

Electromagnetic Probes in Heavy-Ion Collisions II

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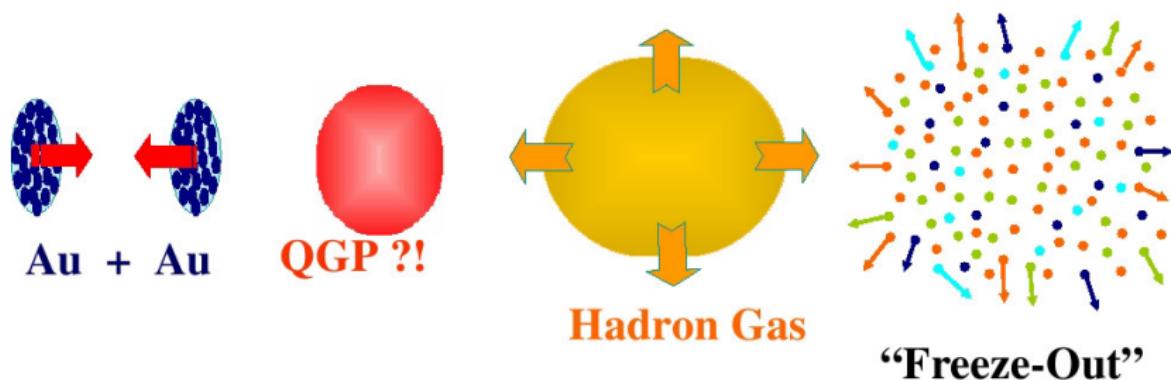
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- 3 In-medium current-current correlator
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 - QCD sum rules
- 4 Hadronic models for vector mesons
 - chiral symmetry constraints
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Heavy-ion phenomenology

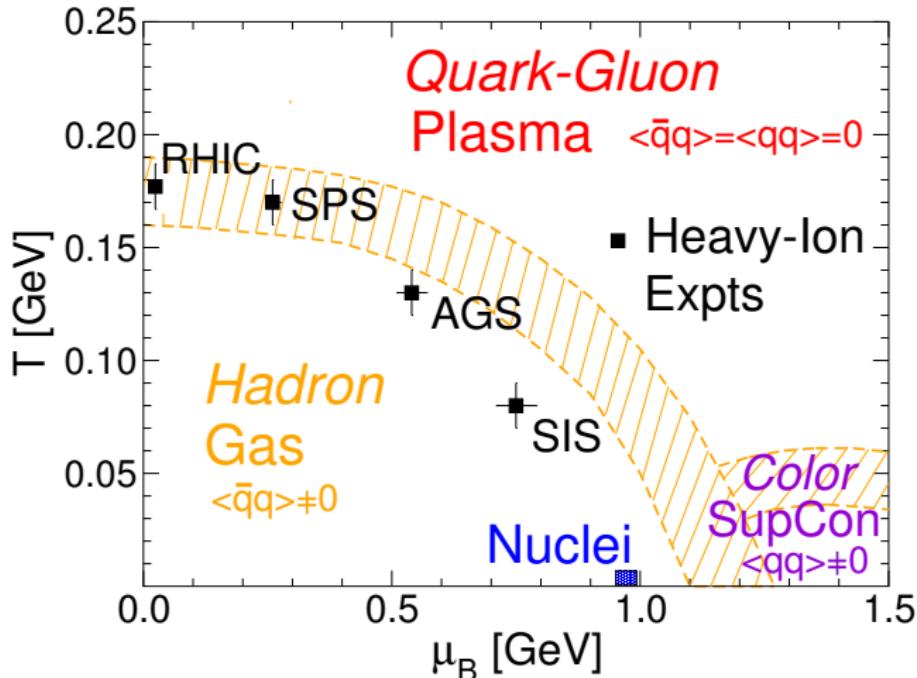
Heavy-ion collisions

- collisions of relativistic (**heavy**) nuclei
- many collisions of **partons** inside nucleons
- creation of many particles \Rightarrow **hot and dense fireball**
- formation of (**thermalized**) QGP?
- how to learn about properties of **QGP**?



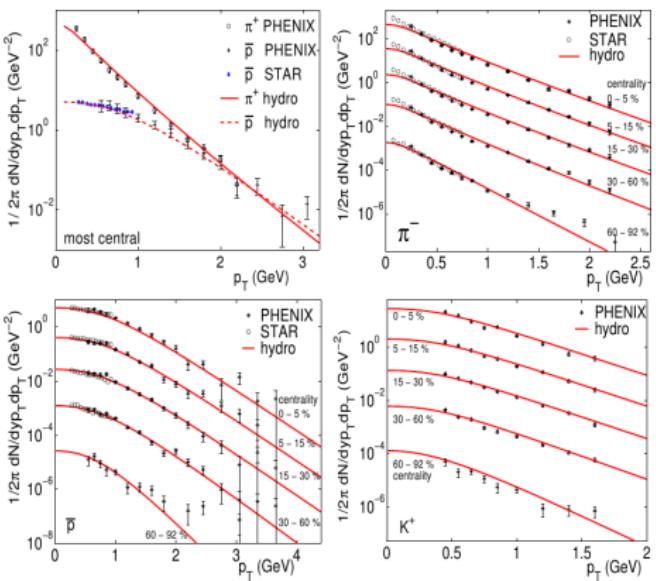
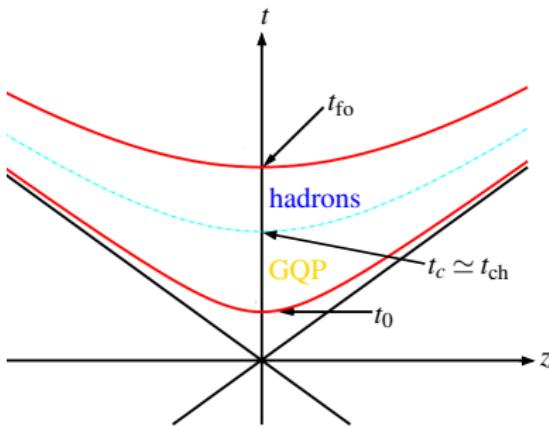
Phase diagram of strongly interacting matter

- hot and dense matter: quarks and gluons at high temperature
- high-energy collisions of quarks and gluons \Rightarrow “Deconfinement”
- quarks and gluons relevant degrees of freedom \Rightarrow Quark-Gluon-Plasma
- interactions still strong: fast thermalization!



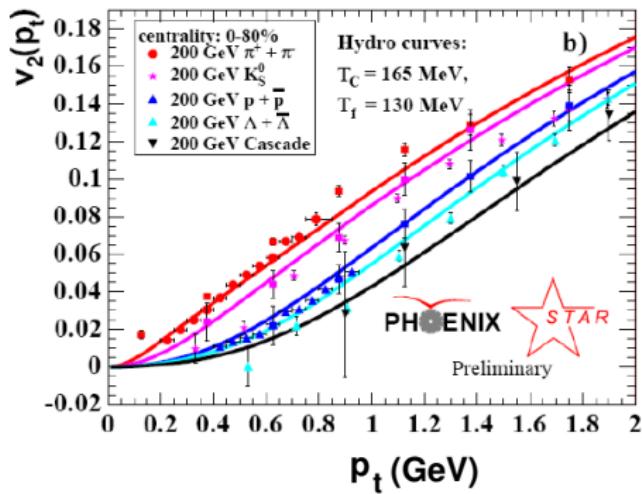
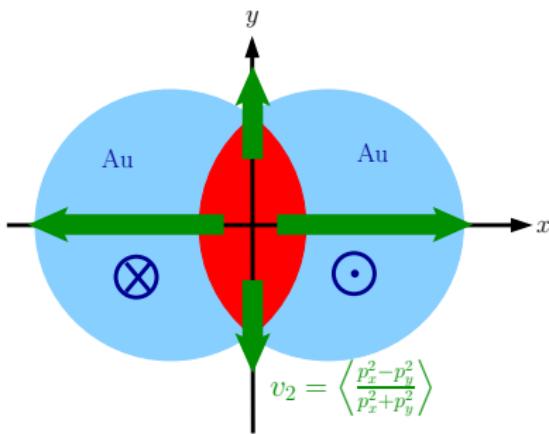
Hydrodynamical radial flow of the bulk

- ideal fluid in local thermal equilibrium
- hydrodynamical model for ultra-relativistic heavy-ion collisions
 - after short formation time ($t_0 \lesssim 1 \text{ fm}/c$)
 - QGP in local thermal equilibrium → hadronization at $T_c \simeq 160 - 190 \text{ MeV}$
 - chemical freeze-out: (inelastic collisions cease) $T_{\text{ch}} \simeq 160 - 175 \text{ MeV}$
 - thermal freeze-out: (also elastic scatterings cease)



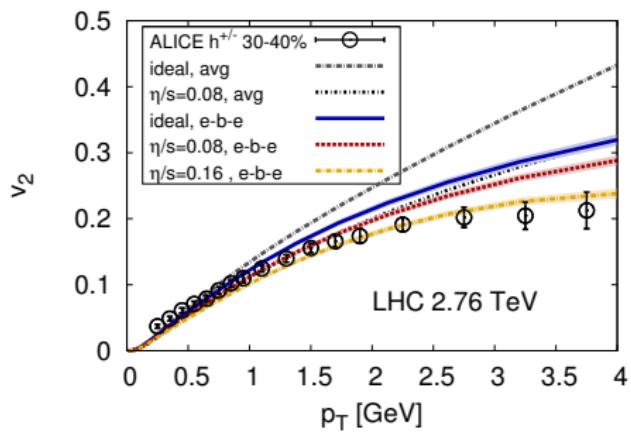
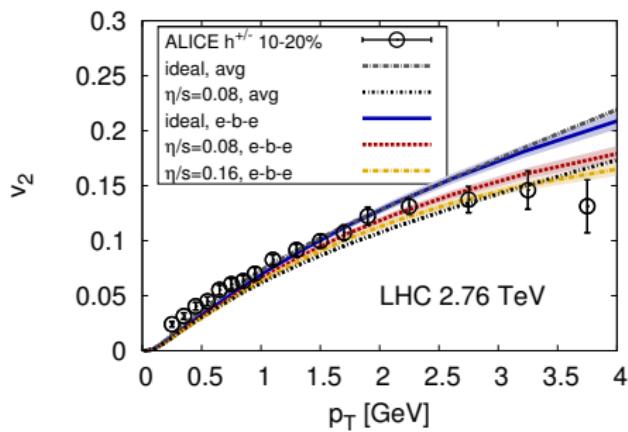
Hydrodynamical behavior

- low- p_T particle spectra compatible with **ideal-fluid** (hydrodynamics) \Rightarrow small shear-viscosity over entropy-density ratio, $\eta/s \simeq 1/(4\pi)$
- medium in **local thermal equilibrium** (after short formation time $\lesssim 1 \text{ fm}/c$)



Hydrodynamical behavior

- successful description with relativistic ideal and viscous hydrodynamics



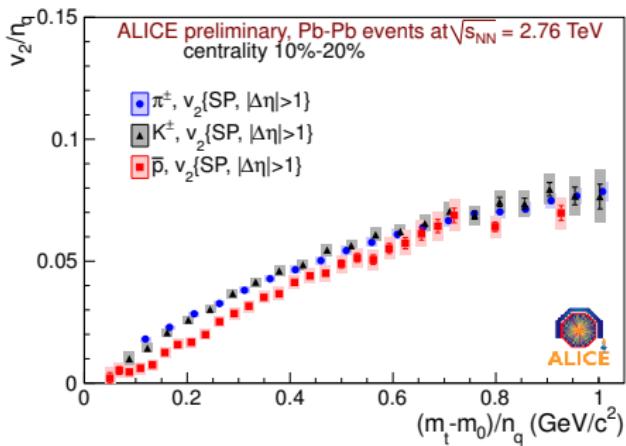
[SJG11]

Constituent-quark-number scaling of v_2

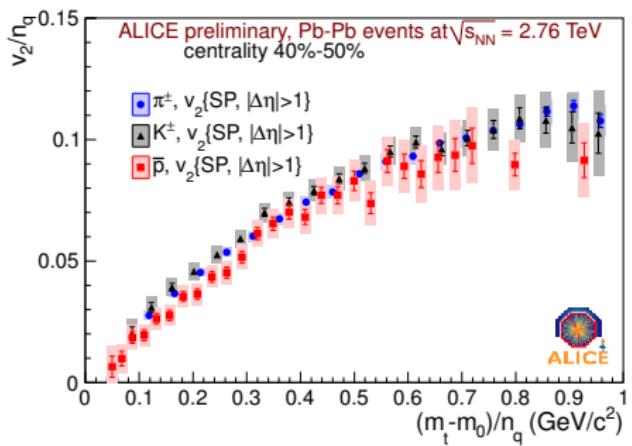
- Elliptic flow scales with number of **constituent quarks**

$$v_2^{(\text{had})}(p_T^{(\text{had})}) = n_q v_2^{(q)}(p_T^{(\text{had})}/n_q)$$

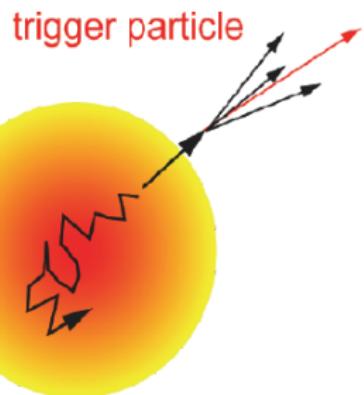
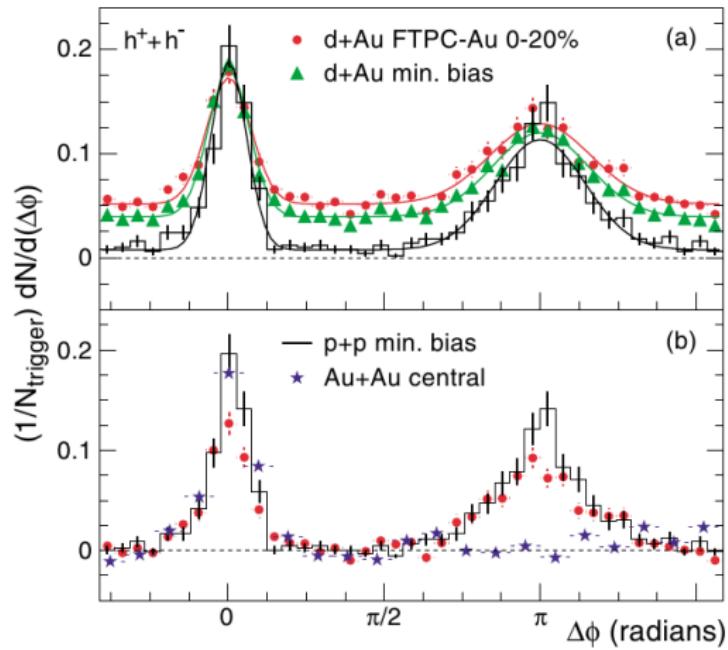
- recombination **Quarks** in the medium at T_c
- meson and baryon $v_2 = \simeq \text{sum of quark } v_2$'s



[Krz11]

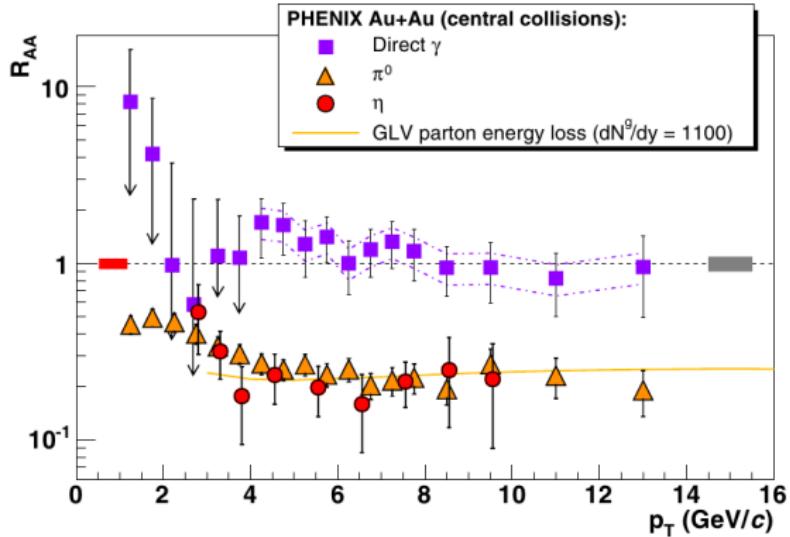


Jet quenching



- jets going through medium **suppressed**
- not seen in d+Au collisions \Rightarrow **medium effect!**
- suppression: **medium of high density** $\Rightarrow \rho > \rho_{\text{krit}}$

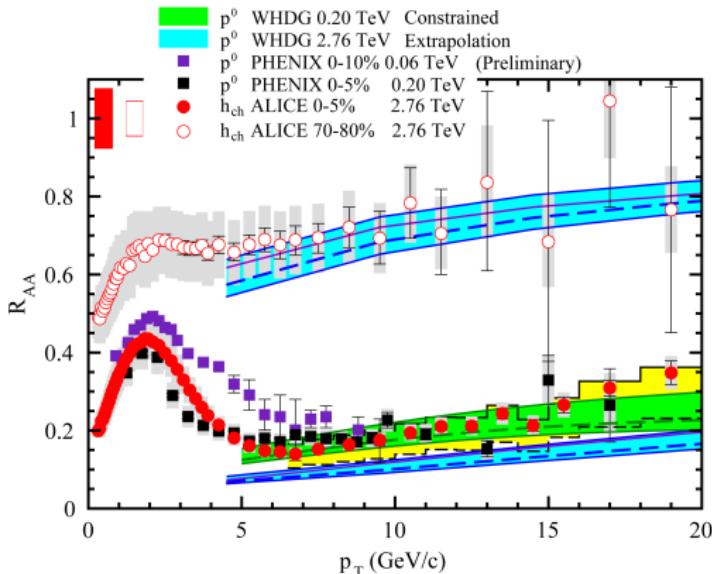
Jet quenching



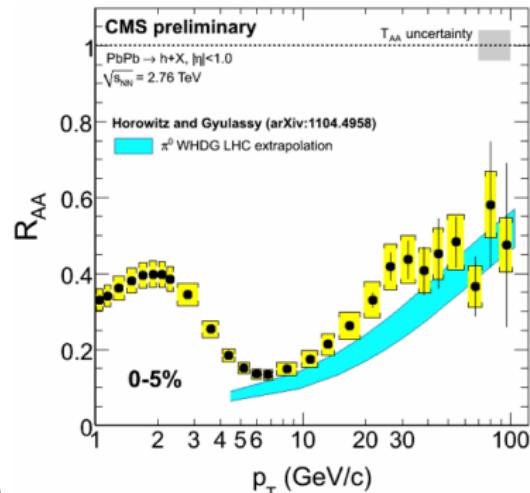
- comparison to pp collisions: $R_{AA} = \frac{dN_{AA}/dp_t}{N_{coll} dN_{pp}/dp_t}$
- $R_{AA} < 1$ for large p_t : jets absorbed by medium
- photons (γ) nearly unsuppressed: medium transparent for photons
- γ only electromagnetically interacting!

Jet quenching

- comparison to pp collisions: $R_{AA} = \frac{dN_{AA}/dp_t}{N_{coll} dN_{pp}/dp_t}$
- $R_{AA} < 1$ for large p_t : jets absorbed by medium



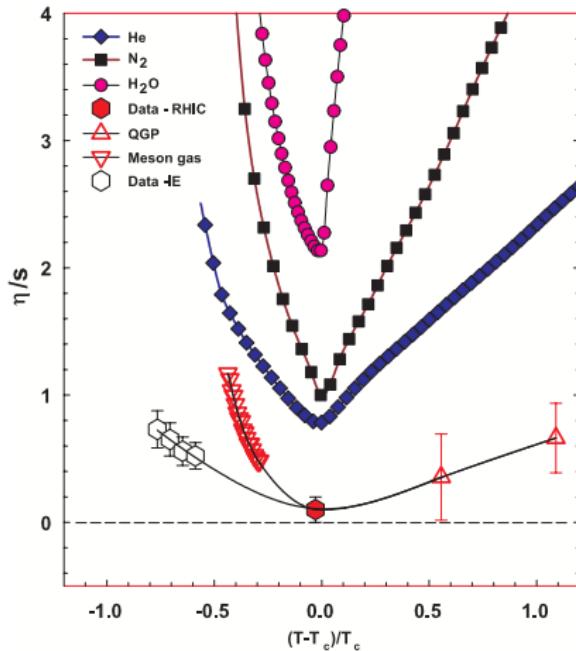
[HG08]



- energy loss: elastic scattering and radiation of gluons in QGP
- density of medium $> \rho_{\text{crit}}$!

QGP in HICs: “most sloshy liquid”?

- viscosity over entropy ratio: η/s
- measure for “perfectness” of a fluid
- from Heisenberg uncertainty relation (or AdS/CFT): $\eta/s \geq 1/(4\pi)$



[LAA⁺07]

Theory of electromagnetic probes

The McLerran-Toimela formula

- derivation of dilepton-production rate [MT85, GK91]

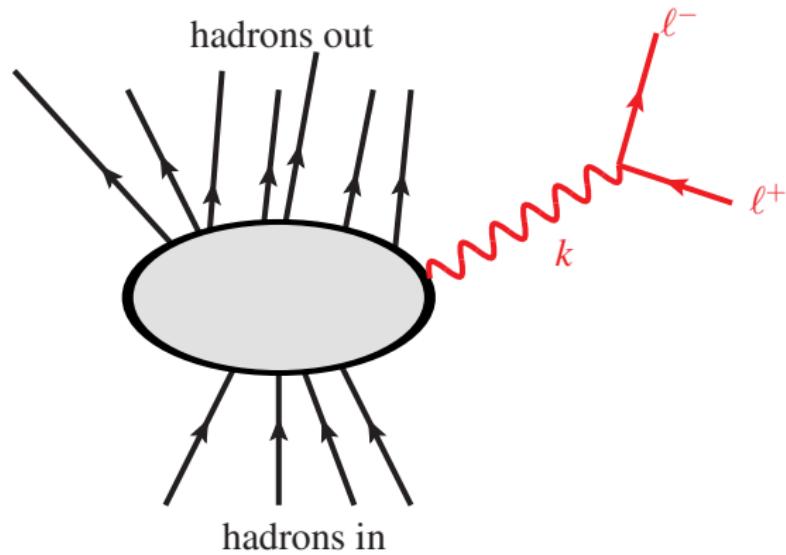
$$\frac{dR_{\ell^+\ell^-}}{d^4k} = \frac{dN_{\ell^+\ell^-}}{d^4x d^4k}$$

- radiation of **dileptons** from **thermalized strongly interacting particles** with total pair four-momentum k
- **dileptons** escape fireball without any final-state interactions
- calculation exact concerning **strong interactions**
- leading-order $\mathcal{O}(\alpha^2)$ in **QED**
- implies assumption that leptons don't suffer final-state interactions

$$H_{\text{em}}^{(\text{int})} = e \int d^3\vec{x} J_\mu(t, \vec{x}) A^\mu(t, \vec{x}), \quad A^\mu(t, \vec{x}) = \frac{\epsilon^\mu}{2\omega V} \exp(ik \cdot x)$$

- J_μ : exact (wrt. strong interaction!) em. current operator of quarks or hadrons in the Heisenberg picture wrt. strong interactions
- $e = \sqrt{4\pi\alpha}, \alpha \simeq 1/137$

The McLerran-Toimela formula



- Fermi's golden rule \Rightarrow transition-matrix element for process
 $|i\rangle \rightarrow |f'\rangle = |f\rangle + |\ell^+\ell^-(k)\rangle$
- QED Feynman rules

$$S_{f'i} = \left\langle f \left| \int d^4x J_\mu(x) \right| i \right\rangle D_\gamma^{\mu\nu}(x, x') e \bar{u}_\ell(x') \gamma_\nu v_\ell(x')$$

The McLerran-Toimela formula

- Fourier transformation: energy-momentum conservation $|f'\rangle = |f, \ell^+ \ell^-(k)\rangle$

$$S_{fi} = T_{fi} (2\pi)^4 \delta^{(4)}(P_f + k - P_i)$$

- Fermi's trick: Rate

$$R_{f'i} = \frac{|S_{f'i}|^2}{\tau V} = (2\pi)^4 \delta^{(4)}(P_f + k - P_i) |T_{f'i}|^2$$

- summing over $|f\rangle$ and polarizations of **dilepton states**
- averaging over initial hadron states: heat bath (grand canonical)

$$\rho = \frac{1}{Z} \exp[-\beta(H_{QCD} - \mu_B Q_{\text{baryon}})]$$

The McLerran-Toimela formula

- result (derivation see [GK91], Appendices)

$$\frac{dR_{\ell^+\ell^-}}{d^4k} = -\frac{\alpha^2}{3\pi^3} \frac{k^2 + 2m_\ell^2}{(k^2)^2} \sqrt{1 - \frac{4m_\ell^2}{k^2}} g_{\mu\nu} n_B(k^0) \text{Im} \Pi_{\text{ret}}^{\mu\nu}(k)$$

- em. current-current correlator

$$i\Pi_{\text{ret}}^{\mu\nu}(k) := \int d^4x \exp(ik \cdot x) \langle [J^\mu(x), J^\nu(0)] \rangle_{T,\mu_B} \Theta(x^0)$$

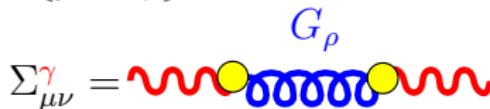
- written in (local) **restframe of the medium**
- in principle measurable: in **linear response approximation** Green's function for lepton current running through medium
- $k^2 = M^2 > 0$ **invariant mass of dilepton**
- probing medium with photons: **same correlator** for $k^2 = M^2 = 0$
- then correlator \Leftrightarrow dielectric function $\epsilon(\omega)$ in electrodynamics!

The McLerran-Toimela formula

- for **real photons**

$$\omega \frac{dR}{d^3\vec{k}} = -\frac{\alpha g_{\mu\nu}}{2\pi^2} \text{Im}\Pi_{\text{ret}}^{\mu\nu}(k) n_B(k^0), \quad k^0 \omega = |\vec{k}|$$

- written in (local) **restframe of the medium**
- Phenomenological **effective hadronic model**: **vector-meson dominance model**
- em. current $\propto V^\mu$ (with $V \in \{\rho, \omega, \phi\}$)



- Dilepton/photon rates: $\propto A_V = -2 \text{Im} D_V^{(\text{ret})}$
(**vector-meson spectral function!**)
- measuring **in-medium vector-meson spectral function!?**

Em. current-current correlator

Vector Mesons and electromagnetic Probes

- photon and dilepton thermal emission rates given by same electromagnetic-current-correlation function ($J_\mu = \sum_f Q_f \bar{\psi}_f \gamma_\mu \psi_f$)
- McLerran-Toimela formula

$$\Pi_{\mu\nu}^{<}(q) = \int d^4x \exp(iq \cdot x) \langle J_\mu(0) J_\nu(x) \rangle_T = -2n_B(q_0) \text{Im} \Pi_{\mu\nu}^{(\text{ret})}(q)$$

$$q_0 \frac{dN_\gamma}{d^4x d^3\vec{q}} = -\frac{\alpha_{\text{em}}}{2\pi^2} g^{\mu\nu} \text{Im} \Pi_{\mu\nu}^{(\text{ret})}(q, u) \Big|_{q_0=|\vec{q}|} f_B(p \cdot u)$$

$$\frac{dN_{e^+e^-}}{d^4x d^4k} = -g^{\mu\nu} \frac{\alpha^2}{3q^2\pi^3} \text{Im} \Pi_{\mu\nu}^{(\text{ret})}(q, u) \Big|_{q^2=M_{e^+e^-}^2} f_B(p \cdot u)$$

- manifestly Lorentz covariant (dependent on four-velocity of fluid cell, u)
- to lowest order in α : $4\pi\alpha \Pi_{\mu\nu} \simeq \Sigma_{\mu\nu}^{(\gamma)}$
- derivable from underlying thermodynamic potential, Ω !

Vector Mesons and chiral symmetry

- vector and axial-vector mesons \leftrightarrow respective current correlators

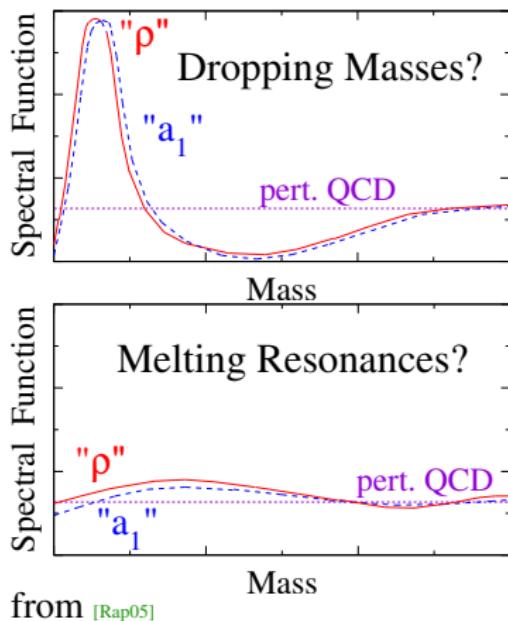
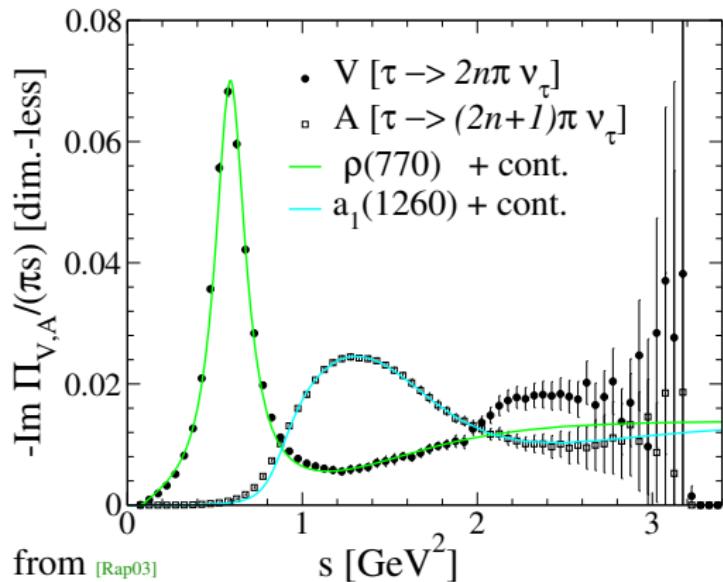
$$\Pi_{V/A}^{\mu\nu}(p) := \int d^4x \exp(ipx) \left\langle J_{V/A}^\nu(0) J_{V/A}^\mu(x) \right\rangle_{\text{ret}}$$

- Ward-Takahashi Identities of χ symmetry \Rightarrow Weinberg-sum rules

$$f_\pi^2 = - \int_0^\infty \frac{dp_0^2}{\pi p_0^2} [\text{Im } \Pi_V(p_0, 0) - \text{Im } \Pi_A(p_0, 0)]$$

- spectral functions of vector (e.g. ρ) and axial vector (e.g. a_1) directly related to order parameter of chiral symmetry!

Vector Mesons and chiral symmetry



- at high enough temperatures and or densities: melting of $\langle \bar{q}q \rangle$
- \Rightarrow spontaneous breaking of chiral symmetry suspended
- \Rightarrow chiral phase transition; chiral-symmetry restoration (χ SR)
- which scenario is right? microscopic mechanisms behind χ SR?

QCD Sum rules

- based on [LPM98]
- calculate current correlator, e.g., the vector part of the em. current

$$j_\mu = \frac{1}{2}(\bar{u}\gamma_\mu u - \bar{d}\gamma_\mu d)$$

- corresponds to the ρ meson!
- use pQCD to determine correlator

$$\Pi_{\mu\nu}(k) = \left(g_{\mu\nu} - \frac{k_\mu k_\nu}{k^2} \right) \Pi(k^2)$$

in deep spacelike region, $Q^2 = -k^2 \gg \Lambda_{\text{QCD}}$

- related to time-like region \Rightarrow sum rule

$$\Pi(k^2) = \Pi(0) + cQ^2 + \frac{Q^4}{\pi} \int_0^\infty ds \frac{\text{Im } \Pi(s)}{s^2(s+Q^2-i\epsilon)}$$

- dispersion relation: spectral function $\text{Im } \Pi$!

QCD Sum rules

- left-hand side of **sum rule**
- pQCD + chiral models for baryon-pion interactions [see, e.g., [DGH92]]

$$R(Q^2) := \frac{\Pi(k^2 = -Q^2)}{Q^2} = -\frac{1}{8\pi^2} \left(1 + \frac{\alpha_s}{\pi}\right) \ln\left(\frac{Q^2}{\mu^2}\right) + \frac{1}{Q^4} m_q \langle \bar{q}q \rangle + \frac{1}{24Q^4} \left\langle \frac{\alpha_s}{\pi} F_{\mu\nu}^a F^{a\mu\nu} \right\rangle - \frac{112}{81Q^6} \kappa \langle \bar{q}q \rangle^2$$

- additional cold-nuclear matter contributions

$$\Delta R(Q^2) = \frac{m_N}{4Q^4} A_2 \rho_N - \frac{5m_N^3}{12Q^6} A_4 \rho_N$$

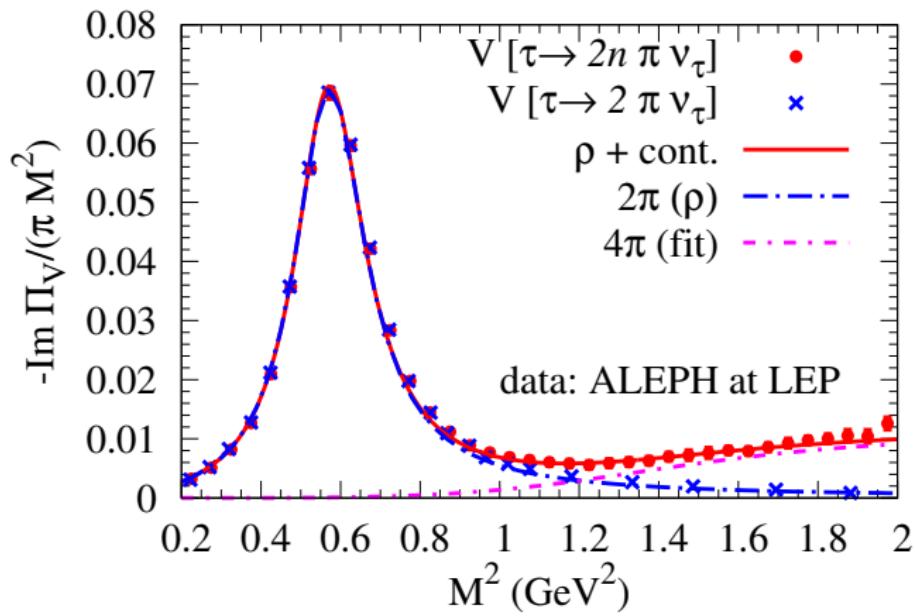
- $A_{2,4}$ from parton-distribution functions
- also condensates medium-modified (in low-density approximation)

$$\langle \bar{q}q \rangle = \langle \bar{q}q \rangle_{\text{vac}} + \frac{\sigma_N}{2m_q} \rho_N,$$

$$\left\langle \frac{\alpha_s}{\pi} F_{\mu\nu}^a F^{a\mu\nu} \right\rangle = \left\langle \frac{\alpha_s}{\pi} F_{\mu\nu}^a F^{a\mu\nu} \right\rangle_{\text{vac}} - \frac{8}{9} m_N^{(0)} \rho_N$$

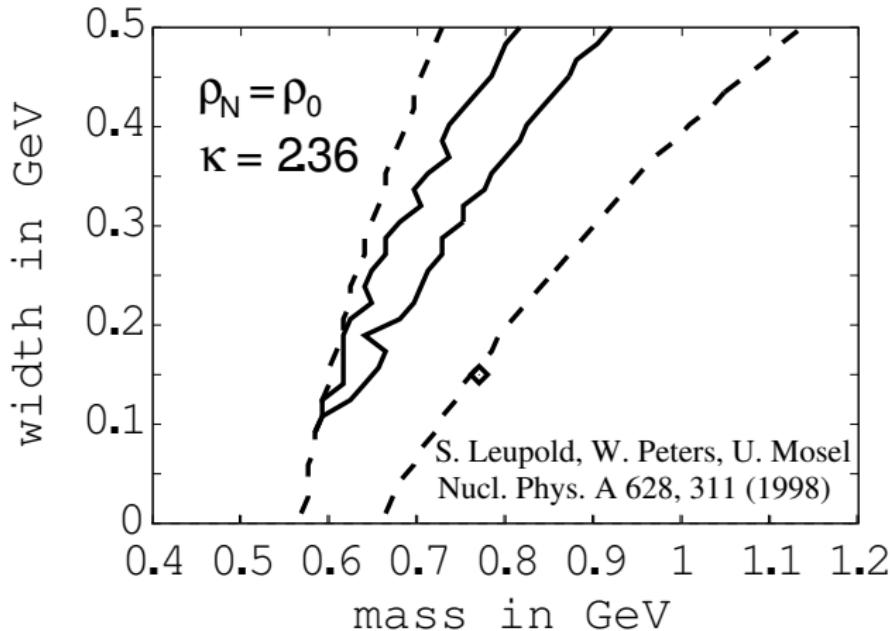
QCD Sum rules

- right-hand side of sum rule
- use hadronic models to fit measured vector-current correlator
- e.g., ALEPH/OPAL data of $\tau \rightarrow \nu + 2n\pi$



QCD Sum rules

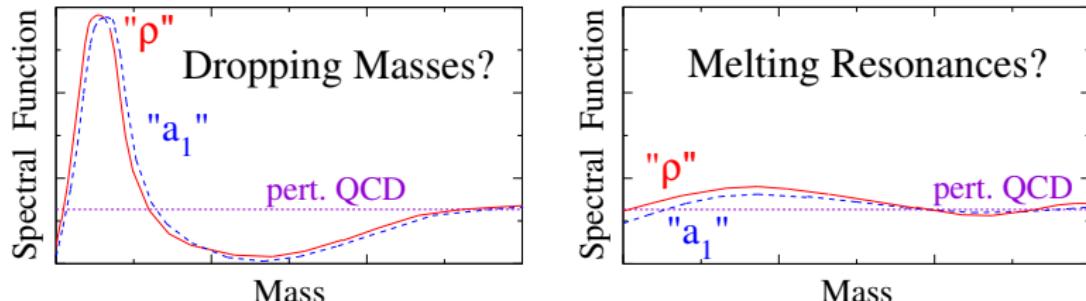
- typical result from [LPM98]



- possible medium effects on ρ meson
 - dropping mass, unchanged/small width
 - unchanged mass, broadened spectrum (large width)

Scenarios for chiral symmetry restoration

- hadron spectrum must become **degenerate** between chiral partners



- models alone of little help (realization of χ S not unique!)
 - “vector manifestation” $\rho_{\text{long}} = \chi$ partner of $\pi \Rightarrow$ dropping mass
 - “standard realization” $\rho = \chi$ partner of a_1 , extreme broadening + little mass shifts
- theory “shopping list”
 - effective hadronic models (well constrained in vacuum!)
 - and concise evaluation in the medium!**
 - models for **fireball evolution**
(blast-wave parametrizations, hydro, transport, and transport-hydro hybrids)
 - must include partonic \rightarrow phase transition \rightarrow hadronic evolution
- precise $\ell^+ \ell^- (\gamma)$ data from HICs mandatory!**

Hadronic models

Effective hadronic models: chiral-symmetry constraints

- different realizations of **chiral symmetry**
- equivalent only on shell (“**low-energy theorems**”)
- model-independent conclusions only in **low-temperature/density limit** (chiral perturbation theory) or from **lattice-QCD calculations**
- QCD sum rules: allow dropping-mass or melting-resonance scenario
- use **phenomenological hadronic many-body theory** (HMBT) to assess medium modifications of vector mesons
 - build models with **hadrons** as effective degrees of freedom
 - based on **(chiral) symmetries**
 - constrained by data on cross sections, branching ratios,... in the vacuum
 - in-medium properties assessed by **many-body (thermal) field theory**

Example: vector meson dominance model

- early model for **electromagnetic interaction** of charged pions [Sak60, KLZ67, GS68, Her92, Hee00]
- QED like U(1)-gauge model with massive vector meson for ρ_0 and π^\pm
- Stückelberg: introduce auxiliary scalar field for free vector mesons:

$$\mathcal{L}_\rho = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + \frac{1}{2}m^2V_\mu V^\mu + \frac{1}{2}(\partial_\mu\varphi)(\partial^\mu\varphi) + m\varphi\partial_\mu V^\mu$$

- gauge invariant under local transformation

$$\delta V_\mu(x) = \partial_\mu\chi(x), \quad \delta\varphi = m\chi(x)$$

- Coupling to pions: **obey gauge invariance!** (like scalar QED)

$$\mathcal{L}_\pi = (D_\mu\pi)^*(D^\mu\pi) - m_\pi^2|\pi|^2 - \frac{\lambda}{8}|\pi|^4$$

- $D_\mu = \partial_\mu + igV_\mu$; g : $\rho\pi\pi$ coupling

VMD model (photon part)

- add photons: $D_\mu = \partial_\mu + igV_\mu + ieA_\mu$
- Lagrangian for photons: usual (gauge fixed) QED
- additional direct $\rho\gamma$ mixing [KLZ67]

$$\mathcal{L}_{\rho\gamma} = -\frac{e}{2g_{\rho\gamma}} V_{\mu\nu} A^{\mu\nu}$$

- classical field equations: \Rightarrow **electromagnetic current**

$$j_{\text{em}}^\nu = \partial_\mu A^{\mu\nu} = ie \left(1 - \frac{g}{g_{\rho\gamma}} \right) \pi \overleftrightarrow{D}^\nu \pi^* + \frac{e}{g_{\rho\gamma}} m^2 V^\nu + \frac{e^2}{g_{\rho\gamma}^2} \partial_\mu A^{\mu\nu}$$

- for $g_{\rho\gamma} = g$: $j_{\text{em}}^\nu = \frac{e}{g} m^2 V^\nu + \mathcal{O}(e^2)$: \Rightarrow **“vector-meson dominance”**

VMD model (Feynman rules in Feynman gauge)

$\mu \nu$

 $= -i \frac{\eta^{\mu\nu}}{p^2 - M^2 + i0^+}$

$\mu \nu$

 $= -i \frac{\eta^{\mu\nu}}{k^2 + i0^+},$

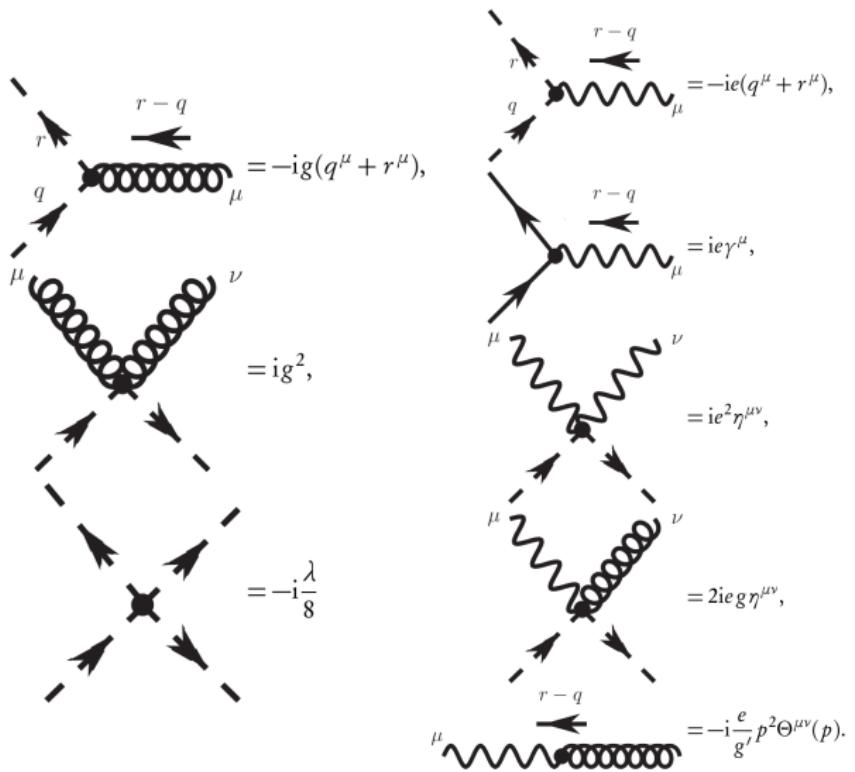
$\mu \nu$

 $= \frac{i}{p^2 - m_\pi^2 + i0^+},$

$\mu \nu$

 $= i \frac{\not{p} + m_c}{p^2 - m_c^2 + i0^+},$

- $\eta^{\mu\nu} =$
 $\text{diag}(1, -1, -1, -1)$
- $\Theta^{\mu\nu}(p) =$
 $\eta^{\mu\nu} - p^\mu p^\nu / p \cdot p$



VMD model (ρ -self-energy and dressed $\gamma\pi\pi$ vertex)

- calculate **ρ -self-energy** (transversality from gauge invariance)

$$i\Pi_{\rho\pi\pi}^{\mu\nu}(p) = \text{Diagram with two wavy lines and a loop, labeled } \mu, l, \nu, l+p = i s \Pi_{\rho\pi\pi}(s) \Theta^{\mu\nu}(p), \quad s = p^2$$

$$i\Pi_{\rho ee}^{\mu\nu}(p) = \text{Diagram with two wavy lines and a loop, labeled } \mu, l, \nu, l+p = i s \Pi_{\rho ee}(s) \Theta^{\mu\nu}(p), \quad s = p^2$$

- Dressed Green's function

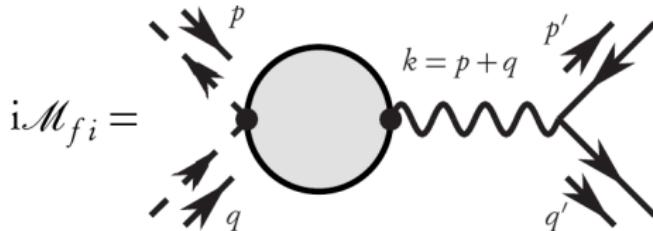
$$G_{\rho}^{\mu\nu}(p) = -\frac{\Theta^{\mu\nu}(p)}{p^2 - M^2 - p^2 \Pi_{\rho\pi\pi}(p^2)} - \frac{\Lambda^{\mu\nu}(p)}{p^2 - M^2 + i0^+}$$

- dressed $\gamma\pi\pi$ vertex to $\mathcal{O}(e)$

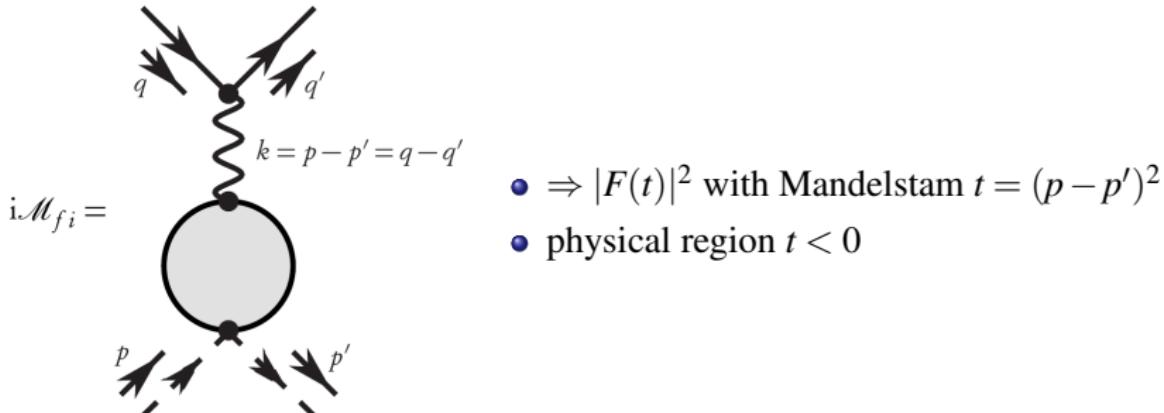
$$i\Pi_{\gamma\pi\pi}^{\mu} = \text{Diagram with one wavy line and one dashed line, labeled } r, q, \mu + \text{Diagram with one wavy line and one dashed line, labeled } r, q, \mu + \text{Diagram with three wavy lines and a loop, labeled } r, q, \mu$$

VMD model (em. form factor of the π)

- $\pi^+ + \pi^- \rightarrow e^+ + e^-$ (“time-like form factor”)

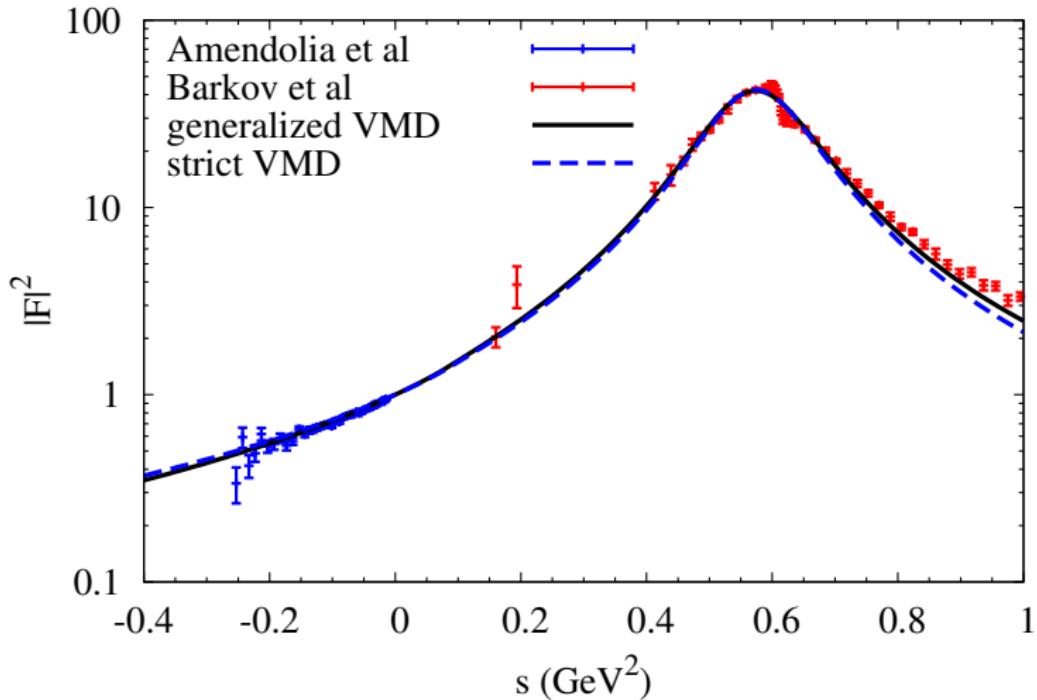


- $\Rightarrow |F(s)|^2$ with Mandelstam $s = (p + q)^2$
- physical region $s > 4m_\pi^2$
- $\pi^+ + e^- \rightarrow \pi^+ + e^-$ (“space-like form factor”)



VMD model: (fit of parameters)

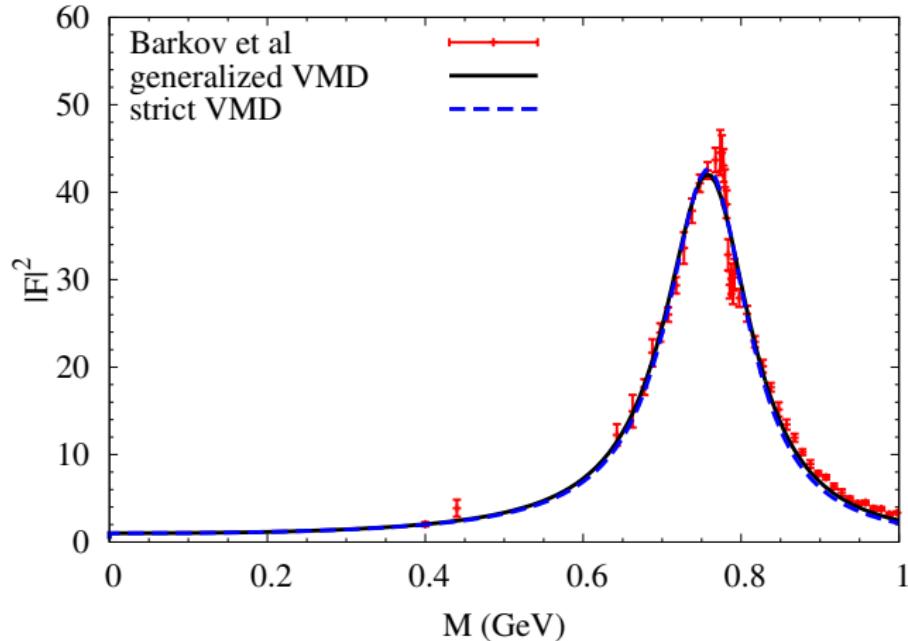
- best fit to form-factor data: $g = 5.461$, $g' = 5.233$, $m_\rho = 763.1 \text{ MeV}/c^2$
strict VMD: $\frac{1}{2}g' = 5.328$, $m_\rho = 763.1 \text{ MeV}/c^2$



data from [A⁺ 86, BCE⁺ 85]

VMD model: (fit of parameters)

- best fit to form-factor data: $g = 5.461$, $g' = 5.233$, $m_\rho = 763.1 \text{ MeV}/c^2$
strict VMD: $g = g' = 5.328$, $m_\rho = 763.1 \text{ MeV}/c^2$



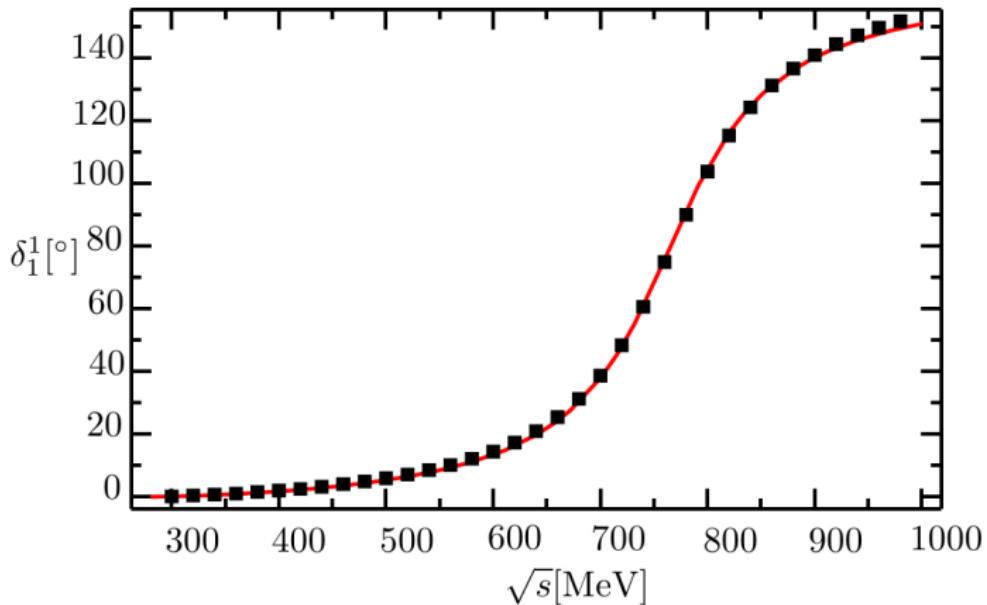
data from [BCE⁺85]

- small discrepancies around ρ peak: contribution from $\omega(782)$ meson!

VMD (elastic $\pi\pi$ phase shift)

- $\pi\pi \rightarrow \pi\pi$ phase shift in $I = 1$ channel

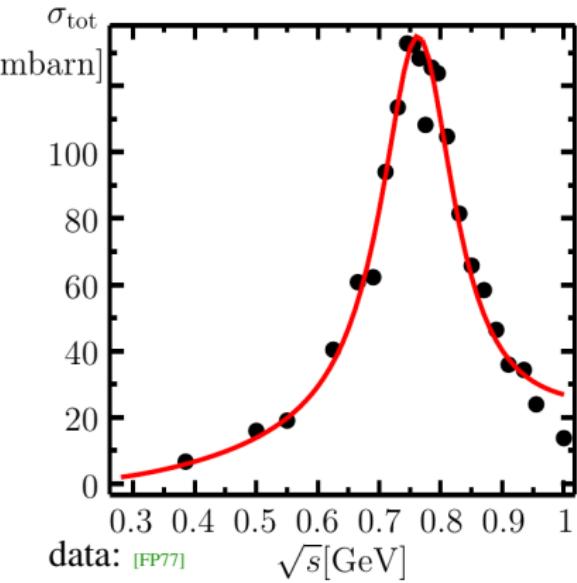
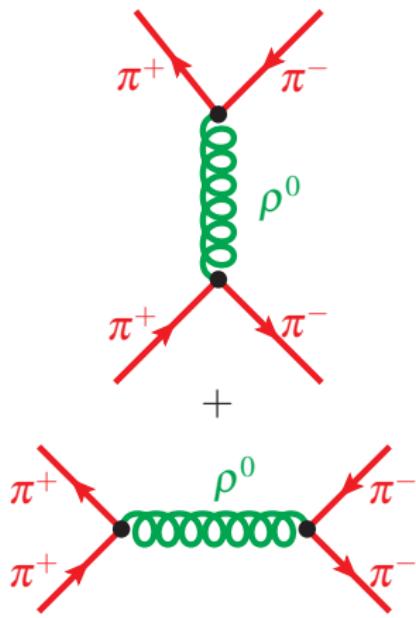
$$\delta_1^1 = \arccos \frac{\operatorname{Re} G_\rho}{|G_\rho|}$$



data: [FP77]

VMD: (total $\pi\pi$ elastic scattering cross section)

- $\pi\pi \rightarrow \pi\pi$ total cross section

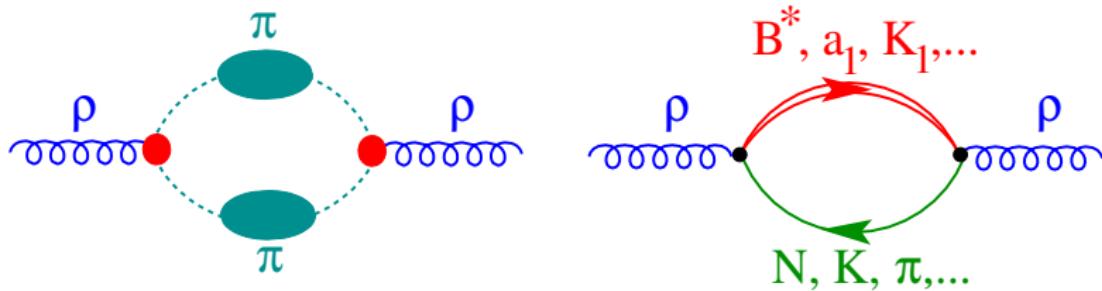


Realistic hadronic models for light vector mesons

- CERES data: pion- ρ model too simplistic
- many approaches to more realistic models
 - gauged linear σ -model + vector-meson dominance [Pis95, UBW02]
gauge-symmetry breaking \Rightarrow pions still in physical spectrum!
 - massive Yang-Mills model; gauged non-linear chiral model with explicitly broken gauge symmetry [Mei88, LSY95]
 - hidden local symmetry: Higgs-like chiral model [BK84, HY03, HY03]
allows for vector manifestation or usual manifestation (with a_1)
- here we concentrate on the phenomenological model by Rapp, Wambach, et al [RW99]

Hadronic many-body theory

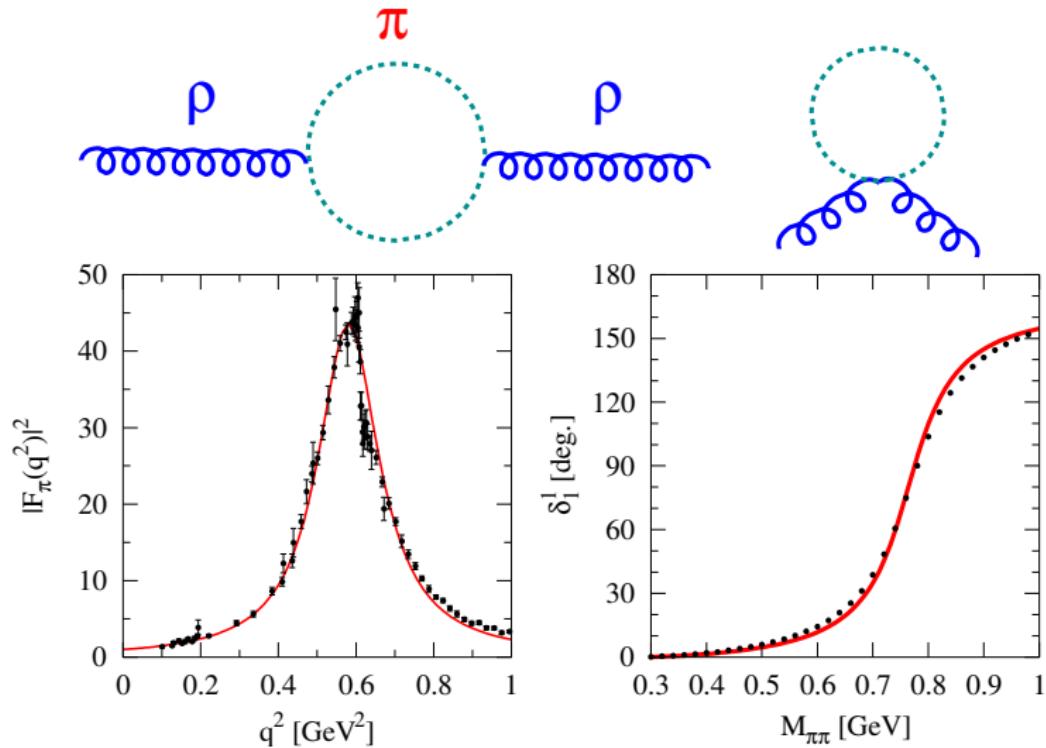
- Phenomenological HMBT [RW99] for vector mesons
- $\pi\pi$ interactions and baryonic excitations



- Baryon (resonances) important, even at RHIC with low **net** baryon density
 $n_B - n_{\bar{B}}$
- reason: $n_B + n_{\bar{B}}$ relevant (CP inv. of strong interactions)

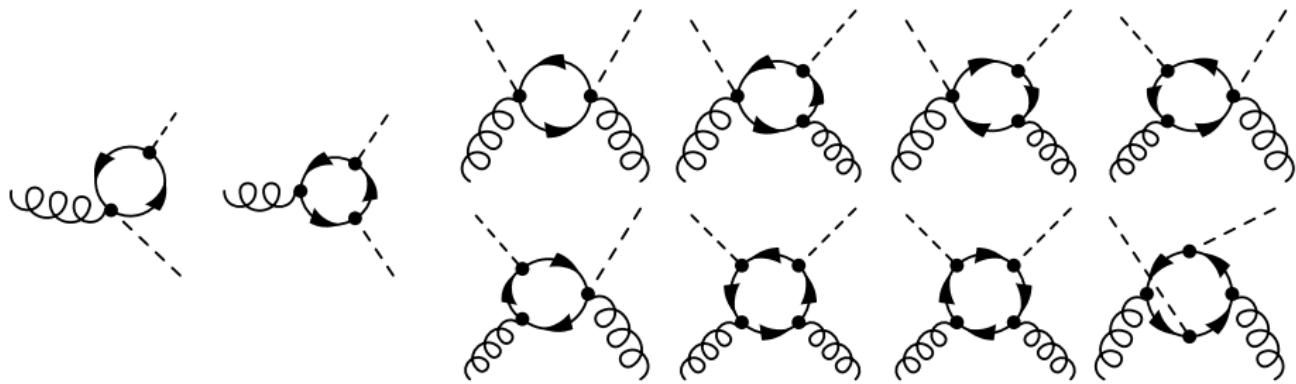
The meson sector (vacuum)

- most important for ρ -meson: pions

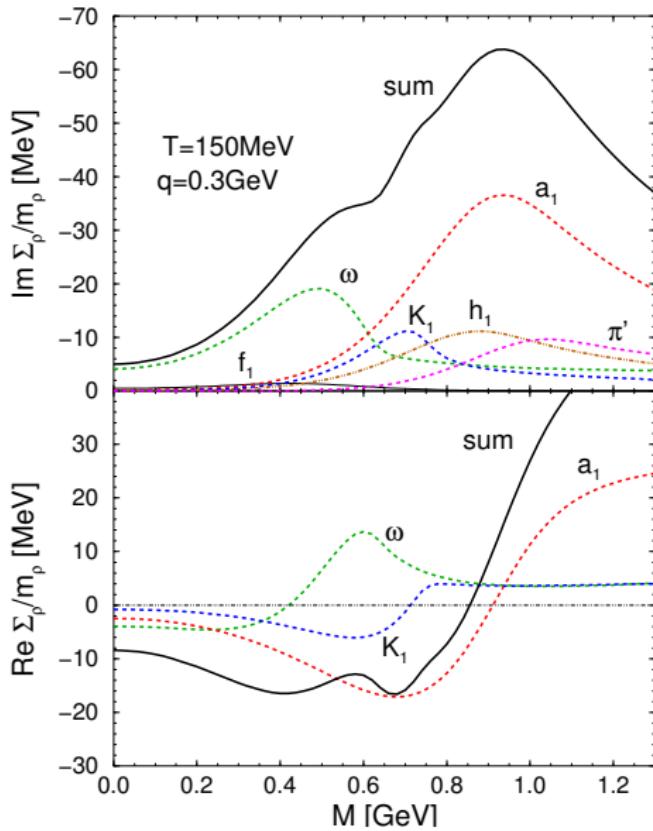


The meson sector (matter)

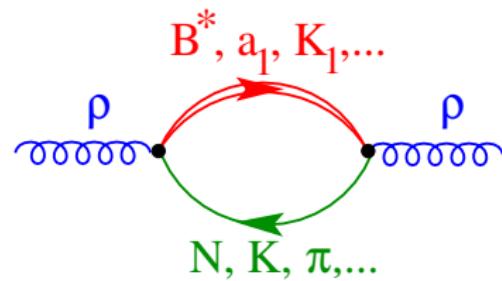
- Pions dressed with **N-hole-, Δ -hole** bubbles
- Ward-Takahashi \Rightarrow **vertex corrections** mandatory!



The meson sector (contributions from higher resonances)

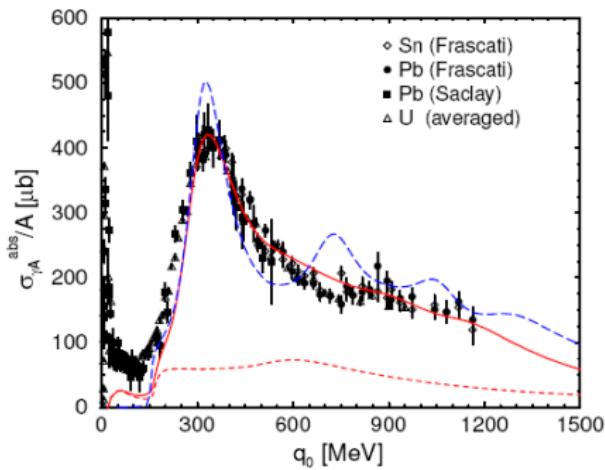
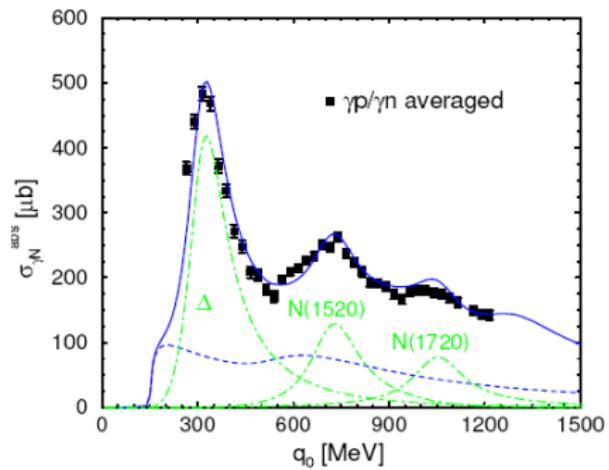


The baryon sector (vacuum)

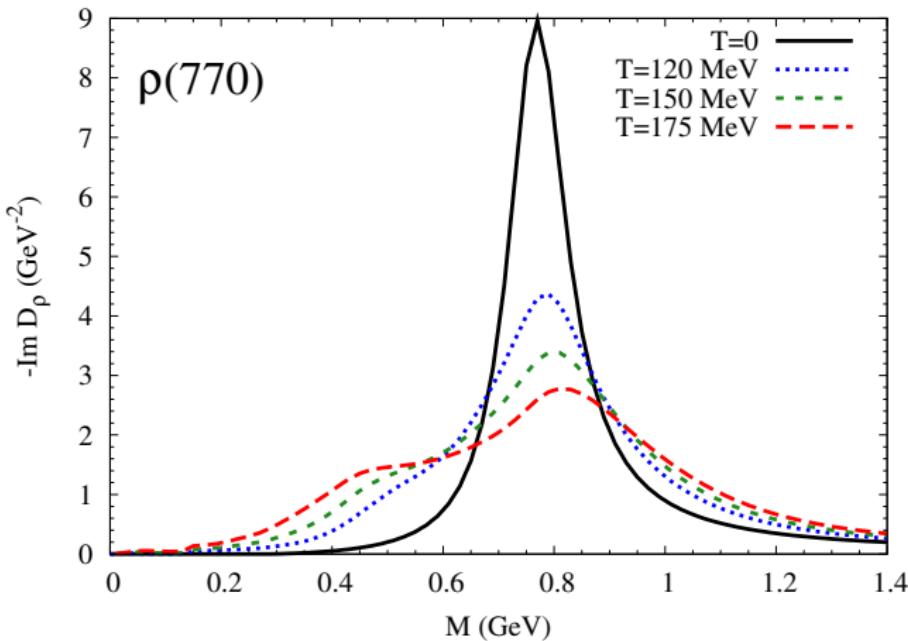


- $P = 1$ -baryons: p -wave coupling to ρ :
 $N(939), \Delta(1232), N(1720), \Delta(1905)$
- $P = -1$ -baryons: s -wave coupling to ρ :
 $N(1520), \Delta(1620), \Delta(1700)$

Photoabsorption on nucleons and nuclei



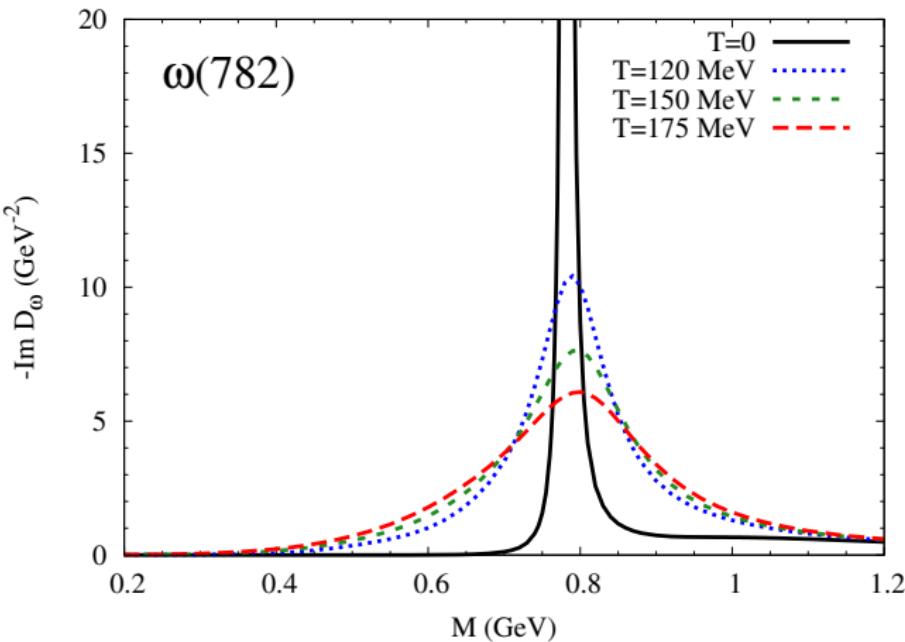
In-medium spectral functions and baryon effects



[R. Rapp, J. Wambach 99]

- baryon effects important
 - large contribution to broadening of the peak
 - responsible for most of the strength at small M

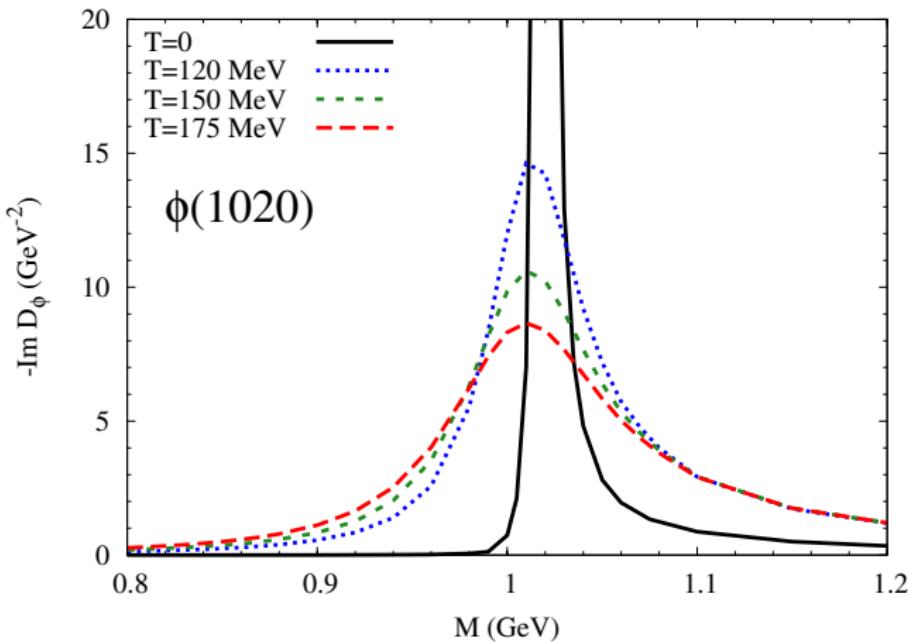
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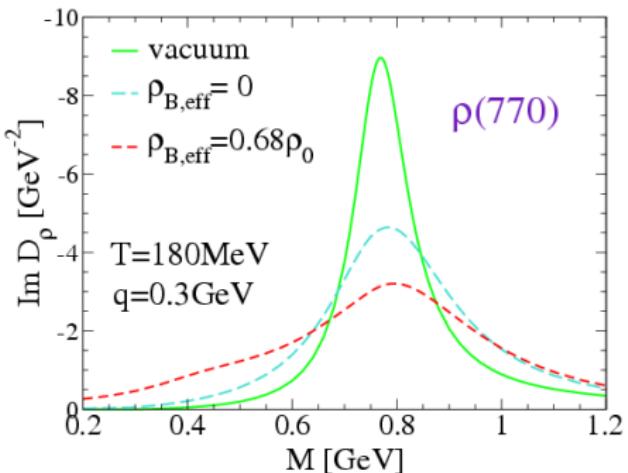
In-medium spectral functions and baryon effects



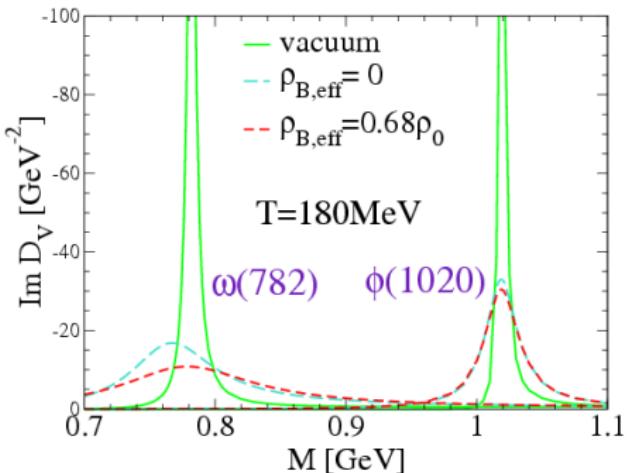
[R. Rapp, J. Wambach 99]

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In-medium spectral functions and baryon effects

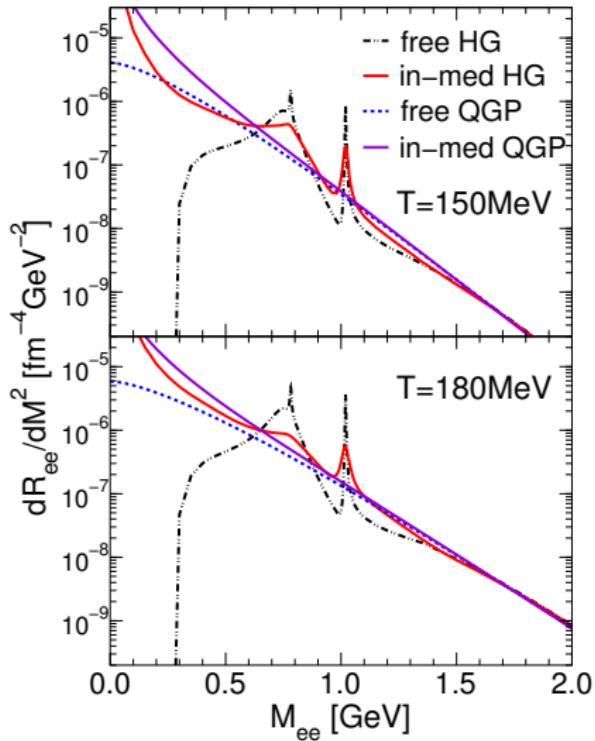


[R. Rapp, J. Wambach 99]



- baryon effects important
 - large contribution to broadening of the peak
 - responsible for most of the strength at small M

Dilepton rates: Hadron gas \leftrightarrow QGP



- in-medium hadron gas matches with QGP
- similar results also for γ rates
- “quark-hadron duality”?
- hidden local symm.+baryons?

[BK84, HY03, Sas05, HS06]

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Quiz

Quiz

- ➊ in the QCD phase diagram some points labeled “Heavy-Ion Experiments” are shown. How are those points “measured” or determined?
- ➋ what indicates that there is a collective fluid-like behavior of the hot and dense medium created in HICs?
- ➌ how do we explain the elliptic flow, v_2 , of hadrons in HICs?
- ➍ why do we believe that the QGP is really created in HICs and why do we think it's the most perfect fluid ever observed?
- ➎ which important “theoretical quantity” can be measured by observing electromagnetic probes in HICs (and elementary reactions)?
- ➏ what is chiral-symmetry restoration and in which ways could it be realized in nature?
- ➐ what can we learn from QCD sum rules about χ SR?
- ➑ what tell effective hadronic models about the medium modification of light vector mesons and the related χ SR?
- ➒ what's basic assumption of the vector-meson dominance (VMD) model?
- ➓ why is the simple $\pi\rho$ model insufficient to explain the dilepton data in HICs?
- ➔ why are baryon-vector-meson interactions important even at high collision energies, where $\mu_B \simeq 0$ (nearly 0 net-baryon density)?