

# Hadronization in BAMPS

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Transport group meeting, Frankfurt am Main, 20.12.2012

# Outline

Motivation

Reminder - previous approaches

New approach - hadronization via partonic clusters

Summary & outlook

# Motivation

- **Transportalgorithm solves Boltzmann equation with Monte-Carlo-technik**

$$p^\mu \partial_\mu f(x, p) = C_{22} + C_{23} + \dots$$

**B**oltzmann  
**A**pproach for  
**M**ulti-  
**P**arton  
**S**catterings

- **stochastic interpretation of collision rates**

$$P_{2i} = V_{rel} \frac{\sigma_{2i}}{N_{test}} \frac{\Delta t}{\Delta^3 X}$$

- **pQCD interactions with 2 $\leftrightarrow$ 3 and 3 $\leftrightarrow$ 2 processes**

**Z. Xu & C. Greiner,**  
**Phys. Rev. C 71 (2005) 064901**

# Motivation

- BAMPS purely gluonic – need for a ‘translation’
- describe hadronization via microscopic processes
- create Pions via (elastic) gluon fusion

# Previous approaches

Describe Hadronization process via  $gg \rightarrow \pi\pi$  reactions.

With constant cross sections for  $\epsilon < \epsilon_{\text{crit}}$ .

-conserves energy and momentum

-Problem: No confinement!

# Previous approaches

Describe Hadronization via instantaneous cell-by-cell process

In each cell with  $\epsilon < \epsilon_{crit}$  every parton is clustered with other partons from the cell until  $\sqrt{s} > 2M_{Pion}$ .

If no more partons in cell, choose geometrically nearest.

Each cluster decays into two Pions.

-conserves energy and momentum

-fulfills confinement

-Problem: entropy drops dramatically!

# Previous approaches

Modify algorithm by allowing 3 Pion decay of a cluster whenever kinematically possible.

- conserves energy and momentum
- fulfills confinement
- roughly conserves entropy

- Problem: Hadronization happens instantaneous
  - diverging cross sections
  - no rates definable

# Hadronization via partonic clusters

Introduce partonic states  $p^*$

$$gg \rightarrow p^*$$

$$p^* \rightarrow p^* \pi$$

$$gp^* \rightarrow p^*$$

$$p^* \rightarrow \pi \pi$$

$$p^* p^* \rightarrow p^*$$

Define partonic cross sections  $\sigma = x_0 / \Delta x$

Use BAMPS stochastic method for collision in cells.

Use geometric collision routines if only one particle in cell.

Define decay probabilities via half-life  $\lambda(E_{\text{cm}})$

- conserves energy and momentum
- fulfills confinement
- roughly conserves entropy
- rates and cross sections well defined



# Hadronization via partonic clusters

Model has three Parameters

$$\sigma = x_0 / \Delta x$$

$$\lambda(E_{\text{cm}})$$

$$\epsilon_{\text{crit}}$$

What is missing?

No colour in BAMPS yet!

No Quarks/Baryons yet!

# The entropy problem

Assuming massless gluon gas going to massive Pion gas

$$f_{gluon} = g_{part} \exp(-p/T) \qquad f_{Pion} = \lambda_{Pion} g_{Pion} \exp(-\sqrt{p^2 + m^2}/T)$$

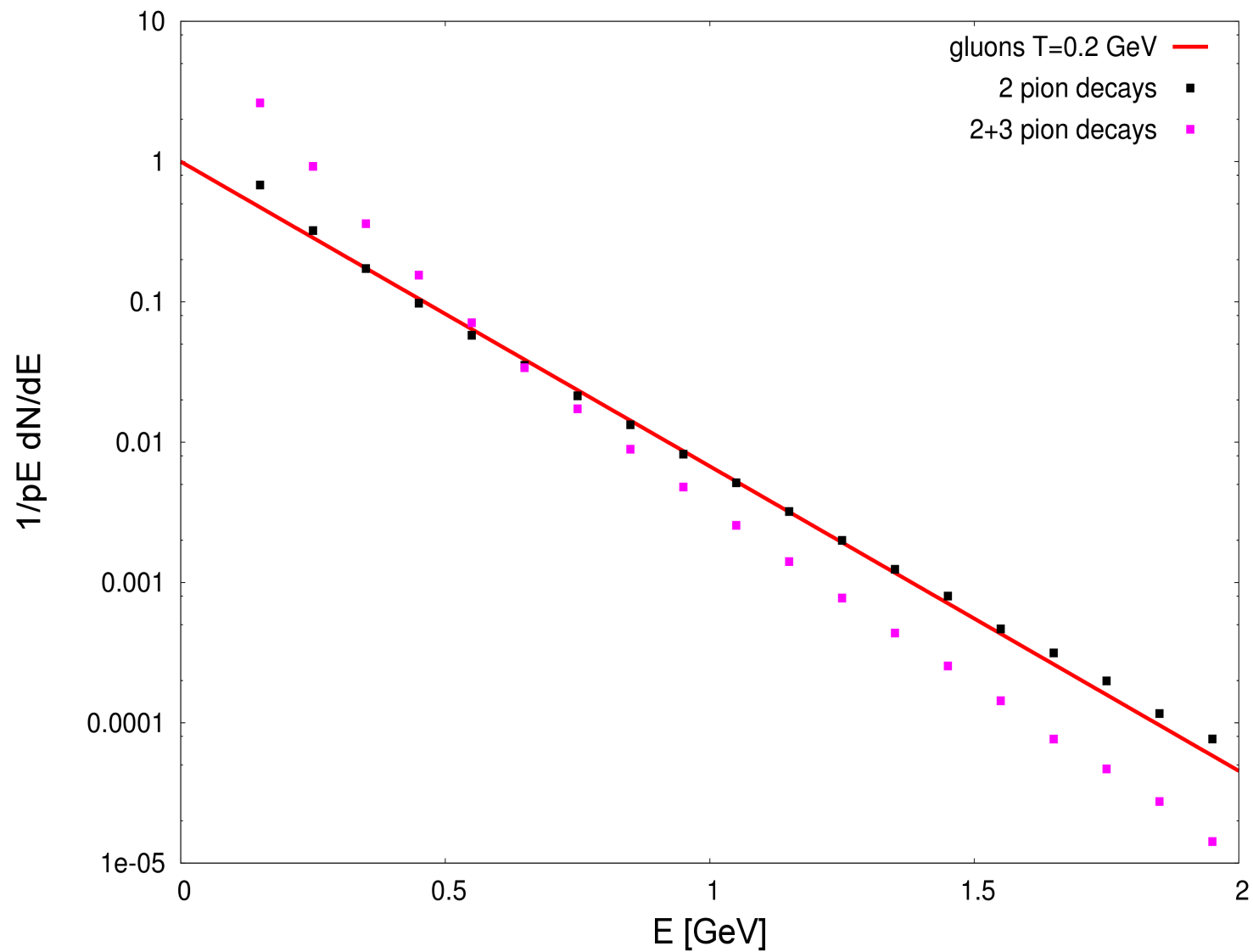
$$s = \int f (1 - \ln(f)) d^3 p$$

Total energy must be conserved!

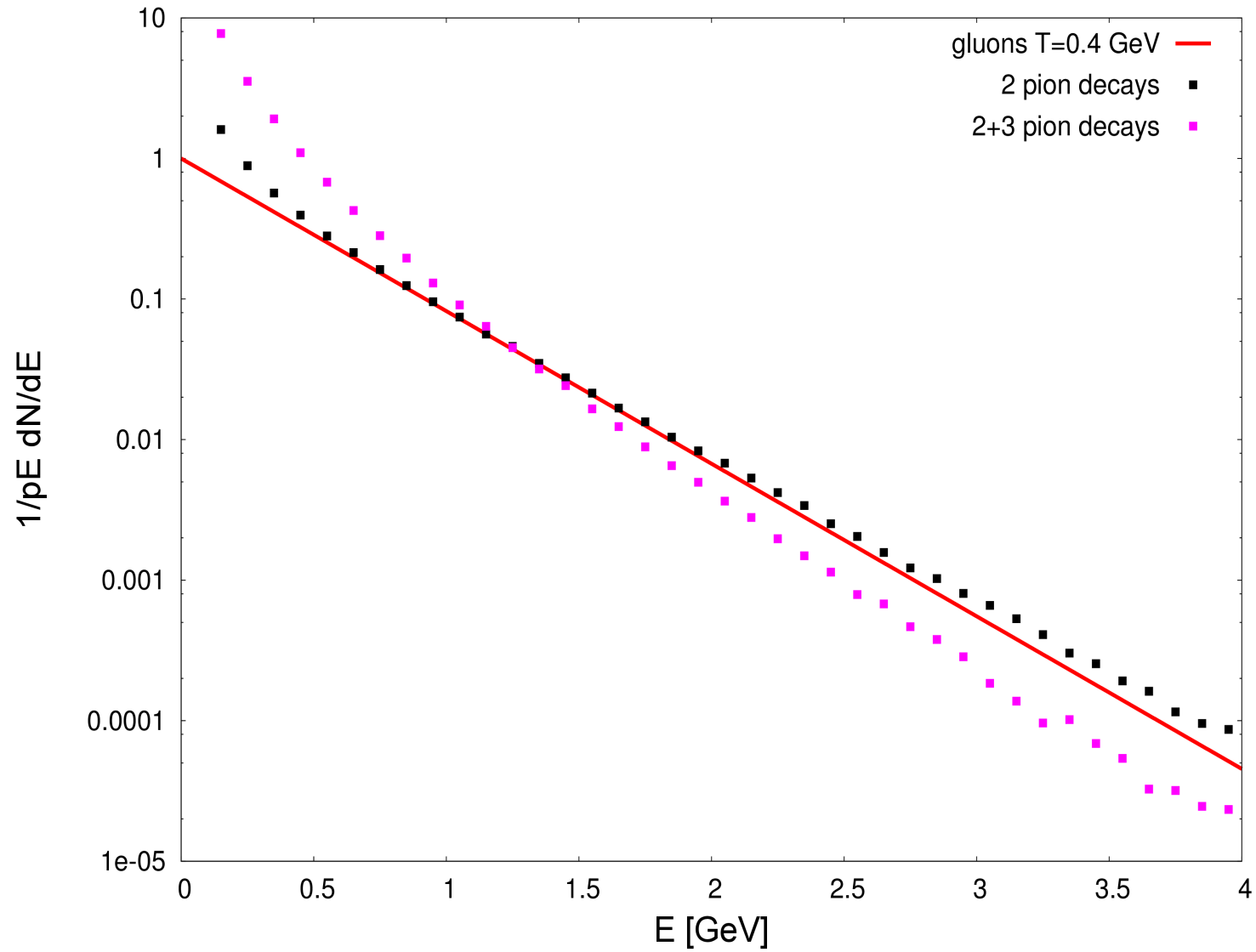
For a given partonic state only one free parameter left!

Task is to find a transition that maximises  $s$ !

# The entropy problem



# The entropy problem



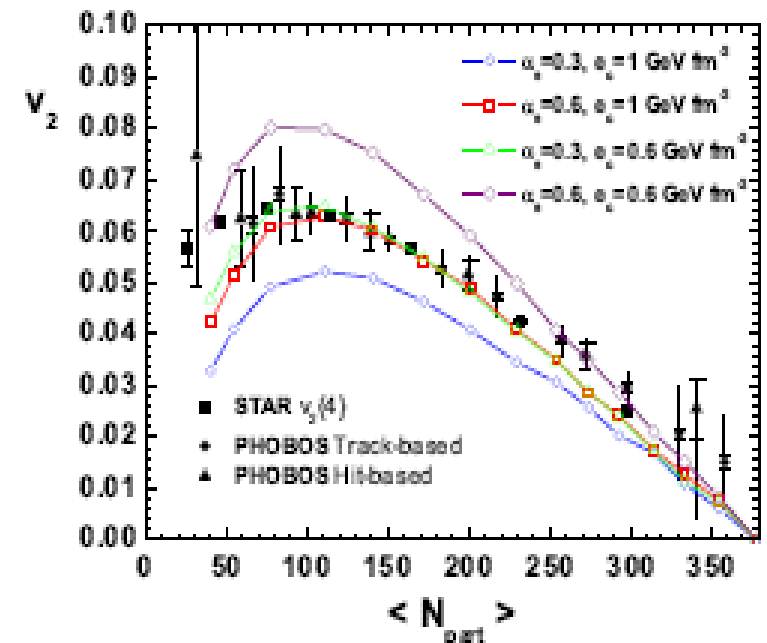
# Hadronization via partonic clusters

Au Au @ RHIC 200GeV  $b= 8.6$  fm  
mid-rapidity

Preliminary results on integrated  $v_2$

BAMPS without hadronization: 6.3 %  
O. Fochler, Z. Xu, C. Greiner, PRL 102 (2009)  
O. Fochler et al. arXiv:0811.4133 [hep-ph]

BAMPS with hadronization 1.2%



# Summary

Approach 1 – elastic scatterings

- no confinement

Approach 2 – instantaneous cell-by-cell hadronization

- confinement

- entropy conserved

- diverging cross sections

Approach 3 – partonic clusters

- confinement

- entropy conserved

- well defined cross sections

# Outlook

If the world doesn't end tomorrow

- improve statistics for results on  $v_2$  and  $v_2(\text{pt})$
- compare to results from Fochler et al.
  
- switch to LHC energies
  
- implement Quarks / Baryons ( and other Mesons)