatial decay of impurity resonance, slow decay of dip-hump → spin fluctuations (real space)

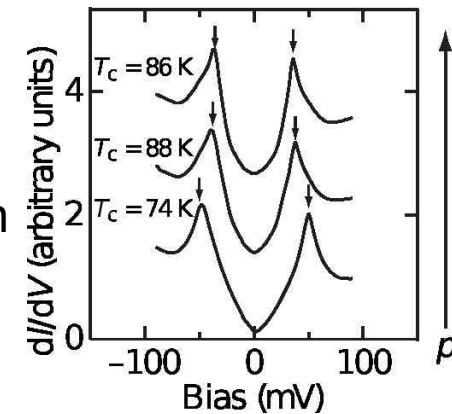
Cuprates: Questions

- signatures of strong impurity in d-wave SC

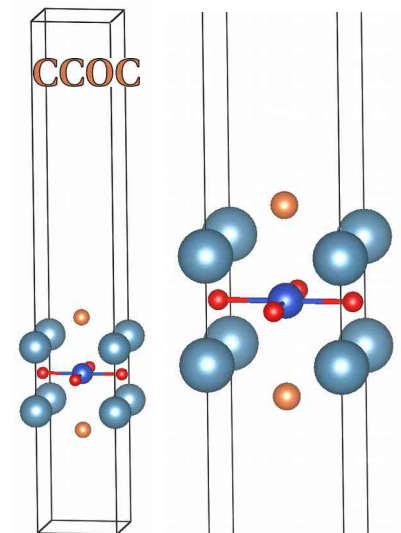
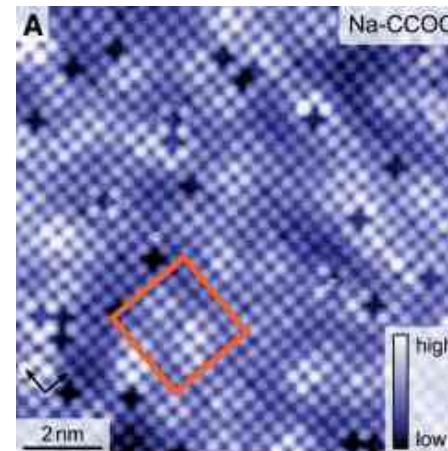
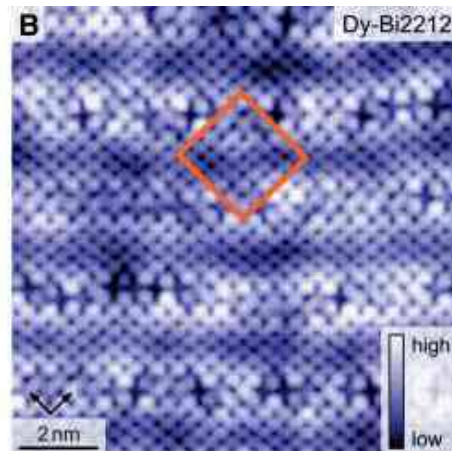
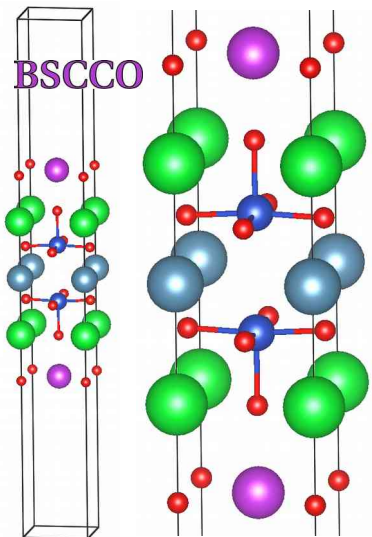


Kohsaka et al. Nature,
454, 1072 (2008)

Crossover between
U-shaped and
V-shaped spectra

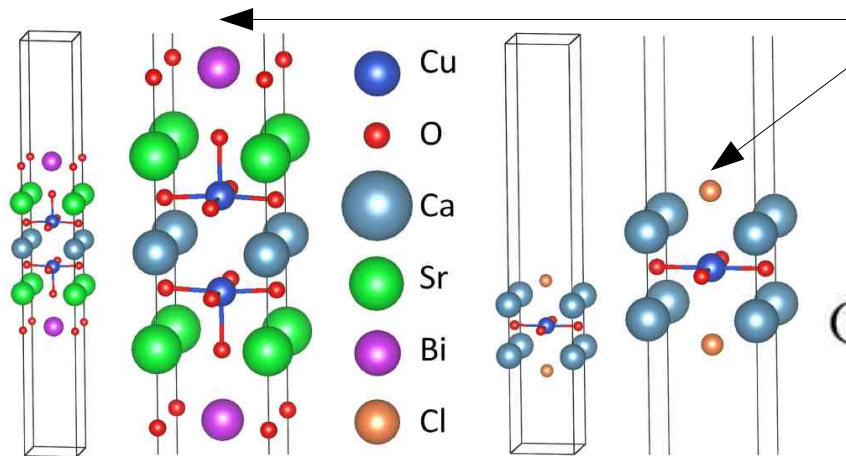


- universalities across materials



same properties for tunneling!

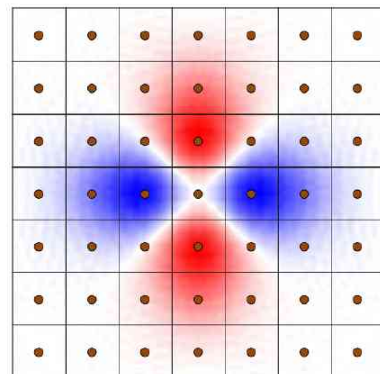
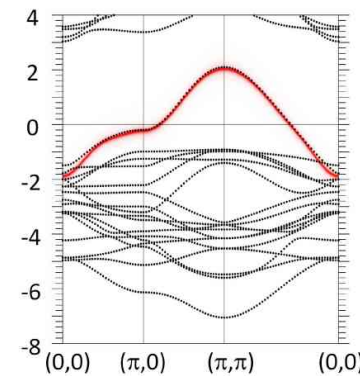
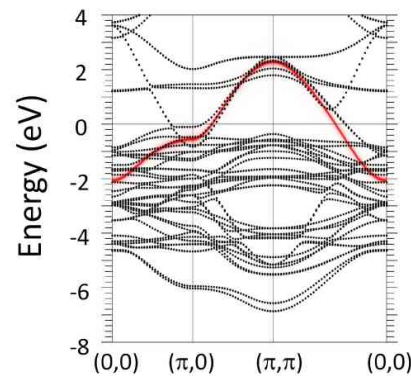
Wannier method: Cuprates



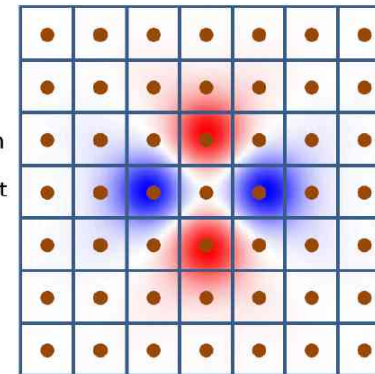
Surface
BiO vs. CaCl
and tunneling path
very different



Ab initio calculation:
1 band model
+Wannier function



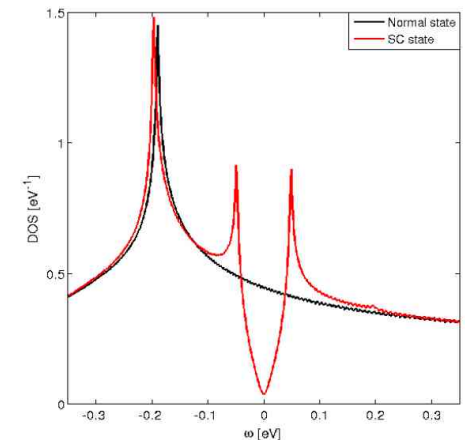
Cu position
relative to
BSCCO unit
cell



similar properties
dictated by
crystal symmetry

Superconductivity

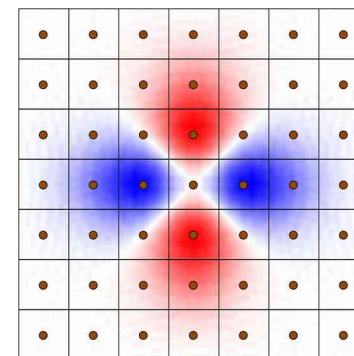
- superconducting order parameter (d-wave) (phenomenology or calculation fx. mean-field)



- continuum Green function

$$\psi_{\sigma}(\mathbf{r}) = \sum_{\mathbf{R}\mu} c_{\mathbf{R}\mu\sigma} w_{\mathbf{R}\mu}(\mathbf{r})$$

$$G(\mathbf{r}, \mathbf{r}'; \omega) = \sum_{\mathbf{R}, \mathbf{R}'} G(\mathbf{R}, \mathbf{R}'; \omega) w_{\mathbf{R}}(\mathbf{r}) w_{\mathbf{R}'}^*(\mathbf{r}')$$



surface Wannier function with phases

lattice Green function

local density of states (LDOS)
 $\rho(\mathbf{r}, \omega) \equiv -\frac{1}{\pi} \text{Im } G(\mathbf{r}, \mathbf{r}; \omega)$

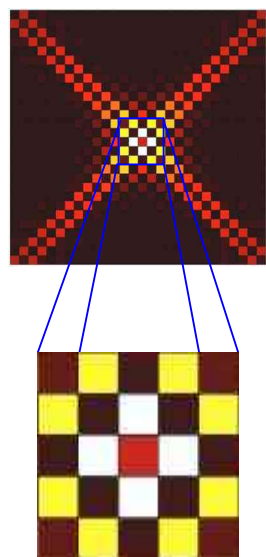
nonlocal contributions

continuum position

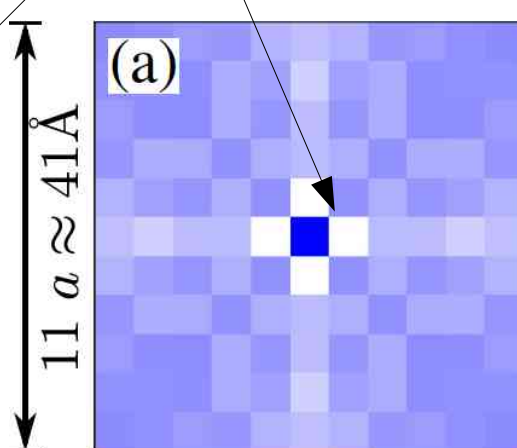
BSCCO: Results STM maps and spectra

- d-wave order parameter
- Zn impurity:
 $V_{\text{imp}} = -5 \text{ eV}$
resonance: -3.6 meV

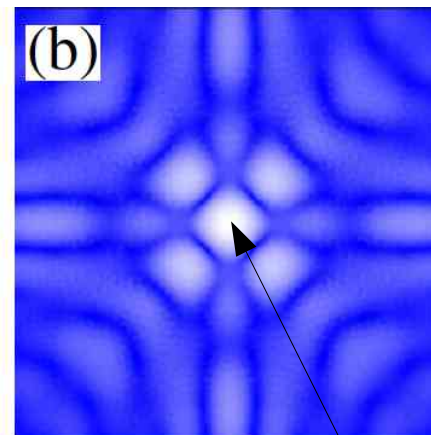
Zhu et al., PRB
67, 094508
(2003)



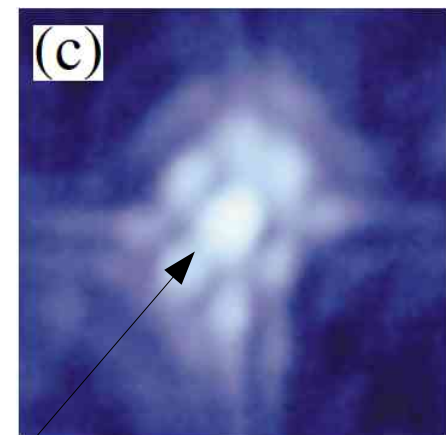
resonance at NN



BdG



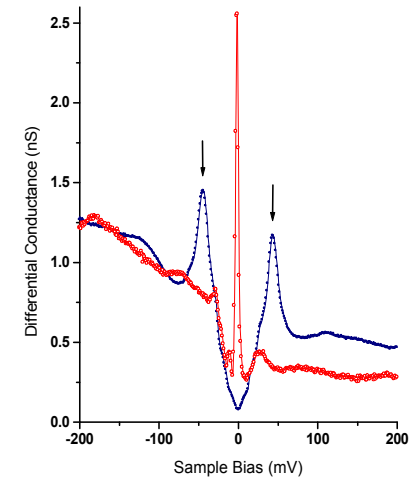
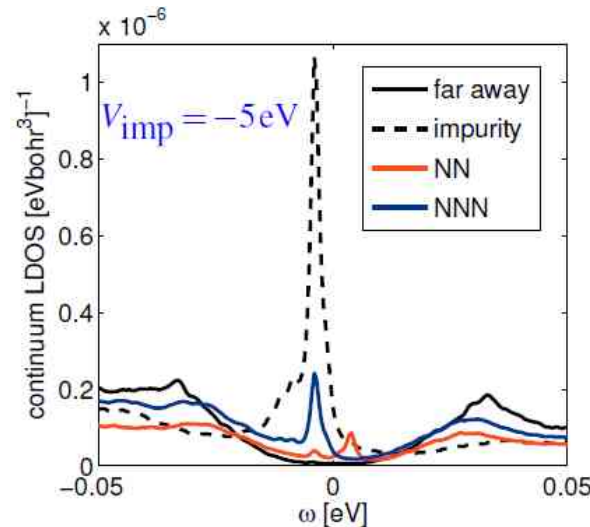
BdG+W



experiment

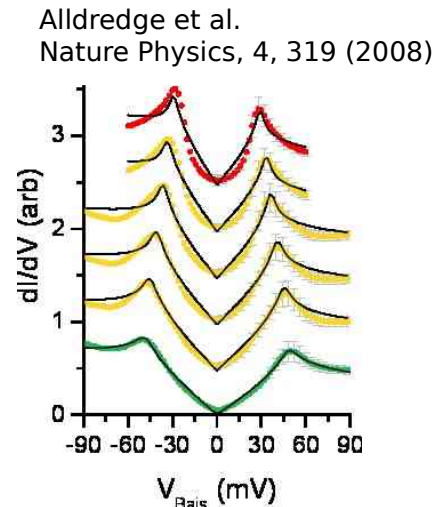
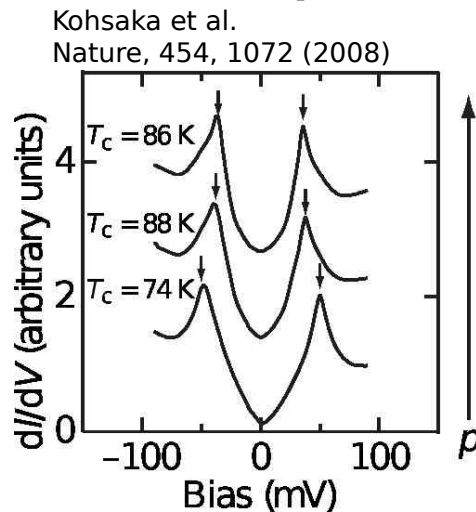
resonance at impurity

Pan et al., Nature
403, 746 (2000)



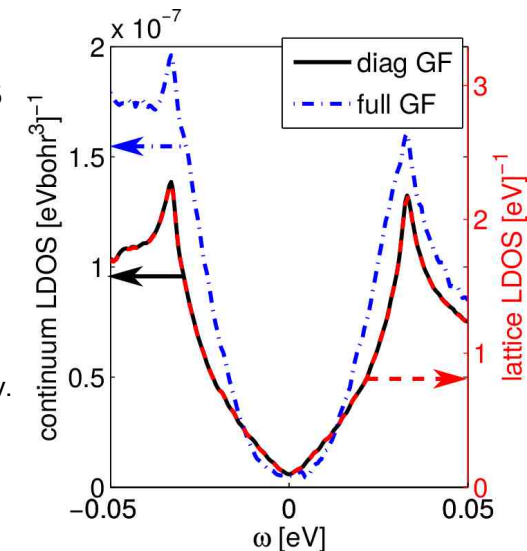
STM Spectra: homogeneous SC

- overdoped: U-shape, lower doping: V-shape



BdG+W:
U-shape enters
naturally within
Wannier
transformation

A. Kreisel, et al., Phys. Rev. Lett. **114**, 217002 (2015)



Analytical result

- Spectral function
- Wannier transformation
- $d_{x^2-y^2}$ Wannier function
- only cubic contribution

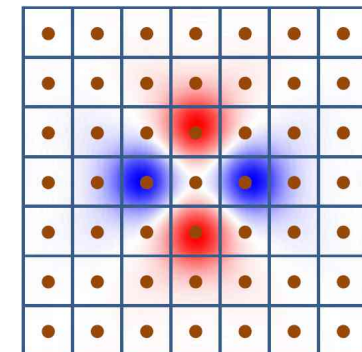
$$A_{\sigma}(\mathbf{k}, \omega) = |u_{\mathbf{k}}|^2 \delta(\omega - E_{\mathbf{k}}) + |v_{\mathbf{k}}|^2 \delta(\omega + E_{\mathbf{k}})$$

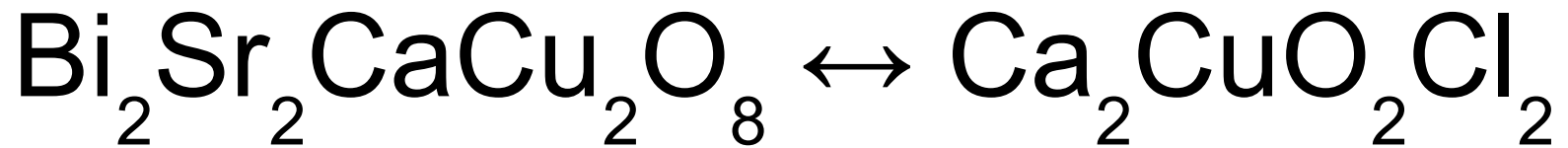
$$\rho_{\sigma}(\mathbf{r}, \omega) = \sum_{\mathbf{k}} A_{\sigma}(\mathbf{k}, \omega) |W_{\mathbf{k}}(\mathbf{r})|^2$$

$$W_{\mathbf{k}}(\mathbf{r}_0) \approx w_0 + 2w_1(\cos k_x - \cos k_y)$$

$$w_0 = 0$$

$$\rho_{\sigma} = w_1^2 \frac{4 \sin^2(k_x^0)}{\pi^3 v_F v_{\Delta}^3} \omega^3$$

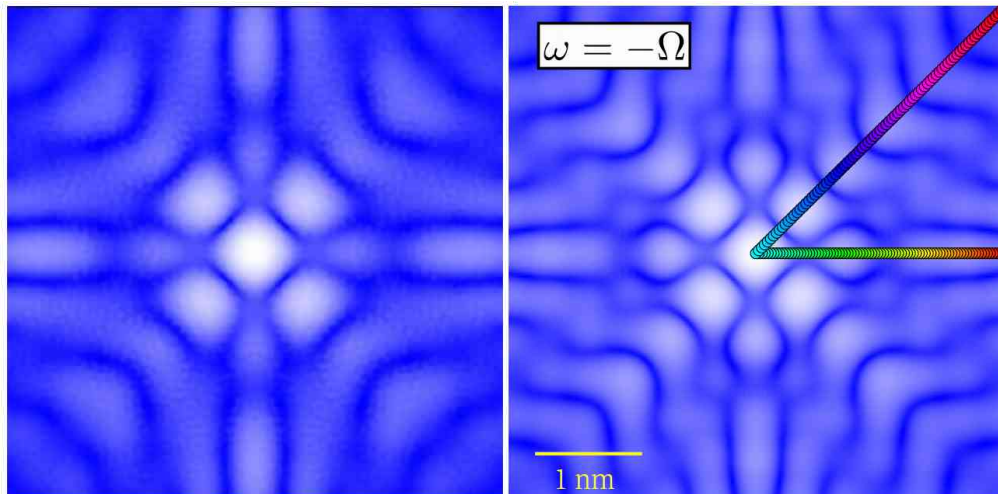




- superconductivity:
d-wave order parameter
- T-matrix calculation+ Wannier method

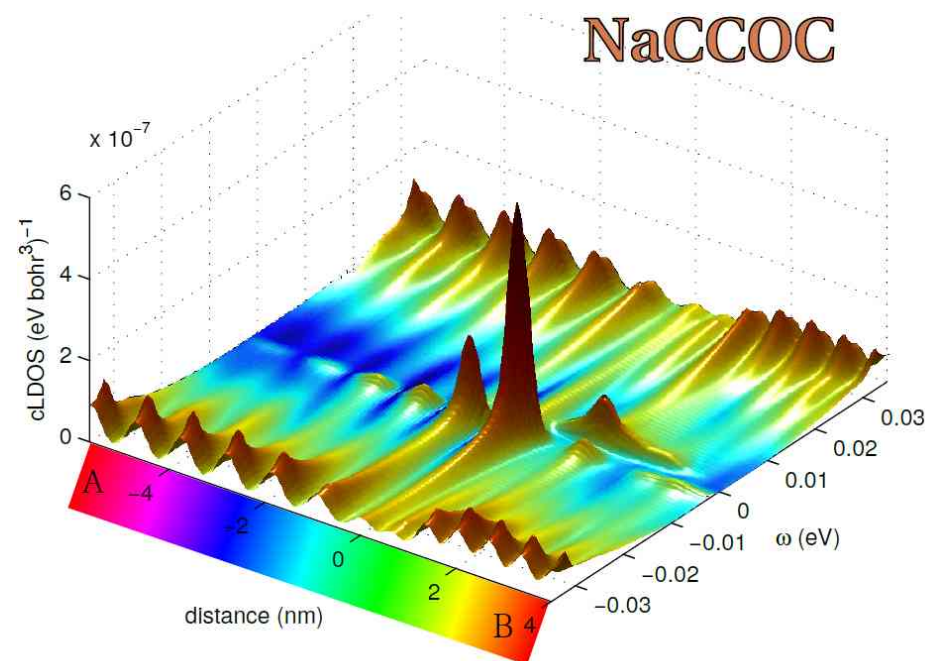
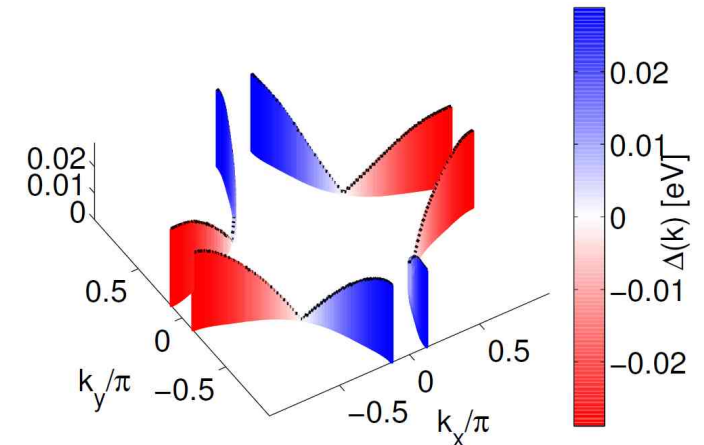
$$G(\mathbf{r}, \mathbf{r}'; \omega) = \sum_{\mu, \nu, \mathbf{R}, \mathbf{R}'} G(\mathbf{R}, \mu, \mathbf{R}', \nu; \omega) w_{\mathbf{R}, \mu}(\mathbf{r}) w_{\mathbf{R}', \nu}^*(\mathbf{r}')$$

- strong impurity
spectra + conductance map



$\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$

$\text{Ca}_2\text{CuO}_2\text{Cl}_2$



Kreisel et al., Phys. Rev. Lett. **114**, 217002 (2015)
 Choubey et al., New J. Phys. **19**, 013028 (2017)
 P. Choubey, et al., Phys. Rev. B **96**, 174523 (2017)

Summary

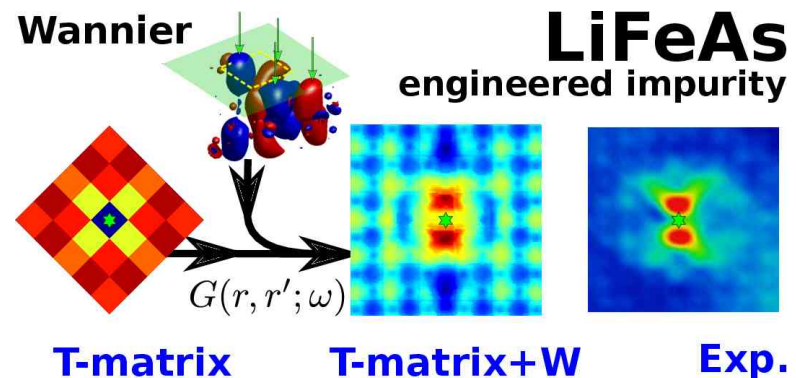
- Wannier method: basis transformation of the lattice Green function
- Qualitative correct (symmetry) and quantitative predictive results
- Impurities and homogeneous lattice in LiFeAs
- inelastic tunneling
- Universality in cuprates
- method to detect sign change of order parameter in STM

S. Chi, (...) , A. Kreisel, *et al.*, Nat. Commun. **8**, 15996 (2017)

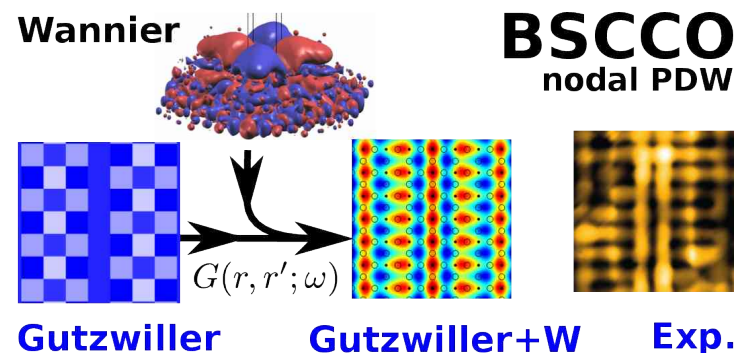
Martiny, Kreisel, Hirschfeld, Andersen Phys. Rev. B **95**, 184507 (2017)
Sprau, *et al.* Science, **357**, 75 (2017)

- Nematicity in Fe-based SC

A. Kostin, *et al.*, arXiv:1802.02266



S. Chi, (...) , A. Kreisel, *et al.* Phys. Rev. B **94**, 134515 (2016)
A. Kreisel, *et al.* Phys. Rev. B **94**, 224518 (2016)



Kreisel *et al.*, Phys. Rev. Lett. **114**, 217002 (2015)
Choubey *et al.*, New J. Phys. **19**, 013028 (2017)
Choubey, *et al.* Phys. Rev. B **96**, 174523 (2017)

Acknowledgments

