

# Hadronic Matter and Electromagnetic Probes

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September 1, 2009



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# Outline

## 1 Electromagnetic probes in heavy-ion collisions

- Vector mesons and electromagnetic probes
- Sources of dileptons

## 2 Comparison to NA60 data

- Invariant-mass spectra
- $m_T$  spectra and slope analysis

## 3 Conclusions and Outlook

# Electromagnetic probes in heavy-ion collisions

- $\gamma, \ell^\pm$ : no strong interactions
- reflect whole “history” of collision:
  - from pre-equilibrium phase
  - from thermalized medium  
**QGP and hot hadron gas**
  - from VM decays after thermal freezeout

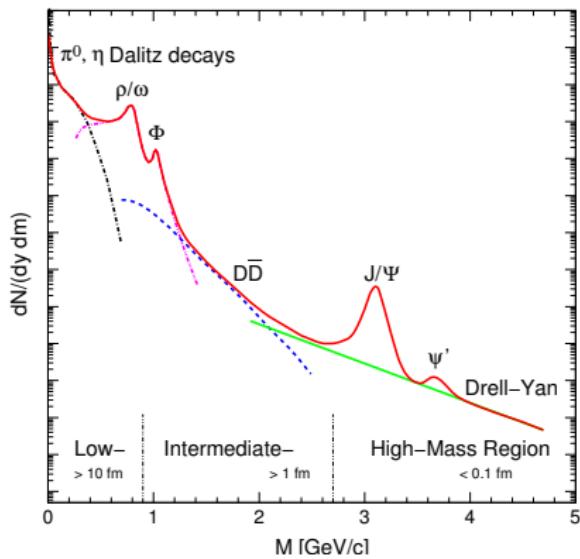
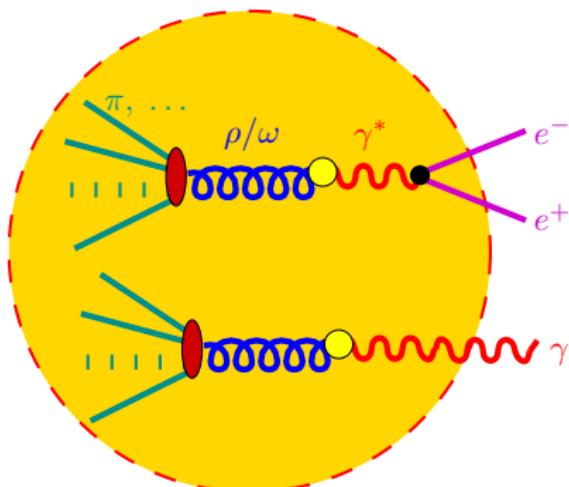


Fig. by A. Drees

# Vector Mesons and electromagnetic Probes

- photon and dilepton thermal emission rates given by same electromagnetic-current-correlation function ( $J_\mu = \sum_f Q_f \bar{\psi}_f \gamma_\mu \psi_f$ )

[L. McLerran, T. Toimela 85, H. A. Weldon 90, C. Gale, J.I. Kapusta 91]

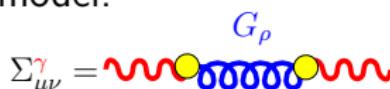
$$\Pi_{\mu\nu}^{<}(q) = \int d^4x \exp(iq \cdot x) \langle J_\mu(0) J_\nu(x) \rangle_T = -2 f_B(q_0) \operatorname{Im} \Pi_{\mu\nu}^{(\text{ret})}(q)$$

$$q_0 \frac{dN_\gamma}{d^4x d^3\vec{q}} = \frac{\alpha}{2\pi^2} g^{\mu\nu} \operatorname{Im} \Pi_{\mu\nu}^{(\text{ret})}(q) \Big|_{q_0=|\vec{q}|} f_B(q_0)$$

$$\frac{dN_{e^+e^-}}{d^4x d^4q} = -g^{\mu\nu} \frac{\alpha^2}{3q^2\pi^3} \operatorname{Im} \Pi_{\mu\nu}^{(\text{ret})}(q) \Big|_{q^2=M_{e^+e^-}^2} f_B(q_0)$$

- to lowest order in  $\alpha$ :  $e^2 \Pi_{\mu\nu} \simeq \Sigma_{\mu\nu}^{(\gamma)}$

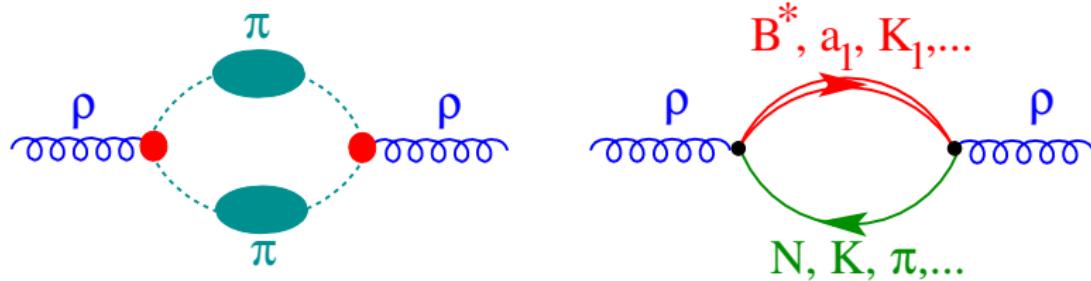
- vector-meson dominance model:



- derivable from partition sum  $Z(V, T, \mu, \Phi)$ !

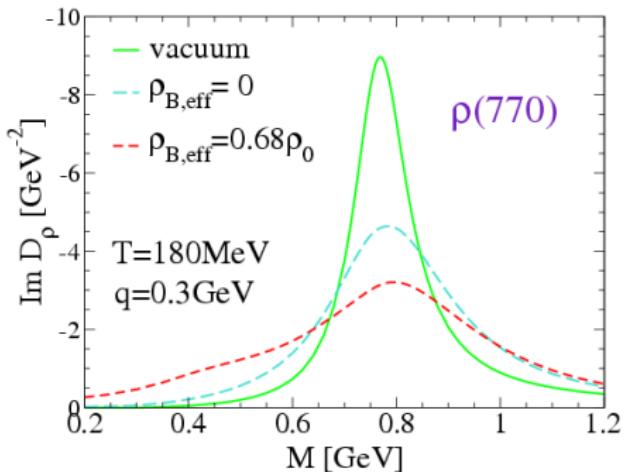
# Hadronic many-body theory

- HMBT for vector mesons [Ko et al, Chanfray et al, Herrmann et al, Rapp et al, ...]
- $\pi\pi$  interactions and baryonic excitations

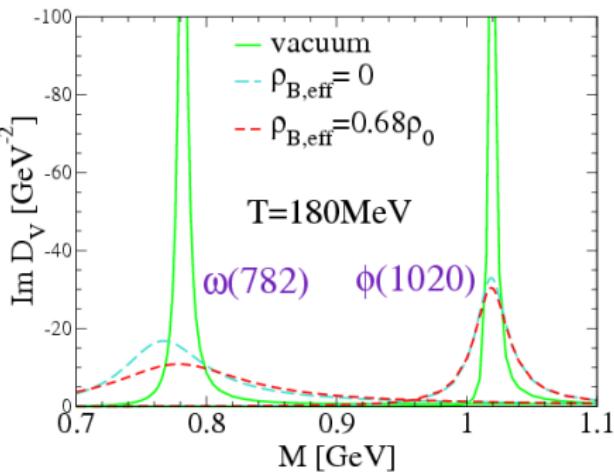


- +corresponding vertex corrections  $\Leftrightarrow$  gauge invariance
- **Baryon (resonances)** important, even at RHIC with low **net** baryon density  $n_B - n_{\bar{B}}$
- reason:  $n_B + n_{\bar{B}}$  relevant (CP inv. of strong interactions)

# In-medium spectral functions and baryon effects

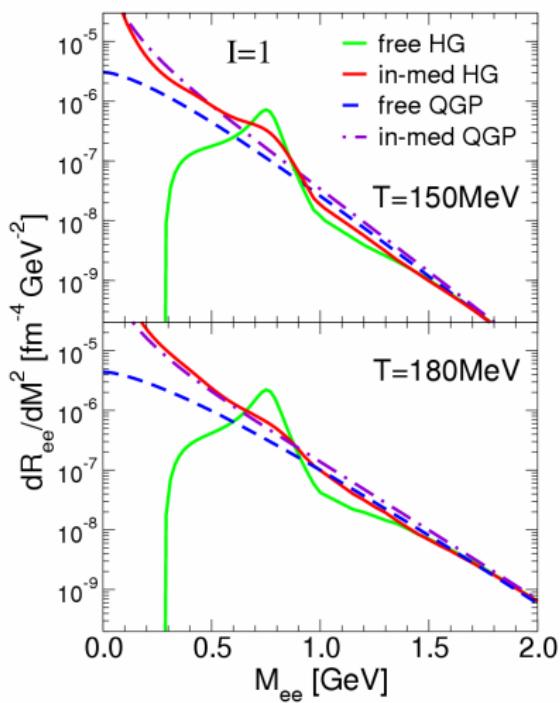


[R. Rapp, J. Wambach 99]



- baryon effects important
  - large contribution to broadening of the peak
  - responsible for most of the strength at small  $M$

# Dilepton rates: Hadron gas $\leftrightarrow$ QGP



- in-medium hadron gas matches with QGP
- similar results also for  $\gamma$  rates
- “quark-hadron duality”!?
- indirect evidence for chiral-symmetry restoration

# Sources of dilepton emission in heavy-ion collisions

- ① initial hard processes: Drell Yan

- ② “core”  $\Leftrightarrow$  emission from thermal source [McLerran, Toimela 1985]

$$\frac{1}{q_T} \frac{dN^{(\text{thermal})}}{dM dq_T} = \int d^4x \int dy \int M d\varphi \frac{dN^{(\text{thermal})}}{d^4x d^4q} \text{Acc}(M, q_T, y)$$

- ③ “corona”  $\Leftrightarrow$  emission from “primordial” mesons (jet-quenching)

- ④ after thermal freeze-out  $\Leftrightarrow$  emission from “freeze-out” mesons

[Cooper, Frye 1975]

$$N^{(\text{fo})} = \int \frac{d^3q}{q_0} \int q_\mu d\sigma^\mu f_B(u_\mu q^\mu / T) \frac{\Gamma_{\text{meson} \rightarrow \ell^+ \ell^-}}{\Gamma_{\text{meson}}} \text{Acc}$$

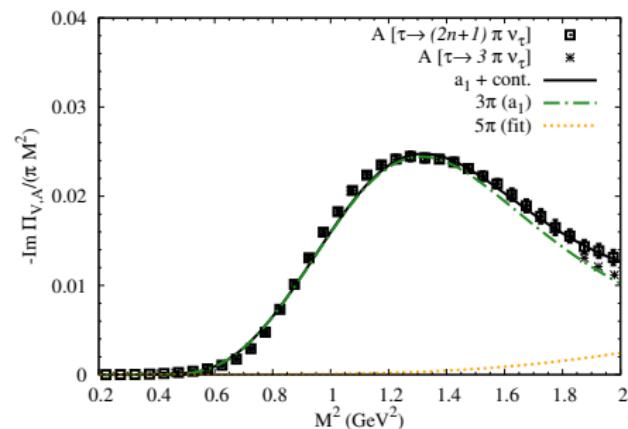
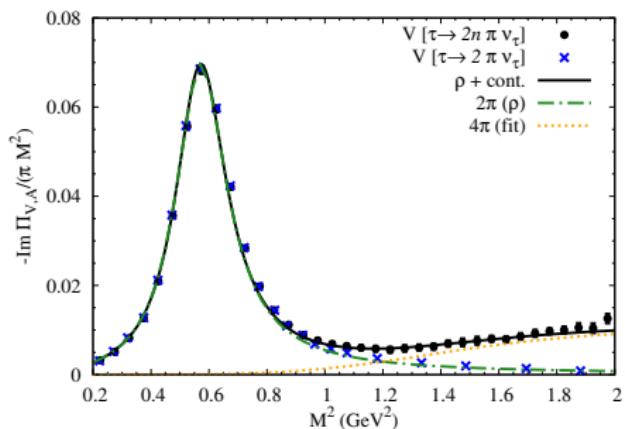
- additional factor  $\gamma = q_0/M$  compared to thermal emission
- physical reason

- thermal source rate  $\propto \tau_{\text{med}} \frac{\Gamma_{\text{meson} \rightarrow \ell^+ \ell^-}}{\gamma}$

- decay of mesons after fo: rate  $\propto \frac{\Gamma_{\text{meson} \rightarrow \ell^+ \ell^-}}{\Gamma_{\text{meson}}}$

# Intermediate masses: hadronic “ $4\pi$ contributions”

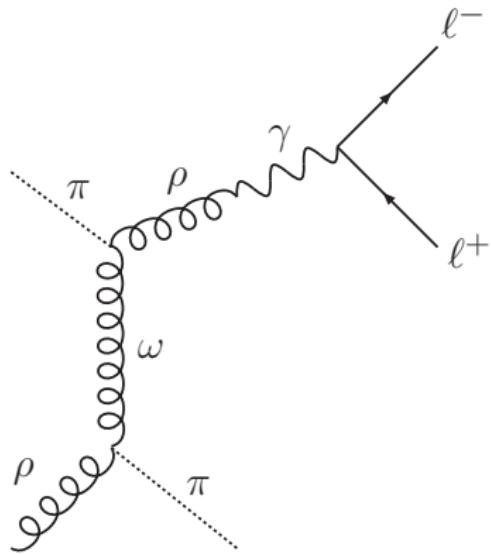
- e.m. current-current correlator  $\Leftrightarrow \tau \rightarrow 2n\pi$



- “ $4\pi$  contributions”:  $\pi + \omega, a_1 \rightarrow \mu^+ + \mu^-$
- leading-order virial expansion for “four-pion piece”
- additional strength through “chiral mixing”

# Radiation from thermal sources: Meson t-channel exchange

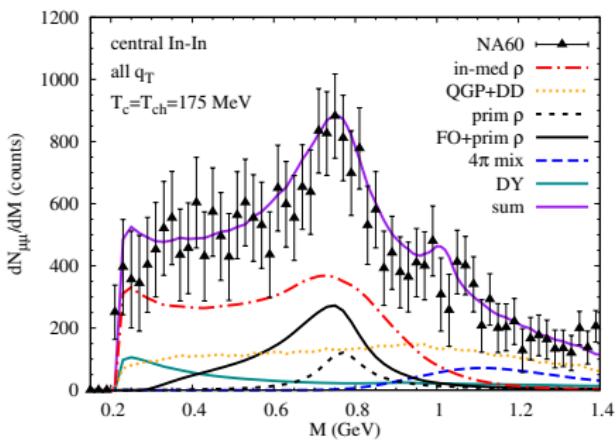
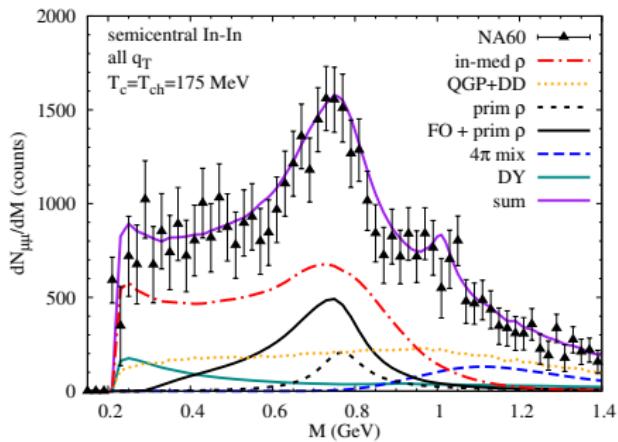
- motivation:  $q_T$  spectra too soft compared to NA60 data
- **thermal contributions** not included in models so far



- also for  $\pi$ ,  $a_1$

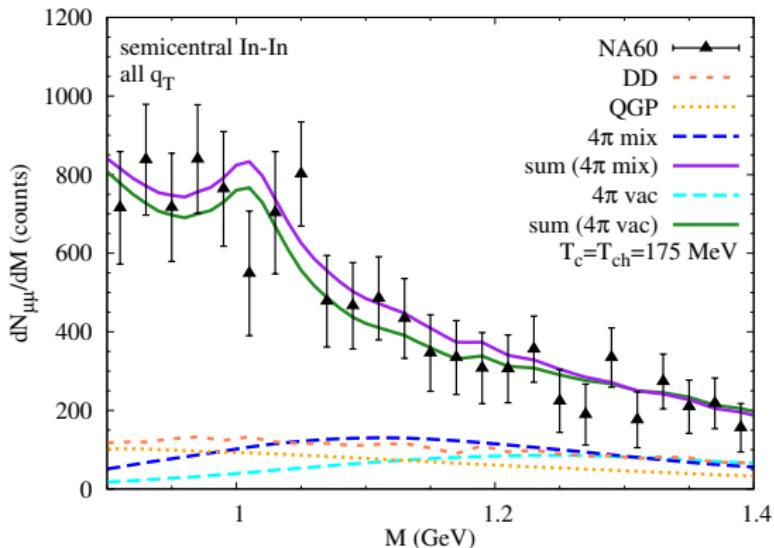
# Excess spectra

- Fireball with “standard” EoS-A ( $T_c = T_{\text{chem}} = 175 \text{ MeV}$ )
- overall normalization  $\Leftrightarrow$  total fireball lifetime
- relative normalization of thermal radiation fixed by rates
- rates integrated over time, volume,  $\vec{q}$  including NA60 acceptance



- good description of data

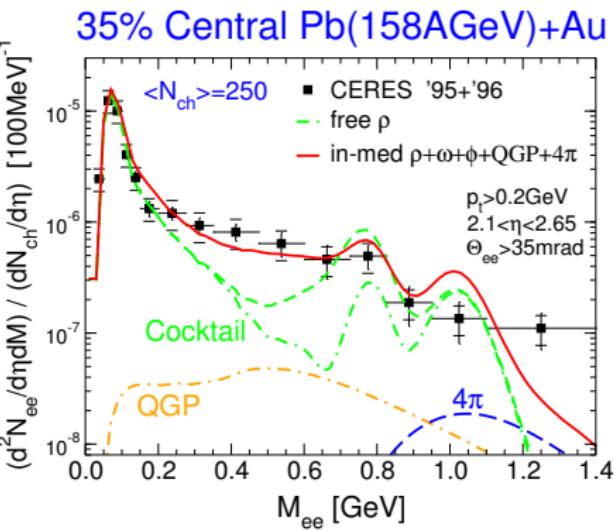
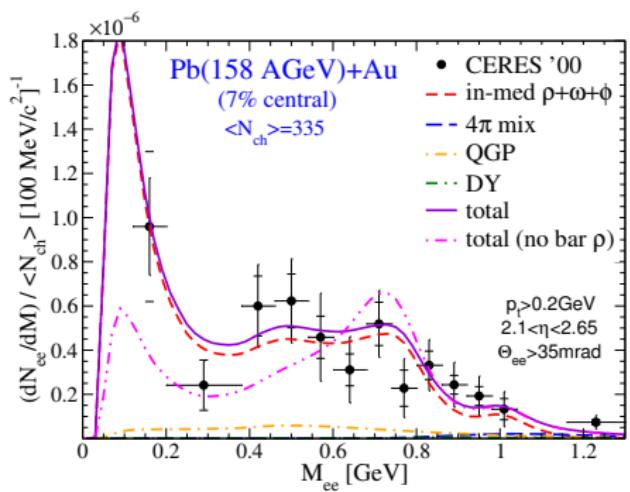
# Excess spectra: IMR and multi-pion contributions



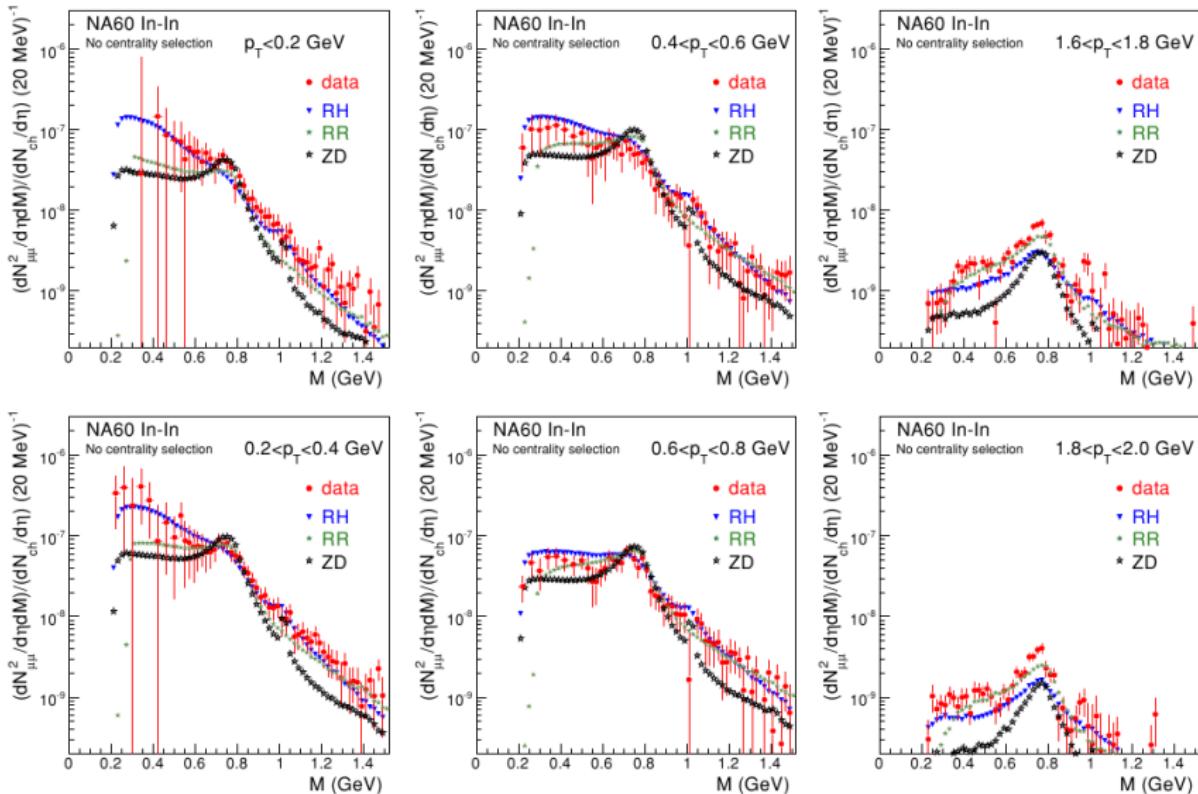
- “ $4\pi$  contributions” ( $\pi + \omega, a_1 \rightarrow \mu^+ + \mu^-$ )
- slightly enhanced by VA mixing

# CERES/NA45 dielectron spectra

- good agreement also for **dielectron** spectra in 158 GeV Pb-Au
- allows further check of **low-mass tail from baryon effects** down to  $M \rightarrow 2m_e$



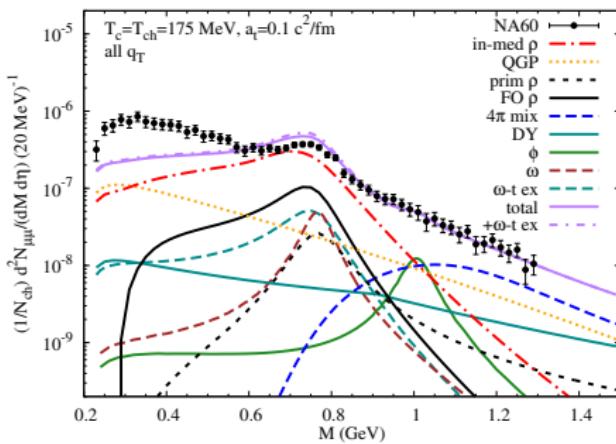
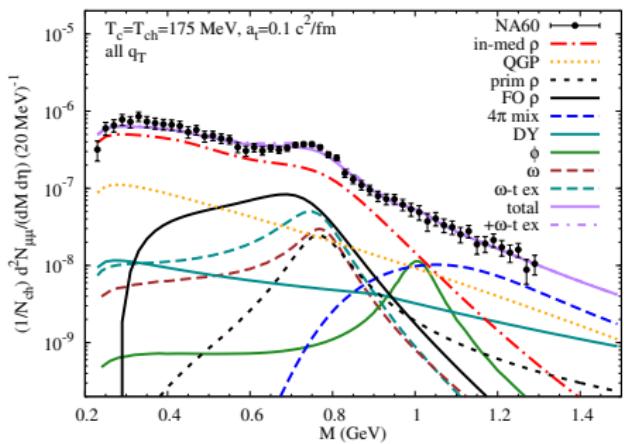
# Excess spectra: acceptance-corrected mass spectra



ZD: [K. Dusling, D. Teaney, I. Zahed 2007], RR: [J. Ruppert, T. Renk et al 2008], RH: [HvH, R. Rapp 2008]

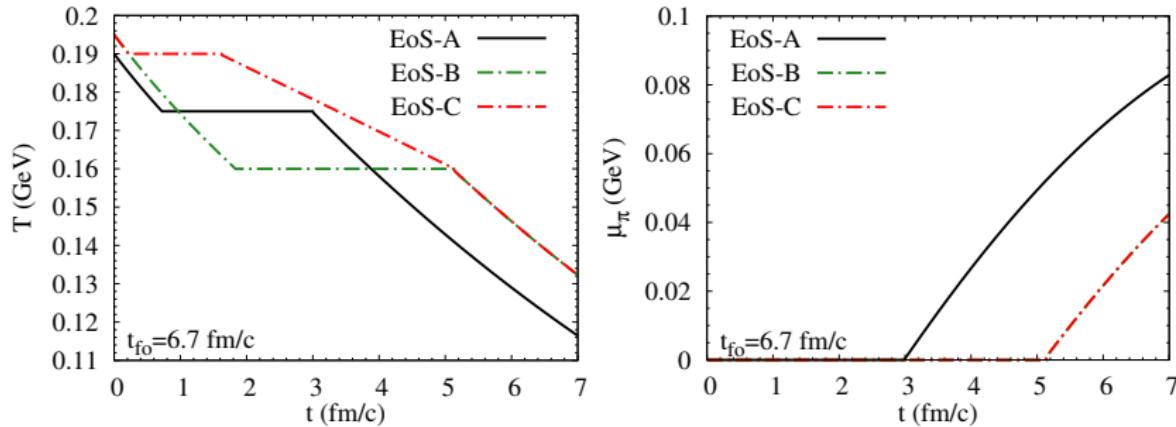
# Importance of baryon effects

- Baryonic interactions important!
- in-medium broadening
- low-mass tail!



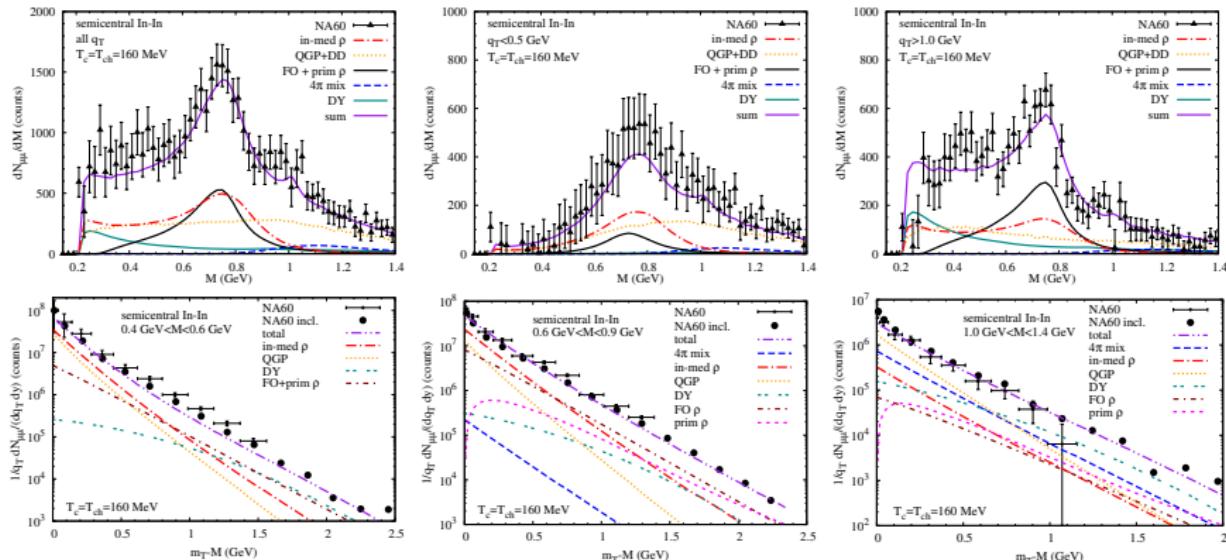
# Sensitivity to $T_c$ and hadro-chemistry

- recent lattice QCD:  $T_c \simeq 190\text{-}200 \text{ MeV}$  or  $T_c \simeq 150\text{-}160 \text{ MeV}$ ?
- thermal-model fits to hadron ratios:  $T_{\text{chem}} \simeq 150\text{-}160 \text{ MeV}$



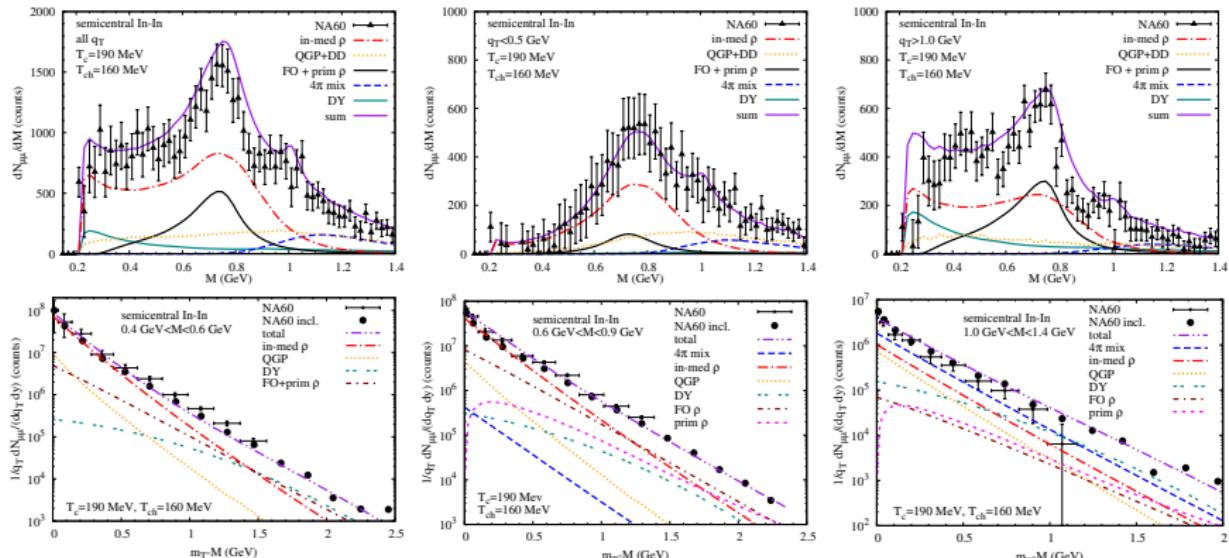
- EoS-A:  $T_c = T_{\text{chem}} = 175 \text{ MeV}$
- EoS-B:  $T_c = T_{\text{chem}} = 160 \text{ MeV}$
- EoS-C:  $T_c = 190 \text{ MeV}$ ,  $T_{\text{chem}} = 160 \text{ MeV}$ 
  - $T_c \geq T \geq T_{\text{chem}}$ : hadron gas in chemical equilibrium
- keep fireball parameters the same (including life time)

# EoS-B



- mass spectra comparable to EoS-A  $\leftrightarrow$  slight enhancement of fireball lifetime
- in IMR **QGP**  $>$  **multi-pion** contribution
- higher hadronic temperatures  $\Rightarrow$  slightly harder  $q_T$  spectra
- not enough to resolve discrepancy with data

# EoS-C



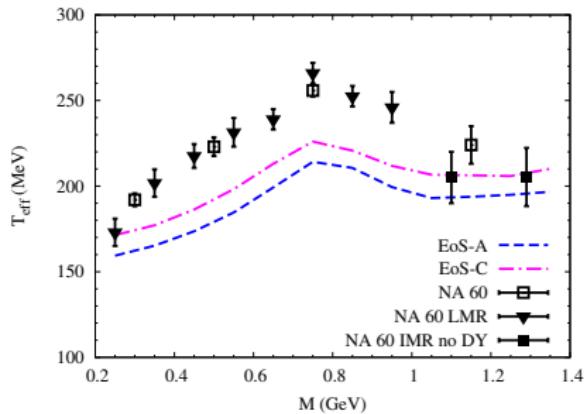
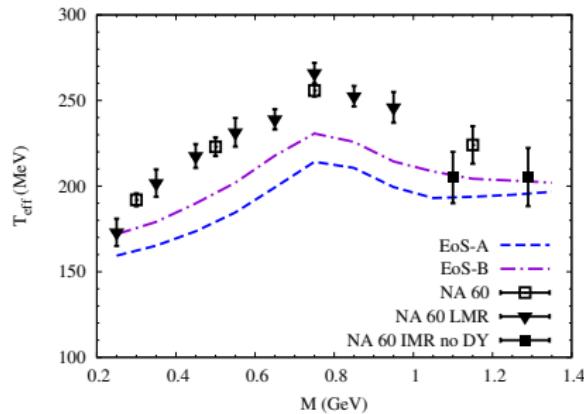
- mass spectra comparable to EoS-A  $\leftrightarrow$  slight reduction of fireball lifetime
- in IMR multi-pion  $\gg$  QGP contribution
- higher hadronic temperatures + high-density hadronic phase  $\Rightarrow$  harder  $q_T$  spectra
- better agreement with data

# Inverse-slope analysis

- to extract  $T_{\text{eff}}$  fit to

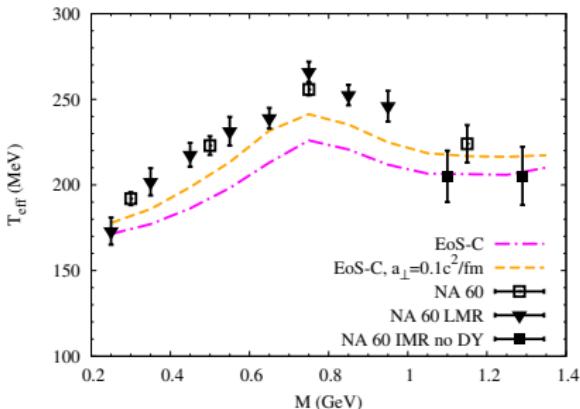
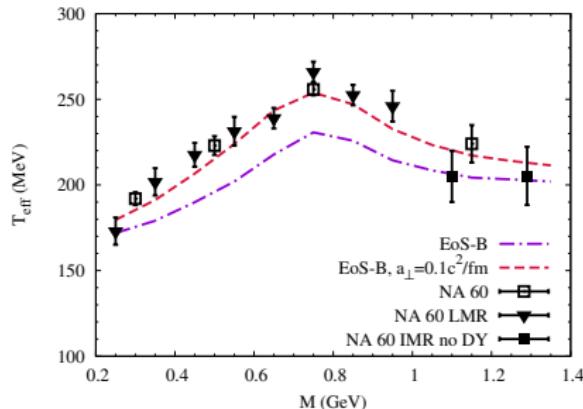
$$\frac{1}{q_T} \frac{dN}{dq_T} = \frac{1}{m_T} \frac{dN}{dm_T} = C \exp\left(-\frac{m_T}{T_{\text{eff}}}\right)$$

- fit of theoretical  $q_T$  spectra:  $1 \text{ GeV} < q_T < 1.8 \text{ GeV}$



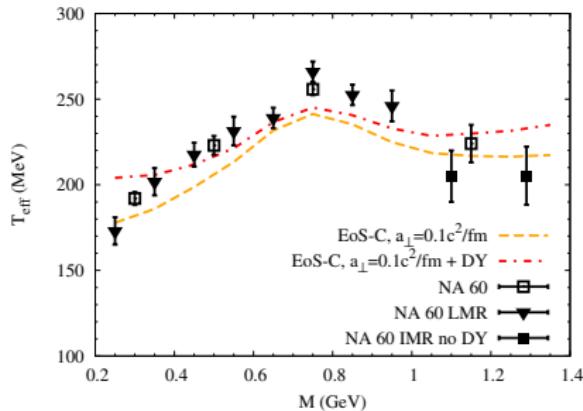
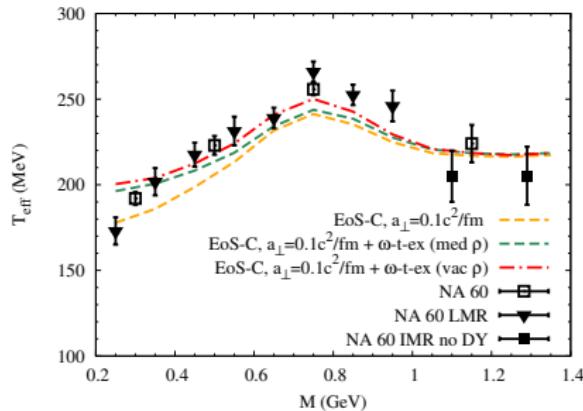
- standard fireball acceleration: **too soft  $q_T$  spectra**
- lower  $T_c$  in EoS-B and EoS-C helps (higher hadronic temperatures)
- NB: here, Drell Yan contribution taken out

# Inverse-slope analysis



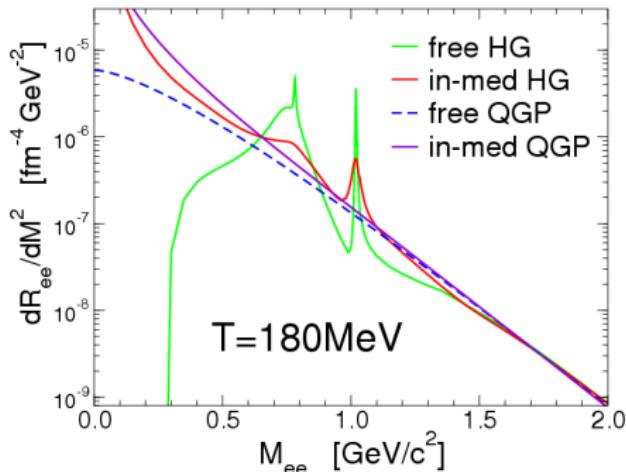
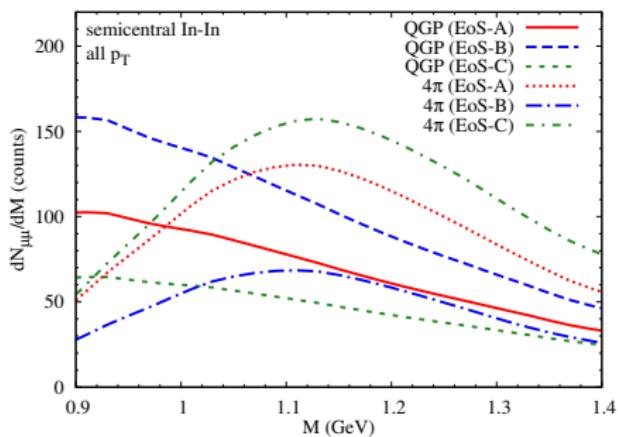
- enhance fireball acceleration to  $a_{\perp} = 0.1c^2/\text{fm}$
- effective at all stages of fireball evolution
- agreement in IMR not spoiled  $\Leftrightarrow$  dominated from earlier stages
- EoS-B harder  $\Leftrightarrow$  relative contribution of harder freezeout  $\rho$  decays vs. thermal  $\rho$ 's larger

# Inverse-slope analysis



- sensitivity to contributions from meson  $t$ -channel exchange
  - hardens low-mass region
  - using vacuum  $\rho$  in  $t$ -channel contribution: enhances slope in  $\rho$  region
- sensitivity to Drell-Yan contribution
  - for IMR: describes effect seen in data (open vs. solid square data point)
  - in LMR: too high around muon threshold  $\Leftrightarrow$  due to uncertainties in extrapolation to low  $M$ ?!

# IMR: QGP vs. multi-pion radiation



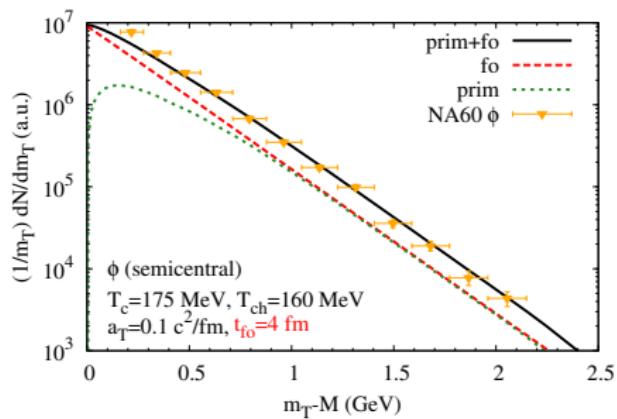
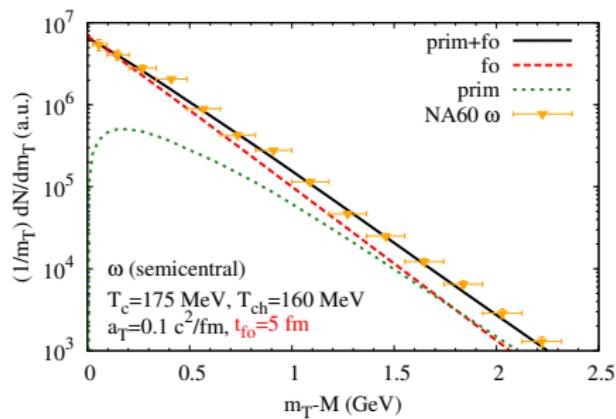
- **EoS-B:** QGP dominates over multi-pion radiation
- opposite in **EoS-A** and **EoS-C**
- multi-pion radiation dominantly from high-density hadronic phase

reason :  $dN_{ll}/dMdT \propto \text{Im } \Pi_{\text{em}}(M, T) \exp(-M/T) T^{-5.5}$

- radiation maximal for  $T = T_{\max} = M/5.5$
- hadronic and partonic radiation “dual” for  $T \sim T_c$   
**compatible with chiral-symmetry restoration!**

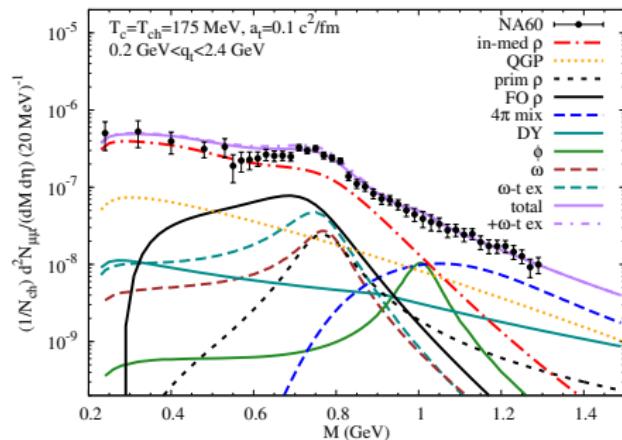
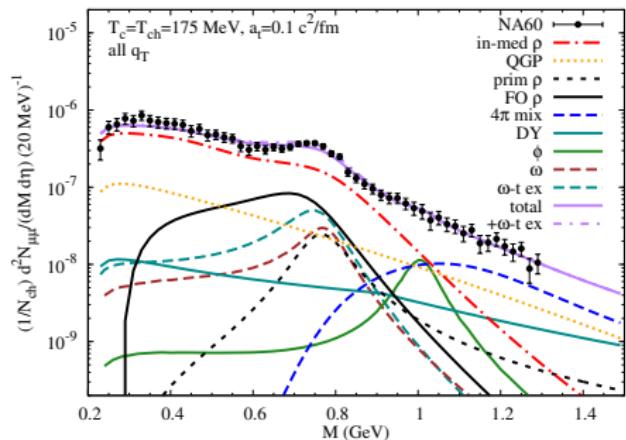
# Hadron spectra

- analysis of “cocktail”: **hadron- $m_T$  spectra**
- comparison to fireball evolution
- “sequential freeze-out” due to different coupling strength



# M spectra (in $p_T$ slices)

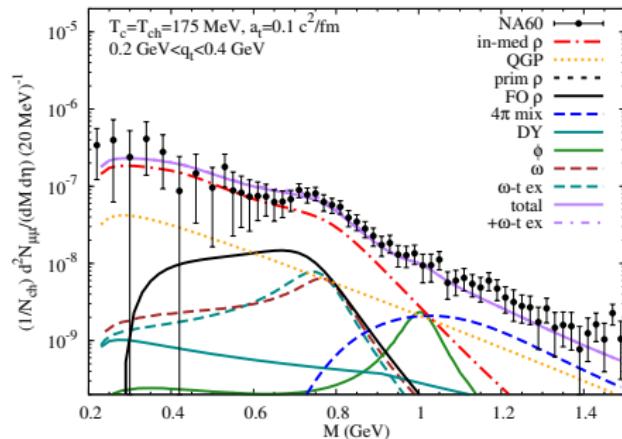
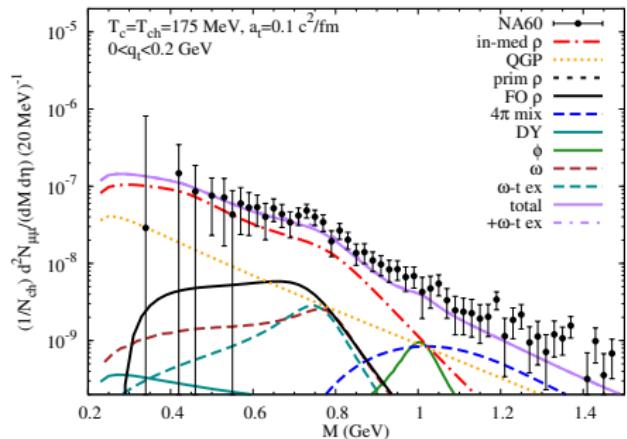
- EoS-A:  $T_c = T_{ch} = 175$  MeV
- transverse acceleration:  $a_\perp = 0.1 c^2/\text{fm}$



- norm corrected by  $\sim 3\%$  due to centrality correction  
(min-bias data:  $\langle N_{ch} \rangle = 120$ , calculation  $N_{ch} = 140$ )

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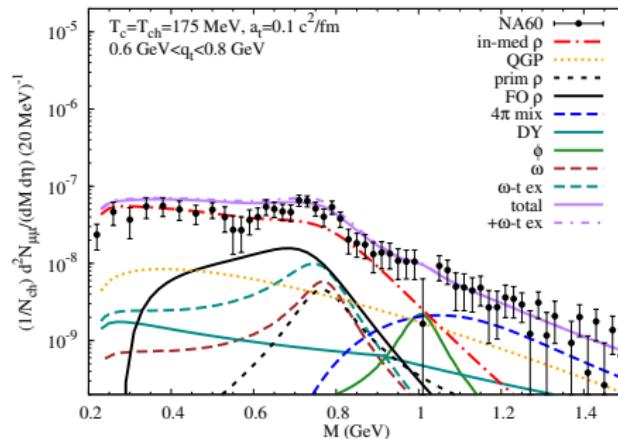
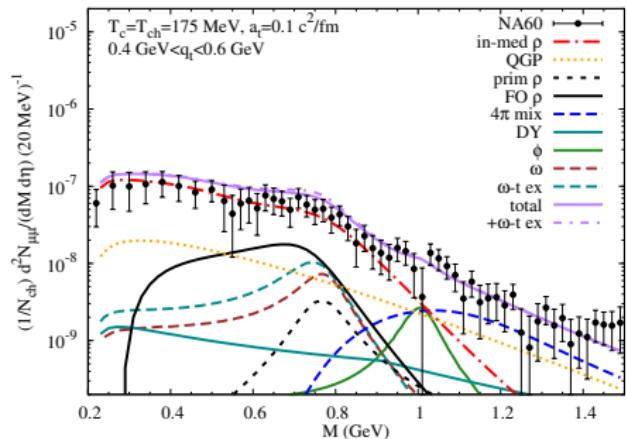
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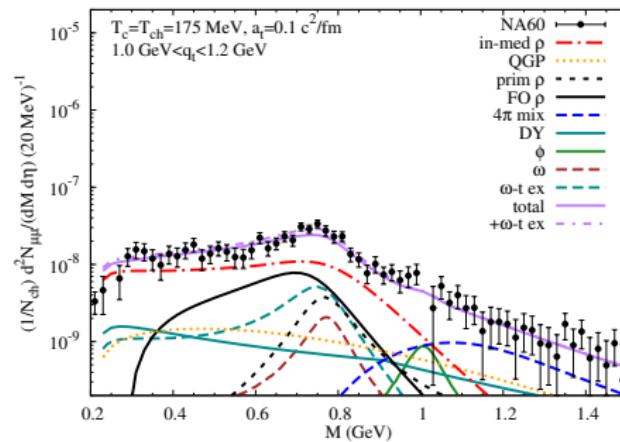
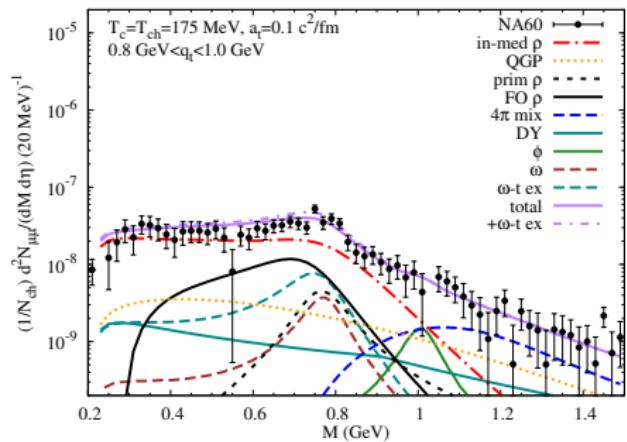
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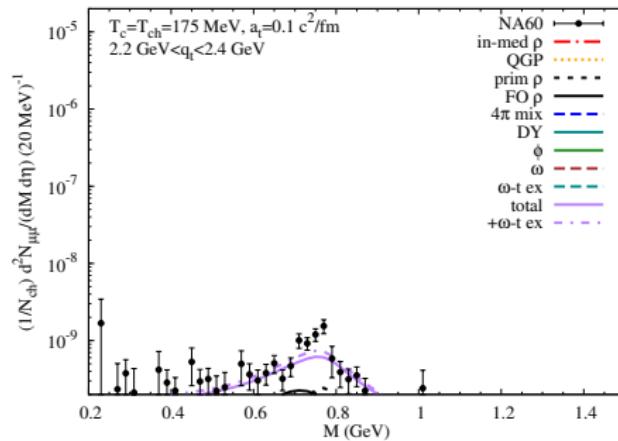
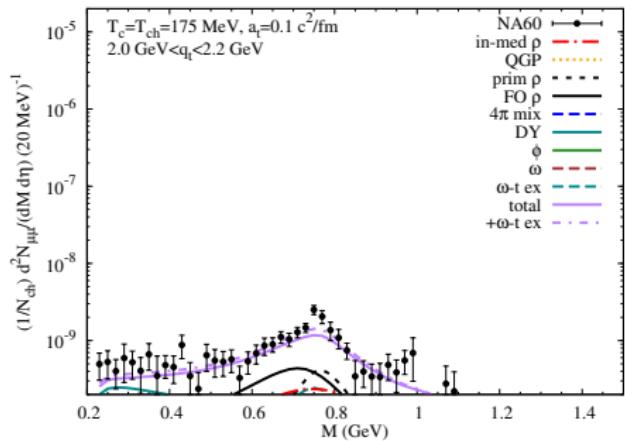
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# Conclusions and Outlook

- dilepton spectra  $\Leftrightarrow$  in-medium em. current correlator
- model for dilepton sources
  - radiation from thermal sources: QGP,  $\rho$ ,  $\omega$ ,  $\phi$
  - $\rho$ -decay after thermal freeze-out
  - decays of non-thermalized primordial  $\rho$ 's
  - Drell-Yan annihilation, correlated  $D\bar{D}$  decays
- invariant-mass spectra and medium effects
  - excess yield dominated by radiation from thermal sources
  - baryons essential for in-medium properties of vector mesons
  - melting  $\rho$  with little mass shift robust signal! (independent of  $T_c$ )
  - IMR well described by scenarios with radiation dominated either by QGP or multi-pion processes (depending on EoS)
    - Reason: mostly from thermal radiation around  $160 \text{ MeV} \leq T \leq 190 \text{ MeV}$   
 $\Leftrightarrow$  "parton-hadron" duality of rates  
 $\Leftrightarrow$  compatible with chiral-symmetry restoration!
  - dimuons in In-In (NA60), Pb-Au (CERES/NA45),  $\gamma$  in Pb-Pb (WA98)

# Conclusions and Outlook

- fireball/freeze-out dynamics  $\Leftrightarrow m_T$  spectra and effective slopes
  - “non-thermal sources” important for  $q_T \gtrsim 1$  GeV
  - lower  $T_c \Rightarrow$  higher hadronic temperatures  $\Rightarrow$  harder  $q_T$  spectra
  - to describe measured effective slopes  $a_\perp = 0.085c^2/\text{fm} \rightarrow 0.1c^2/\text{fm}$
  - off-equilibrium effects (viscous hydro)?
- Further developments
  - understand recent PHENIX results (large dilepton excess in LMR)
  - understand “DLS puzzle” (exp. confirmed by HADES)  
*NN (np!) bremsstrahlung!*
  - **vector-** should be complemented with **axial-vector**-spectral functions  
( $a_1$  as chiral partner of  $\rho$ )
  - constrained with IQCD via **in-medium Weinberg chiral sum rules**
  - **direct connection to chiral phase transition!**