Spin alignment of ρ meson in the hadronic phase

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Outline

- Background
- Evolution of the spin alignment for ρ meson in a pion gas (Local effect)
- Shear induced spin alignment for ρ meson (Nonlocal effect)



Spin polarization



Works on spin polarization

Z.-T. Liang et al. Phys. Rev. Lett. 94, 102301 (2005)
Z.-T. Liang et al. Phys. Lett. B 629, 20 (2005)
J.-H. Gao et al. Phys. Rev. C 77, 044902 (2008)
F. Becattini et al. Phys. Rev. C 77, 024906 (2008)
I. Karpenko et al. Eur. Phys. J. C 77, 213 (2017)
H. Li et al. Phys. Rev. C 96, 054908 (2017)
Y. Xie et al. Phys. Rev. C 95, 031901(R) (2017)
S. Shi et al. Phys. Lett. B 788, 409 (2019)



Bernett effect

S. J. Barnett, Rev. Mod. Phys. 7, 129 (1935)

Einstein-de Haas effect

A. Einstein and W. de Haas, Deuts. Physik. Gesells. Verhandlun. 17, 152 (1915)

Spin polarization



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Spin alignment of vector mesons

Spin density matrix:



Spin alignment of ϕ mesons



STAR, Nature 614, 244–248 (2023)

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Spin alignment of ϕ mesons

| Physics Mechanisms | (ρ ₀₀) |
|--|---|
| c_Λ: Quark coalescence vorticity & magnetic field ^[1] | < 1/3 (Negative ~ 10 ⁻⁵) |
| c _ε : E-comp. of Vorticity tensor ^[1] | < 1/3 (Negative ~ 10 ⁻⁴) |
| c_E: Electric field ^[2] | > 1/3 (Positive ~ 10 ⁻⁵) |
| c_F: Fragmentation ^[3] | > or, < 1/3 (~ 10 ⁻⁵) |
| c _L : Local spin alignments ^[4] | < 1/3 |
| c _A : Turbulent color field ^[5] | < 1/3 |
| c _φ : Vector meson strong force field ^[6] | > 1/3 (Can accommodate large positive signal) |
| c _g : Glasma fields + effective potential | could be significant |

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Spin alignment of J/Ψ mesons



Spin alignment of ρ mesons



AuAu for run 2011 at 200 GeV, Centrality: 60-80%, pT: 1.8-2.4 GeV/c Taken from Baoshan Xi - Quark Matter 2023

Outline



- Evolution of the spin alignment for ρ meson in a pion gas (Local effect)
- Shear induced spin alignment for ρ meson (Nonlocal effect)

Motivation



Hadron interaction

Quark-gluon interaction, $\rho_{00} - \frac{1}{3} \approx c_A + c_{\epsilon} + c_E + c_{\phi} + \cdots$

The width of ρ^0 meson is much larger than ϕ meson, so the coupling between ρ^0 mesons and hadron gas must be considered.

| | ρ^0 | $oldsymbol{\phi}$ |
|--------------------------|----------------------------|--|
| Mass | $m \approx 770 { m MeV}$ | $m pprox 1020 { m MeV}$ |
| Width | $\Gamma \approx 147.4 MeV$ | $\Gamma \approx 4.249 \text{MeV}$ |
| Main decay channel | $\rho^0 \to \pi^+ \pi^-$ | $ \phi \to K^+ K^- \phi \to K_L^0 K_S^0 \dots$ |
| Quark constitution | $uar{u},dar{d}$ | SS |

Chiral magnetic effect (CME)



Chirality imbalance
 $(\mu_5 \neq 0)$ Charge separationExternal magnetic field

$$\overrightarrow{J_e} = \frac{e^2}{2\pi^2} \mu_5 \overrightarrow{B}$$

$$\overrightarrow{I}$$
Ddd parity Even parity

D. Kharzeev, Phys. Lett. B 633, 260 (2006)
D. E. Kharzeev et al. Nucl. Phys. A 803, 227 (2008)
K. Fukushima et al. Phys. Rev. D 78, 074033 (2008)

γ correlator and tensor polarization

The γ correlator for the chiral magnetic effect (CME) is defined as

$$\gamma_{112} \equiv \langle \cos(\phi_{\alpha} + \phi_{\beta} - 2\Psi_{RP}) \rangle$$
Azimuthal angle
Reaction plane

The difference between γ correlators for the opposite-sign (OS) and same-sign (SS) pairs can be regarded as a CME signal

$$\Delta \gamma_{112} \equiv \gamma_{112}^{\rm OS} - \gamma_{112}^{\rm SS}$$

The contribution to $\Delta \gamma_{112}$ from pions in the decay $\rho_0 \rightarrow \pi^+ \pi^-$:

$$\Delta \gamma_{112}^{\rho} = \frac{N_{\rho}}{N_{+}N_{-}} \Delta \overline{\gamma}_{112}^{\rho}$$
$$\Delta \overline{\gamma}_{112}^{\rho} \equiv \operatorname{Cov}(\cos \Delta \phi_{+}, \cos \Delta \phi_{-})$$
$$- \operatorname{Cov}(\sin \Delta \phi_{+}, \sin \Delta \phi_{-}),$$



The decay products of ρ meson contribute to the γ correlator.

Diyu Shen et al. Phys. Lett. B 839 137777 (2023)

γ correlator and tensor polarization

$$\begin{split} \Delta \overline{\gamma}_{112}^{\rho} &= \frac{1}{n_{\rho}} \int \frac{d^{3} \mathbf{p}_{\rho}}{(2\pi\hbar)^{3}} f(\mathbf{p}_{\rho}) \\ &\times \left[\int d\Omega^{*} \frac{dN}{d\Omega^{*}} (\cos \phi_{+} \cos \phi_{-} - \sin \phi_{+} \sin \phi_{-}) \right. \\ &- \int d\Omega^{*} \frac{dN}{d\Omega^{*}} \cos \phi_{+} \int d\Omega^{*} \frac{dN}{d\Omega^{*}} \cos \phi_{-} \\ &+ \int d\Omega^{*} \frac{dN}{d\Omega^{*}} \sin \phi_{+} \int d\Omega^{*} \frac{dN}{d\Omega^{*}} \sin \phi_{-} \right], \\ \Delta \overline{\gamma}_{112}^{\rho} &= \sum_{i=1}^{5} A_{i} t_{i} + \sum_{i,j=1}^{5} B_{ij} t_{i} t_{j} \\ &\downarrow \text{ inear Quadratic} \end{split}$$

 $\delta \rho_{00}$ and $Re \rho_{1,-1} (T_{11} - T_{22})$ have dominant effects!

$$\rho_{\lambda_{1}\lambda_{2}} = \left(\frac{1}{3} + \frac{1}{2}P_{i}\Sigma_{i} + T_{ij}\Sigma_{ij}\right)_{\lambda_{1}\lambda_{2}},$$

$$\frac{dN}{d\Omega^{*}} = \frac{3}{8\pi} [(1 - \rho_{00}) + (3\rho_{00} - 1)\sin^{2}\theta^{*}\sin^{2}\phi^{*} - (T_{11} - T_{22})(\cos^{2}\theta^{*} - \sin^{2}\theta^{*}\cos^{2}\phi^{*}) - 2T_{12}\sin(2\theta^{*})\cos\phi^{*} - 2T_{31}\sin(2\theta^{*})\sin\phi^{*} - 2T_{23}\sin^{2}\theta^{*}\sin(2\phi^{*})].$$

Linear and quadratic coefficients

| t_i | $\rho_{00} - 1/3$ | $T_{11} -$ | T_{22} T_{12} | <i>T</i> ₃₁ <i>T</i> | 23 |
|---------------------|-------------------|-------------------|-------------------------|---------------------------------|------------------------|
| A_i | 0.5215 | -0.17 | 0 | 0 | 0 |
| $\overline{B_{ij}}$ | $\rho_{00} - 1/3$ | $T_{11} - T_{22}$ | <i>T</i> ₁₂ | <i>T</i> ₃₁ | <i>T</i> ₂₃ |
| $p_{00} - 1/3$ | 0.03885 | 0.01295 | 0 | 0 | 0 |
| $T_{11} - T_{22}$ | 0.01295 | -0.01295 | 0 | 0 | 0 |
| T_{12} | 0 | 0 | -6.089×10^{-4} | 0 | 0 |
| T_{31} | 0 | 0 | 0 | -6.089×10^{-4} | 0 |
| T_{23} | 0 | 0 | 0 | 0 | 0 |

1. Two-point Green's function in CTP formalism: *Xin-Li Sheng et al. Phys. Rev. D 109, 036004 (2024)*

Two-point Green's functions in closed-time-path (CTP) formalism for vector mesons:

$$\begin{split} G_{CTP}^{\mu\nu}(x_1, x_2) &= \langle T_C A^{\mu}(x_1) A^{\nu}(x_2) \rangle & \xrightarrow{t_0} \\ & t_0 \\ G_{\mu\nu}^{<}(x, p) &= 2\pi\hbar \sum_{\lambda_1, \lambda_2} \delta\left(p^2 - m_{\rho}^2\right) \left\{ \theta(p^0) \epsilon_{\mu}\left(\lambda_1, \mathbf{p}\right) \epsilon_{\nu}^*\left(\lambda_2, \mathbf{p}\right) \overbrace{f_{\lambda_1\lambda_2}(x, \mathbf{p})}^{\bullet} \right) & \text{matrix valued spin dependent distribution } \\ & +\theta(-p^0) \epsilon_{\mu}^*\left(\lambda_1, -\mathbf{p}\right) \epsilon_{\nu}\left(\lambda_2, -\mathbf{p}\right) \left[\delta_{\lambda_2\lambda_1} + f_{\lambda_2\lambda_1}(x, -\mathbf{p}) \right] \right\}, \\ G_{\mu\nu}^{>}(x, p) &= 2\pi\hbar \sum_{\lambda_1, \lambda_2} \delta\left(p^2 - m_{\rho}^2\right) \left\{ \theta(p^0) \epsilon_{\mu}\left(\lambda_1, \mathbf{p}\right) \epsilon_{\nu}^*\left(\lambda_2, \mathbf{p}\right) \left[\delta_{\lambda_1\lambda_2} + f_{\lambda_1\lambda_2}(x, \mathbf{p}) \right] \\ & +\theta(-p^0) \epsilon_{\mu}^*\left(\lambda_1, -\mathbf{p}\right) \epsilon_{\nu}\left(\lambda_2, -\mathbf{p}\right) f_{\lambda_2\lambda_1}(x, -\mathbf{p}) \right\}, \end{split}$$

2. Kadanoff-Baym (KB) equation:

$$p \cdot \partial_{x}G^{<,\mu\nu}(x,p) - \frac{1}{4} \Big[p^{\mu}\partial_{\eta}^{x}G^{<,\eta\nu}(x,p) + p^{\nu}\partial_{\eta}^{x}G^{<,\mu\eta}(x,p) \Big]$$

$$= \frac{1}{4} \big[\Sigma^{<,\mu}{}_{\alpha}(x,p)G^{>,\alpha\nu}(x,p) - \Sigma^{>,\mu}{}_{\alpha}(x,p)G^{<,\alpha\nu}(x,p) \big]$$

$$+ \frac{1}{4} \big[G^{>,\mu}{}_{\alpha}(x,p) \underbrace{\Sigma^{<,\alpha\nu}(x,p)}_{} - G^{<,\mu}{}_{\alpha}(x,p)\Sigma^{>,\alpha\nu}(x,p) \big]$$

Self energy

- The self energy should be calculated with a explicit Lagrangian;
- Since ρ meson is a real vector meson, we can only consider the positive-energy part of the equation.

We have neglected the

Poisson bracket terms

(Nonlocal effect).

3. Effective Lagrangian:

T. Fujiwara et al., Prog. Theor. Phys. **74**, 128 (1985) Chiral effective theory with SU(2) flavor symmetry.

4. Spin Boltzmann equations:

Xin-Li Sheng et al. Phys. Rev. D 109, 036004 (2024)

$$p \cdot \partial_{x} f_{\lambda_{1}\lambda_{2}}(x, \mathbf{p}) = -\frac{1}{4} \delta_{\lambda_{2}\lambda_{2}'} \epsilon_{\mu}^{*} (\lambda_{1}, \mathbf{p}) \epsilon^{\alpha} (\lambda_{1}', \mathbf{p}) \\ \times \left\{ \left[\delta_{\lambda_{1}'\lambda_{2}'} + f_{\lambda_{1}'\lambda_{2}'}(x, \mathbf{p}) \right] \Sigma^{<,\mu} (x, p) - f_{\lambda_{1}'\lambda_{2}'}(x, \mathbf{p}) \Sigma^{>,\mu} (x, p) \right\} \\ -\frac{1}{4} \delta_{\lambda_{1}\lambda_{1}'} \epsilon_{\nu} (\lambda_{2}, \mathbf{p}) \epsilon_{\alpha}^{*} (\lambda_{2}', \mathbf{p}) \\ \times \left\{ \left[\delta_{\lambda_{1}'\lambda_{2}'} + f_{\lambda_{1}'\lambda_{2}'}(x, \mathbf{p}) \right] \Sigma^{<,\alpha\nu} (x, p) - f_{\lambda_{1}'\lambda_{2}'}(x, \mathbf{p}) \Sigma^{>,\alpha\nu} (x, p) \right\} \right\}$$

Collision terms

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5. Collision terms:

We decompose the collision terms into coalescence-dissociation part and scattering part, and assumed that the system is homogeneous in space.

$$\partial_t f_{\lambda_1 \lambda_2}(x, \mathbf{p}) = C_{\text{coal/diss}} + C_{\text{scat}}$$

A. Leading order

$$\begin{split} C^{(0)}_{\text{coal/diss}}(\rho^{0} \leftrightarrow \pi^{+}\pi^{-}) \\ &= \hbar \frac{g_{V}^{2}}{E_{p}^{\rho}} \int \frac{d^{3}k}{(2\pi\hbar)^{3}4E_{k}^{\pi}E_{p-k}^{\pi}} 2\pi\hbar\delta \left(E_{p}^{\rho}-E_{k}^{\pi}-E_{p-k}^{\pi}\right) \\ &\times \left[\delta_{\lambda_{2}\lambda_{2}'}k\cdot\epsilon^{*}(\lambda_{1},\mathbf{p})k\cdot\epsilon(\lambda_{1}',\mathbf{p})\right. \\ &\left. + \delta_{\lambda_{1}\lambda_{1}'}k\cdot\epsilon(\lambda_{2},\mathbf{p})k\cdot\epsilon^{*}(\lambda_{2}',\mathbf{p})\right] \\ &\left. + \left\{f_{\pi^{+}}(x,\mathbf{k})f_{\pi^{-}}(x,\mathbf{p}-\mathbf{k})\left[\delta_{\lambda_{1}'\lambda_{2}'}+f_{\lambda_{1}'\lambda_{2}'}(x,\mathbf{p})\right]\right. \\ &\left. - \left[1+f_{\pi^{+}}(x,\mathbf{k})\right]\left[1+f_{\pi^{-}}(x,\mathbf{p}-\mathbf{k})\right]f_{\lambda_{1}'\lambda_{2}'}(x,\mathbf{p})\right], \end{split}$$



5. Collision terms:

B. Next-to-leading order

$$C_{\text{scat}}(\rho^{0}\pi^{\pm} \leftrightarrow \rho^{0}\pi^{\pm}) = \frac{4g_{V}^{4}}{E_{P}^{0}}\hbar^{2}\int \frac{d^{3}k_{1}}{(2\pi\hbar)^{3}2E_{k_{1}}^{\pi}} \int \frac{d^{3}k_{2}}{(2\pi\hbar)^{3}2E_{k_{2}}^{\pi}} \int \frac{d^{3}p_{1}}{(2\pi\hbar)^{3}2E_{p_{1}}^{\rho}} (2\pi\hbar)^{4}\delta^{(4)}(p+k_{2}-p_{1}-k_{1}) \\ \times \left[\delta_{\lambda_{2}\lambda_{2}^{1}}D_{(1)}(s_{1},\lambda_{1})D_{(1)}^{*}(s_{2},\lambda_{1}^{\prime}) + \delta_{\lambda_{1}\lambda_{1}^{\prime}}D_{(1)}(s_{1},\lambda_{2}^{\prime})D_{(1)}^{*}(s_{2},\lambda_{2})\right] \\ \times \left[f_{s_{1}s_{2}}(x,\mathbf{p}_{1})f_{\pi^{\pm}}(x,\mathbf{k}_{1})(1+f_{\pi^{\pm}}(x,\mathbf{k}_{2}))(\delta_{\lambda_{1}^{\prime}\lambda_{2}^{\prime}} + f_{\lambda_{1}^{\prime}\lambda_{2}^{\prime}}(x,\mathbf{p})) \\ - \left(\delta_{s_{1}s_{2}} + f_{s_{1}s_{2}}(x,\mathbf{p}_{1})\right)(1+f_{\pi^{\pm}}(x,\mathbf{k}_{2})f_{\lambda_{1}^{\prime}\lambda_{2}^{\prime}}(x,\mathbf{p})\right] \\ - \left(\delta_{s_{1}s_{2}} + f_{s_{1}s_{2}}(x,\mathbf{p}_{1})\right)(1+f_{\pi^{\pm}}(x,\mathbf{k}_{2})f_{\lambda_{1}^{\prime}\lambda_{2}^{\prime}}(x,\mathbf{p})\right] \\ \times \left[\delta_{\lambda_{2}\lambda_{2}^{\prime}}D_{(2)}(s_{1},\lambda_{1}^{\prime})D_{(2}^{*}(s_{2},\lambda_{1}) + \delta_{\lambda_{1}\lambda_{1}^{\prime}}D_{(2)}(s_{1},\lambda_{2})D_{(2)}^{*}(s_{2},\lambda_{2}^{\prime})\right] \\ \times \left[\delta_{\lambda_{2}\lambda_{2}^{\prime}}D_{(2)}(s_{1},\lambda_{1}^{\prime})D_{(2}^{*}(s_{2},\lambda_{1}) + \delta_{\lambda_{1}\lambda_{1}^{\prime}}D_{(2)}(s_{1},\lambda_{2})D_{(2)}^{*}(s_{2},\lambda_{2}^{\prime})\right] \\ \times \left[\delta_{\lambda_{2}\lambda_{2}^{\prime}}D_{(2)}(s_{1},\lambda_{1}^{\prime})D_{(2}^{*}(s_{2},\lambda_{1}) + \delta_{\lambda_{1}\lambda_{1}^{\prime}}D_{(2)}(s_{1},\lambda_{2})D_{(2)}^{*}(s_{2},\lambda_{2}^{\prime})\right] \\ \times \left[f_{\pi^{+}}(x,\mathbf{k}_{1})f_{\pi^{-}}(x,\mathbf{k}_{2})(\delta_{s_{1}s_{2}} + f_{s_{1}s_{2}}(x,\mathbf{p}_{1}))(\delta_{\lambda_{1}\lambda_{2}^{\prime}} + f_{\lambda_{1}\lambda_{2}^{\prime}}(x,\mathbf{p})) \\ - (1+f_{\pi^{+}}(x,\mathbf{k}_{1}))(1+f_{\pi^{-}}(x,\mathbf{k}_{2}))f_{s_{1}s_{2}}(x,\mathbf{p}_{1})f_{\lambda_{1}\lambda_{2}^{\prime}}(x,\mathbf{p})\right],$$

(c)

$$D_{(1)}(s,\lambda) = \hbar \frac{[k_1 \cdot \epsilon (s, \mathbf{p}_1)] [k_2 \cdot \epsilon^* (\lambda, \mathbf{p})]}{(p+k_2)^2 - m_\pi^2} + \hbar \frac{[k_2 \cdot \epsilon (s, \mathbf{p}_1)] [k_1 \cdot \epsilon^* (\lambda, \mathbf{p})]}{(p-k_1)^2 - m_\pi^2},$$
$$D_{(2)}(s,\lambda) = \hbar \frac{[k_1 \cdot \epsilon (s, \mathbf{p}_1)] [k_2 \cdot \epsilon (\lambda, \mathbf{p})]}{(p-k_2)^2 - m_\pi^2} + \hbar \frac{[k_2 \cdot \epsilon (s, \mathbf{p}_1)] [k_1 \cdot \epsilon (\lambda, \mathbf{p})]}{(p-k_1)^2 - m_\pi^2}.$$

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(d)

5. Collision terms:

C. Regulation of pion propagators

$$D_{(1)}(s,\lambda) = \hbar \frac{[k_1 \cdot \epsilon (s, \mathbf{p}_1)] [k_2 \cdot \epsilon^* (\lambda, \mathbf{p})]}{(p+k_2)^2 - m_\pi^2} + \hbar \frac{[k_2 \cdot \epsilon (s, \mathbf{p}_1)] [k_1 \cdot \epsilon^* (\lambda, \mathbf{p})]}{(p-k_1)^2 - m_\pi^2}, \longrightarrow \mathsf{Divergent}$$

$$D_{(2)}(s,\lambda) = \hbar \frac{[k_1 \cdot \epsilon (s, \mathbf{p}_1)] [k_2 \cdot \epsilon (\lambda, \mathbf{p})]}{(p-k_2)^2 - m_\pi^2} + \hbar \frac{[k_2 \cdot \epsilon (s, \mathbf{p}_1)] [k_1 \cdot \epsilon (\lambda, \mathbf{p})]}{(p-k_1)^2 - m_\pi^2}.$$

Introduce self-energy corrections with medium effects:

$$S^{F}(k) = \frac{i\hbar}{k^{2} - m_{\pi}^{2}},$$

$$S^{\overline{F}}(k) = \frac{-i\hbar}{k^{2} - m_{\pi}^{2}}.$$

$$S^{F}(k) = \frac{-i\hbar}{k^{2} - m_{\pi}^{2} + \hbar\Sigma^{\overline{F}}(k)},$$

The final results:

$$D_{\pi^{+}(1)}(s,\lambda) = \hbar \frac{[k_{1} \cdot \epsilon(s,\mathbf{p}_{1})][k_{2} \cdot \epsilon^{*}(\lambda,\mathbf{p})]}{(p+k_{2})^{2} - m_{\pi}^{2} + i\hbar\Gamma(p+k_{2})} \qquad D_{\pi^{-}(1)}(s,\lambda) = \hbar \frac{[k_{1} \cdot \epsilon(s,\mathbf{p}_{1})][k_{2} \cdot \epsilon^{*}(\lambda,\mathbf{p})]}{(p+k_{2})^{2} - m_{\pi}^{2} + i\hbar\Gamma(-p-k_{2})} + \hbar \frac{[k_{2} \cdot \epsilon(s,\mathbf{p}_{1})][k_{1} \cdot \epsilon^{*}(\lambda,\mathbf{p})]}{(p-k_{1})^{2} - m_{\pi}^{2} + i\hbar\Gamma(-p+k_{1})} \qquad + \hbar \frac{[k_{2} \cdot \epsilon(s,\mathbf{p}_{1})][k_{1} \cdot \epsilon^{*}(\lambda,\mathbf{p})]}{(p-k_{1})^{2} - m_{\pi}^{2} + i\hbar\Gamma(-p+k_{1})}$$



$$\begin{split} \Sigma(k) &\equiv \operatorname{Im}\Sigma^{F}(k) = 2g_{V}^{2}\theta(k^{0})\int \frac{d^{3}k_{1}}{(2\pi\hbar)^{3}2E_{k_{1}}^{\pi}}\int \frac{d^{3}p}{(2\pi\hbar)^{3}2E_{p}^{\rho}} \\ &\times (2\pi\hbar)^{4}\delta^{(4)}\left(k+k_{1}-p\right)f_{\pi^{-}}(\mathbf{k}_{1})\left[m_{\pi}^{2}-\frac{\left(k_{1}\cdot p\right)^{2}}{m_{\rho}^{2}}\right] \\ &+ 2g_{V}^{2}\theta(-k^{0})\int \frac{d^{3}k_{1}}{(2\pi\hbar)^{3}2E_{k_{1}}^{\pi}}\int \frac{d^{3}p}{(2\pi\hbar)^{3}2E_{p}^{\rho}} \\ &\times (2\pi\hbar)^{4}\delta^{(4)}\left(k-k_{1}+p\right)f_{\pi^{+}}(\mathbf{k}_{1})\left[m_{\pi}^{2}-\frac{\left(k_{1}\cdot p\right)^{2}}{m_{\rho}^{2}}\right] \end{split}$$

we only consider the imaginary part of the self-energy since the mass correction from the real part is much smaller.

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We assume that π^{\pm} are in global thermal equilibrium, so they obey the Bose-Einstein distribution

$$f_{\pi^{\pm}}(x, \mathbf{p}) = f_{\pi^{\pm}}(\mathbf{p}) = \frac{1}{\exp\left[\beta \left(E_p \mp \mu_{\pi}\right)\right] - 1},$$

and we choose $\mu_{\pi} = 0$ and T = 156.5 MeV.



Monte Carlo method: Momentum range: -2.5 ~ 2.5 GeV Lattice: $100 \times 100 \times 100 \text{ MeV}^3$ Time step: 10^{-3} fm/c

Does the choice of ρ meson's **initial state** affect the final spin alignment?

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Initial state:

$$f_{\lambda_1 \lambda_2} = \text{diag}(0.9, 1.2, 0.9) \times f_{\text{BE}}$$

The spin alignment for ρ^0 mesons will **decay rapidly toward zero** no matter what the initial state is.

Yi-Liang Yin et al. PhysRevC.110.024905 (2024)

Initial state:

$$f_{\lambda_1 \lambda_2} = \text{diag}(1.1, 0.8, 1.1) \times f_{\text{BE}}$$

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Blast wave model with elliptic flow



Fabrice Retiere et al. Phys. Rev. C 70, 044907 (2004)

$$f_{\pi} = \frac{1}{\mathrm{e}^{u_{\mu}\mathrm{p}^{\mu}/\mathrm{T}} - 1}$$

 $u^{\mu}(r, \phi_s) = (\cosh \rho(r, \phi_s), \sinh \rho(r, \phi_s) \cos \phi_s,$ $\sinh \rho(r, \phi_s) \sin \phi_s, 0),$ r

$$\rho(r,\phi_s) = \frac{r}{R} [\rho_0 + \rho_2 \cos(2\phi_s)].$$

The parameters are chosen as:

$$R = 13 \text{ fm}, \rho_0 = 0.89, \rho_2 = 0.06$$

elliptic flow

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The ρ^0 spin alignment in blast wave model



The spin alignment of the ρ^0 meson at z = 0 for $|\eta| < 1$ in the blast wave model with the elliptic flow.

Conclusion

- Because of the strong ρ π interaction in hadron gas, the spin alignment of ρ mesons decreases rapidly. The initial value of the spin alignment can be easily washed out in several fm/c.
- The spin density matrix of ρ mesons has an influence on the CME signal $\Delta \gamma_{112}$. The contributions from $\delta \rho_{00}$ and $\text{Re}\rho_{1,-1}$ are dominant.
- In this work we only consider the local effect in collision terms, which proves that ρ mesons will reach local equilibrium rapidly. The spin alignment of ρ mesons may come from nonlocal effects.

Outline

- Shear induced spin alignment for Φ meson
- Evolution of the spin alignment for p meson in a pion gas (Local effect)
- Shear induced spin alignment for ρ meson (Nonlocal effect)

Spectral function

Interaction from SU(3) chiral perturbation theory

$$\mathcal{L}_{\text{int}} = ig_V A^{\mu} \left(\phi^{\dagger} \partial_{\mu} \phi - \phi \partial_{\mu} \phi^{\dagger} \right) + g_V^2 A_{\mu} A^{\mu} \phi^{\dagger} \phi, \qquad \qquad \phi: \text{ Scalar field}$$

A · Vector field

Dyson Schwinger equation in closed-time-path (CTP) formalism:

Spectral function

Self energy:

C. Gale and J. I. Kapusta, Nucl. Phys. B 357, 65 (1991)

Linear response theory

Local Equilibrium Density Operator:

$$\widehat{\rho}_{LE} = \frac{1}{Z_{LE}} \exp\left[-\int_{\Sigma(\tau)} d\Sigma \ n_{\mu} \left(\widehat{T}^{\mu\nu}(x)\beta_{\nu}(x) - \overline{\zeta(x)}\widehat{j}^{\mu}(x)\right)\right]$$
Vanishes for
 ρ^{0} meson
F. Becattini et al. Particles 2, 197 (2019)

The linear response of $\hat{O}(x)$ to the perturbation $\partial_{\mu}\beta_{\nu}$:

$$\begin{split} \left\langle \hat{O}(x) \right\rangle - \left\langle \hat{O}(x) \right\rangle_{\text{LE}} &= \partial_{\mu} \beta_{\nu}(x) \lim_{K^{\mu} \to 0} \frac{\partial}{\partial K_{0}} \\ \times \text{Im} \left[iT(x) \int_{-\infty}^{t} d^{4}x' \left\langle \left[\hat{O}(x), T^{\mu\nu}(x') \right] \right\rangle_{\text{LE}} e^{-iK \cdot (x'-x)} \right] \\ T^{\mu\nu} &= F^{\mu}_{\ \rho} F^{\rho\nu} + m^{2}_{V} A^{\mu} A^{\nu} - g^{\mu\nu} \left(-\frac{1}{4} F_{\rho\sigma} F^{\rho\sigma} + \frac{1}{2} m^{2}_{V} A_{\rho} A^{\rho} \right) \end{split}$$

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Linear response theory

The next-to-leading order of Green's function:

$$G_{<,\text{NLO}}^{\mu\nu}(x,p) = 2T \overline{\xi_{\gamma\lambda}} \frac{\partial n_B(p_0)}{\partial p_0} I^{\mu\nu\gamma\lambda}(p)$$

Thermal shear: $\xi_{\gamma\lambda} = \partial_{(\gamma}\beta_{\lambda)}$

Longitudinal and transverse projectors:

$$\Delta_L^{\mu\nu}(p) \equiv \frac{\Delta^{\mu\rho} u_\rho \Delta^{\nu\sigma} u_\sigma}{\Delta^{\rho\sigma} u_\rho u_\sigma},$$

$$\Delta_T^{\mu\nu}(p) \equiv \Delta^{\mu\nu} - \Delta_L^{\mu\nu}.$$

$$I^{\mu\nu\gamma\lambda}(p) \equiv -\left[g^{\lambda\gamma}\left(p^2 - m^2\right) - 2p^{\lambda}p^{\gamma}\right]\left(\Delta_L^{\mu\nu}\rho_L^2 + \Delta_T^{\mu\nu}\rho_T^2\right) + 2\left(p^2 - m^2\right)\left(\Delta_L^{\mu\lambda}\rho_L + \Delta_T^{\mu\lambda}\rho_T\right)\left(\Delta_L^{\nu\gamma}\rho_L + \Delta_T^{\nu\gamma}\rho_T\right)$$

Feng Li et al. 2206.11890

The total Green's function:

$$G_{<}^{\mu\nu}(x,p) = G_{<,\text{LO}}^{\mu\nu}(x,p) + G_{<,\text{NLO}}^{\mu\nu}(x,p)$$
Off-shell effect
Thermal shear effect (nonlocal)

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Spin density matrix

Corrections for spin density matrix:

$$\delta \rho_{\lambda_{1}\lambda_{2}}(\mathbf{p}) = \frac{\int_{0}^{\infty} dp_{0} \int d\Sigma^{\mu} p_{\mu} \overline{L_{\mu\nu}(\lambda_{1},\lambda_{2},p)} \left[G_{<,\mathrm{LO}}^{\mu\nu}(x,p) + G_{<,\mathrm{NLO}}^{\mu\nu}(x,p) \right]}{-\int_{0}^{\infty} dp_{0} \int d\Sigma^{\mu} p_{\mu} \Delta_{\mu\nu}(p) \left[G_{<,\mathrm{LO}}^{\mu\nu}(x,p) + G_{<,\mathrm{NLO}}^{\mu\nu}(x,p) \right]} \\ \mathbf{F}_{\mathbf{h}}(\lambda,p_{on}) \qquad \qquad \mathbf{F}_{\mathbf{h}}(\lambda,p_{on}) \qquad \mathbf{F}_{\mathbf{h}}(\lambda,p_{on}) \\ \mathbf{F}_{\mathbf{h}}(\lambda,p_{on}) \qquad \mathbf{F}_{\mathbf{h}}(\lambda,p_{on}) \\ \mathbf{F}_{\mathbf{h}}(\lambda,p_{on}) \qquad \mathbf{F}_{\mathbf{h}}(\lambda,p) \\ \mathbf{F}_{\mathbf{h}}$$

 $\xi^{\mu\nu}, \Sigma^{\mu}$ by drodynamical model CLVisc

Xiang-Yu Wu, Phys. Rev. C 105, 064909 (2022)

Numerical result for ρ_{00}



- Thermal shear induces negative $\delta \rho_{00}$ at the order of $O(10^{-3})$;
- ho_{00} decreases when p_T goes larger, when $p_T > 1.5 GeV$, $\delta \rho_{00} \sim -0.01$.

 ρ_{00} as a function of p_T :



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Numerical result for ρ_{00}

ρ_{00} as a function of ϕ :



- $\delta \rho_{00}$ is positive for $\phi = \pi/2, 3\pi/2$ and negative for $\phi = 0, \pi$.
- Thermal shear has a negative contribution to ρ_{00} for all ϕ .

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Numerical result for $Re\rho_{-1,1}$



Numerical result for $Re\rho_{-1,1}$

$Re\rho_{-1,1}$ as a function of ϕ :



- $Re\rho_{-1,1}$ is positive for $\phi = 0, \pi$ and negative for $\phi = \pi/2, 3\pi/2$.
- Thermal shear has a negative contribution to $Re\rho_{-1,1}$.

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Conclusion

- Although the $\rho \pi$ interaction can wash out the initial spin alignment of ρ mesons, the **spectral effect** and **thermal shear effect** can induce local and global spin alignment for ρ mesons;
- The correction for ρ meson's density matrix is calculated through linear response theory. $\delta \rho_{00}$ and $Re \rho_{-1,1}$ are both negative at the order $10^{-3} \sim 10^{-2}$ and decrease with p_T ;
- The global corrections for spin density matrix are resulted from the thermal shear effect (NLO)(nonlocal), while the corrections as a function of azimuthal angle are mainly resulted from the spectral effect (LO).

Summary

- 1. The spin density matrix of ρ mesons has an influence on the **CME signal** $\Delta \gamma_{112}$, especially for the elements ρ_{00} and $Re\rho_{-1,1}$.
- 2. The width of ρ meson is very large, so the evolution of ρ meson in the hadron phase should be considered.
- 3. Because of the strong $\rho \pi$ interaction in hadron gas, the spin alignment of ρ mesons **decreases rapidly**, so the messages carried from QGP can be washed out.
- 4. Thermal shear induces a negative global correction to ρ_{00} and $Re\rho_{-1,1}$ at the order 10^{-3} , and for high p_T region, it will reach the order of 10^{-2} .

Outlook

- The contributions from other nonlocal effects (like thermal vorticity) should be considered.
- The interaction in hadron phase is important for ρ meson. Is it important for other particles (like K*⁰), especially for those with a short lifetime? Some experimental data may be explained in this way.



Thanks



