

# in the Context of the Hadron-Quark Phase Transition

*ADVANCES IN ASTROPARTICLE PHYSICS AND COSMOLOGY*  
*ON THE OCCASION OF THE 125TH BIRTH ANNIVERSARY OF PROF. MEGHNAD SAHA*

*SAHA INSTITUTE, KOLKATA, INDIA, 09. MARCH 2018*

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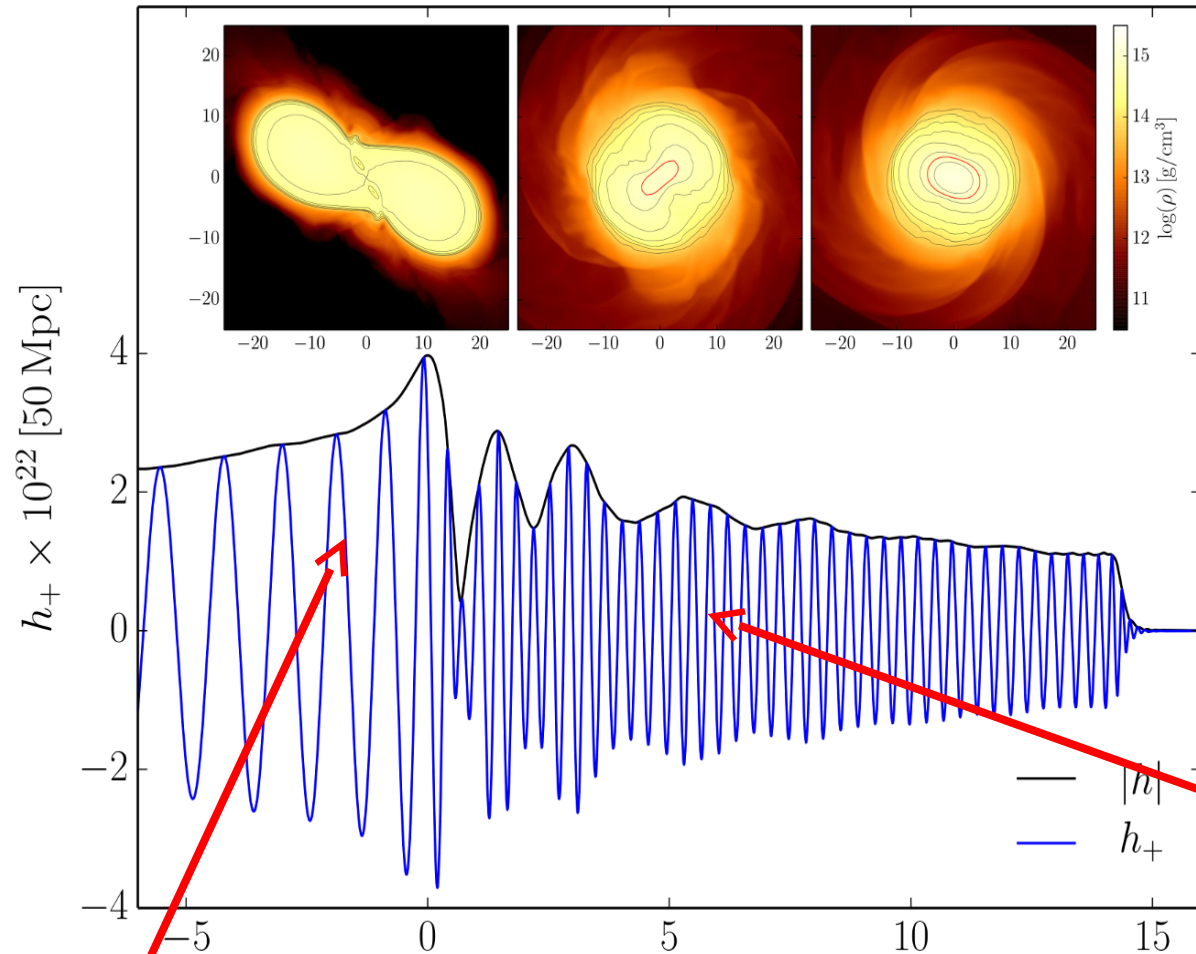
# The long-awaited event

## GW170817

	Low-spin priors ( $ \chi  \leq 0.05$ )	High-spin
Primary mass $m_1$	1.36–1.60 $M_\odot$	1
Secondary mass $m_2$	1.17–1.36 $M_\odot$	0
Chirp mass $\mathcal{M}$	$1.188^{+0.004}_{-0.002} M_\odot$	1
Mass ratio $m_2/m_1$	0.7–1.0	
Total mass $m_{\text{tot}}$	$2.74^{+0.04}_{-0.01} M_\odot$	
Radiated energy $E_{\text{rad}}$	$> 0.025 M_\odot c^2$	$>$
Luminosity distance $D_L$	$40^{+8}_{-14}$ Mpc	
Viewing angle $\Theta$	$\leq 55^\circ$	
Using NGC 4993 location	$\leq 28^\circ$	
Combined dimensionless tidal deformability $\tilde{\Lambda}$	$\leq 800$	
Dimensionless tidal deformability $\Lambda(1.4M_\odot)$	$\leq 800$	

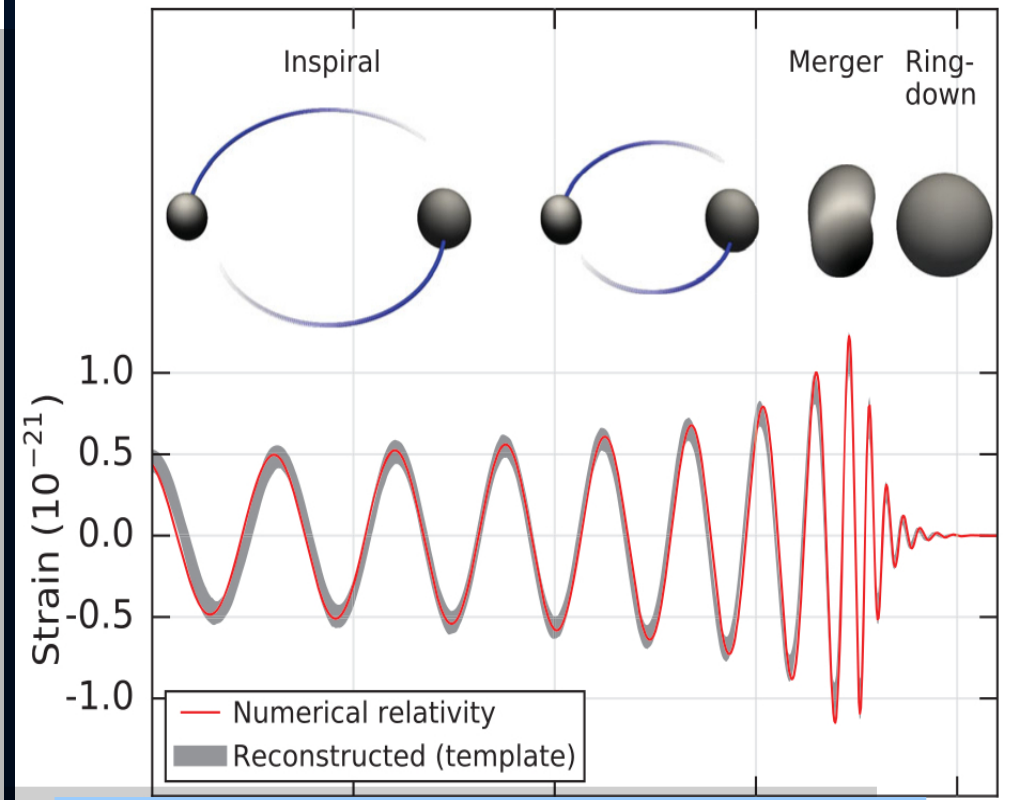
# Gravitational Waves from Neutron Star Mergers

## Neutron Star Collision (Simulation)



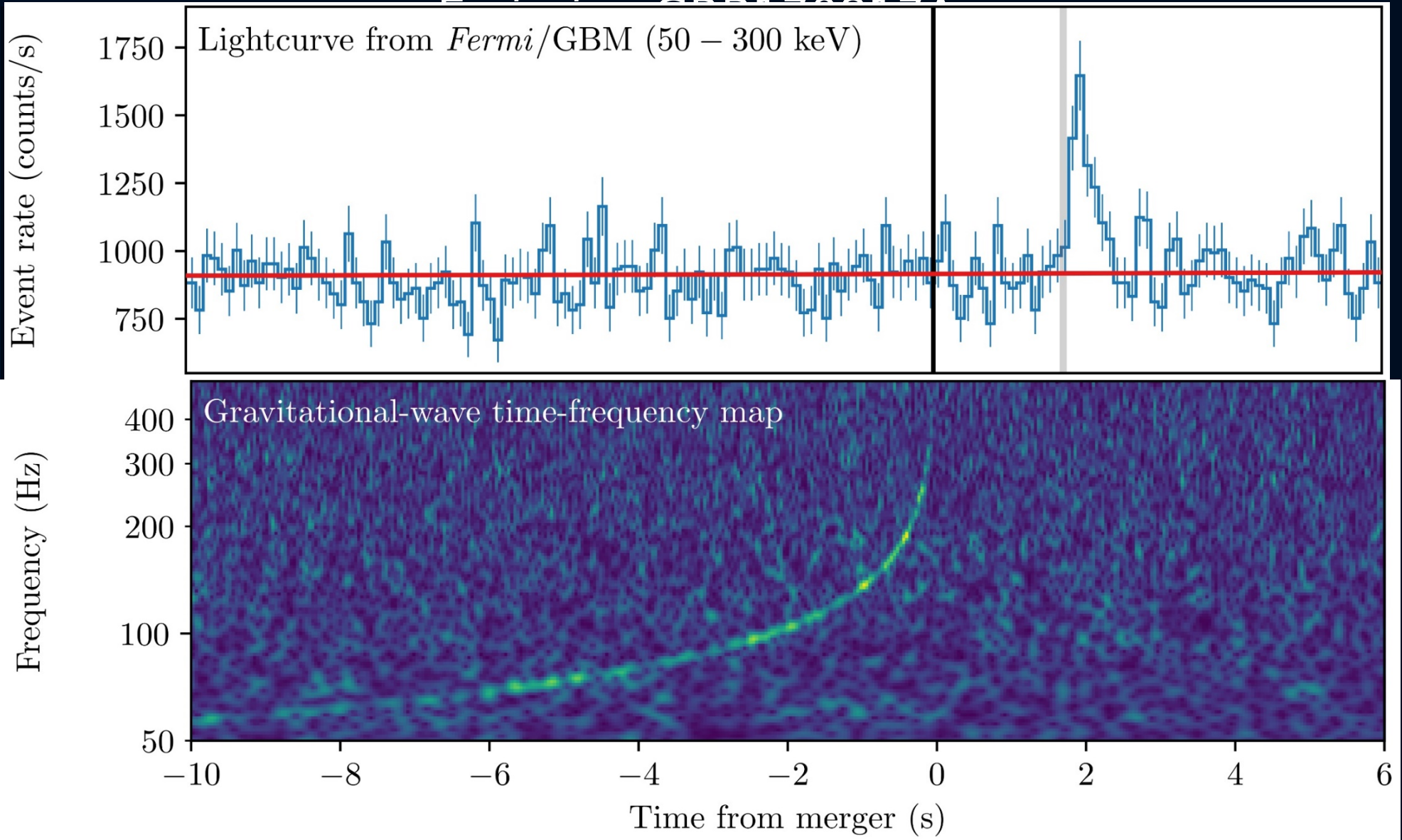
Difference due to tidal deformation in the late Inspiral phase

## Collision of two Black Holes GW150914



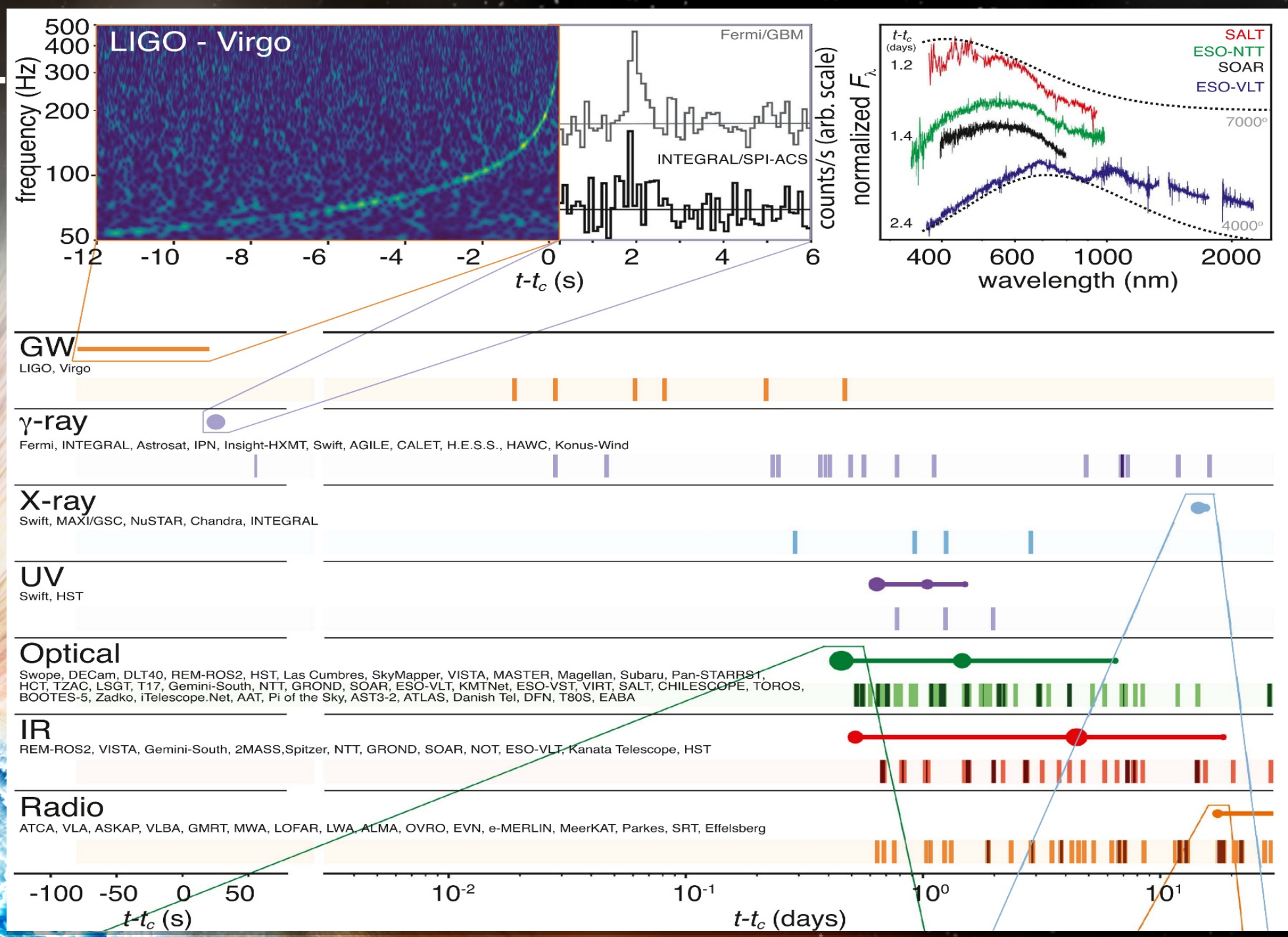
Main difference:  
In binary neutron star mergers a **Post-Merger Phase** often exists

# Gravitational Wave GW170817 and Gamma-Ray



# GW170817

Multi-Messenger Observations of a Binary Neutron Star Merger, LIGO and Virgo Collaborations together with 50 teams of electromagnetic and neutrino astronomers, *Astrophys. J. Lett.* 848, L12 (2017)



# Numerical Relativity and Relativistic Hydrodynamics of Binary Neutron Star Mergers

Numerical simulations of a merger of two compact objects are based on a (3+1) decomposition of spacetime of Einstein and hydrodynamic equations.

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu}$$

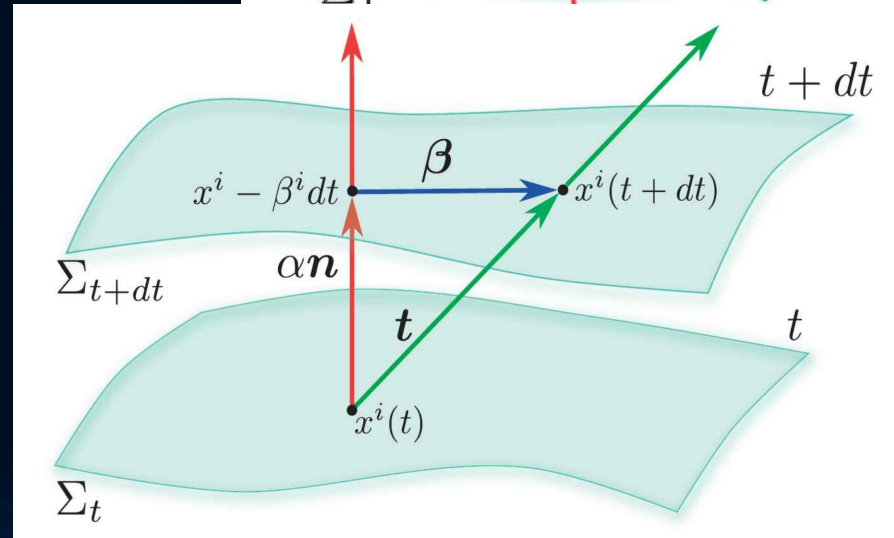
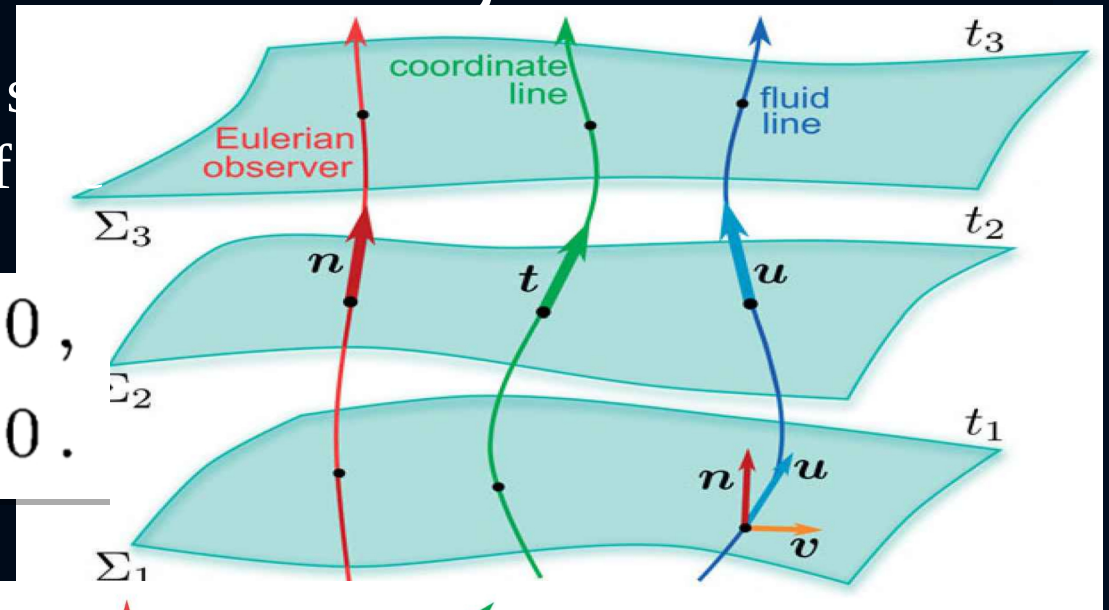
$$\begin{aligned} \nabla_{\mu}(\rho u^{\mu}) &= 0, \\ \nabla_{\nu}T^{\mu\nu} &= 0. \end{aligned}$$

(3+1) decomposition of spacetime

$$g_{\mu\nu} = \begin{pmatrix} -\alpha^2 + \beta_i\beta^i & \beta_i \\ \beta_i & \gamma_{ij} \end{pmatrix}$$

$$d\tau^2 = \alpha^2(t, x^j)dt^2$$

$$x^i_{t+dt} = x^i_t - \beta^i(t, x^j)dt$$



# *Computersimulation of a Neutron Star Merger in full General Relativity*

**Credits: Cosima Breu, David Radice  
and Luciano Rezzolla**



**Density**

8.5 14



$\lg(\rho)$  [g/cm<sup>3</sup>]

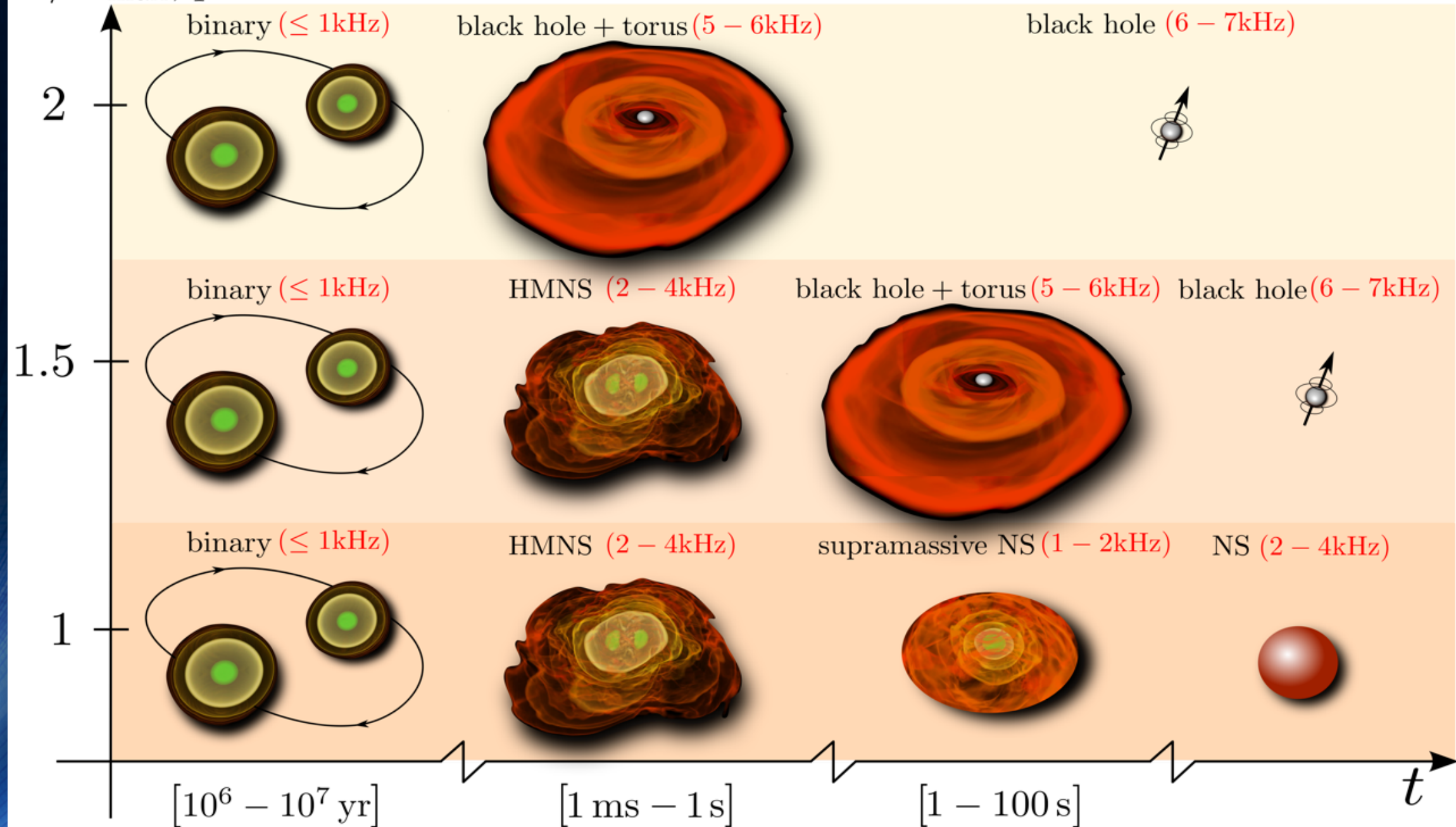
**Temperature**

0 50



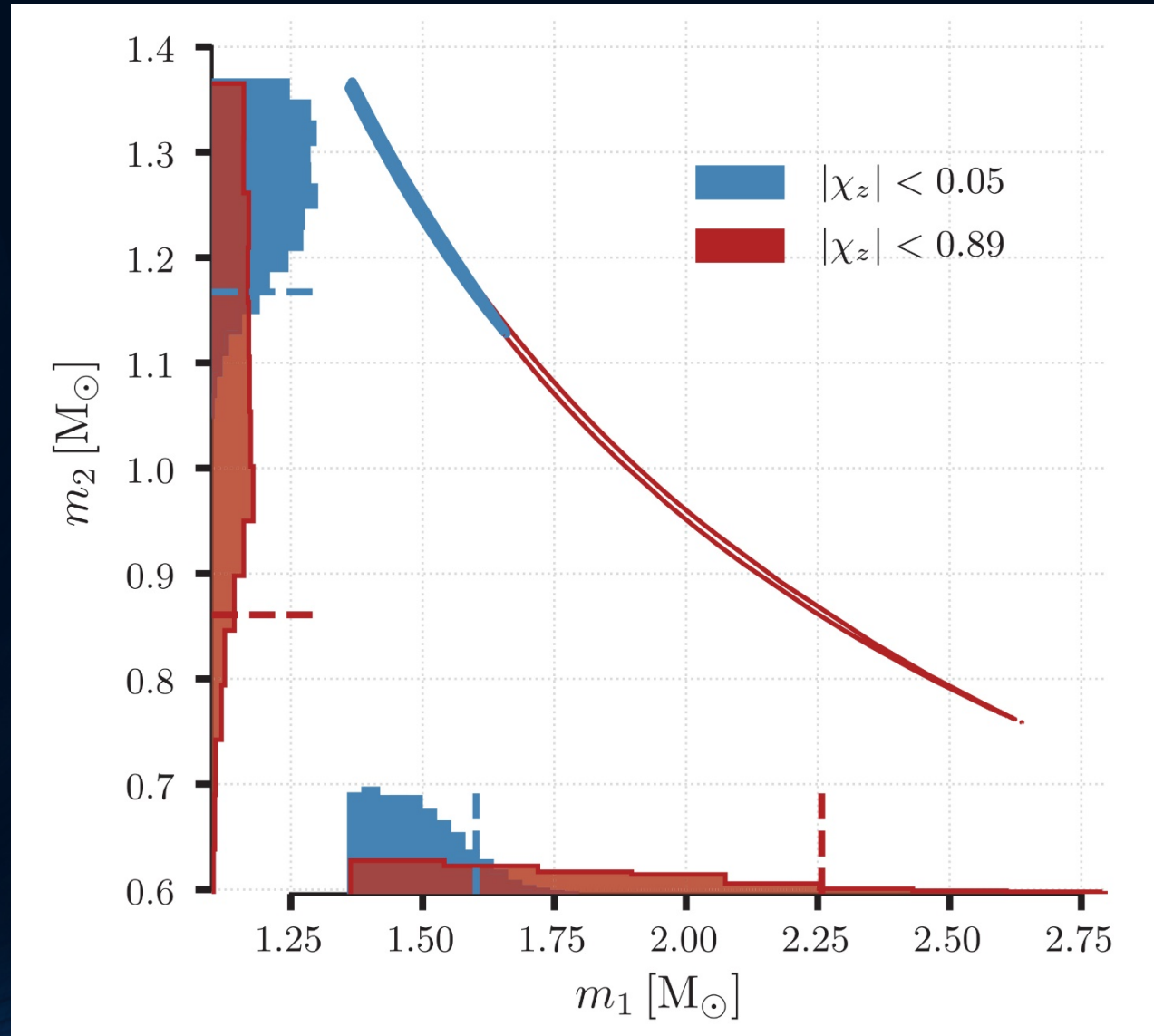
T [MeV]

$M/M_{\max}, q \simeq 1$





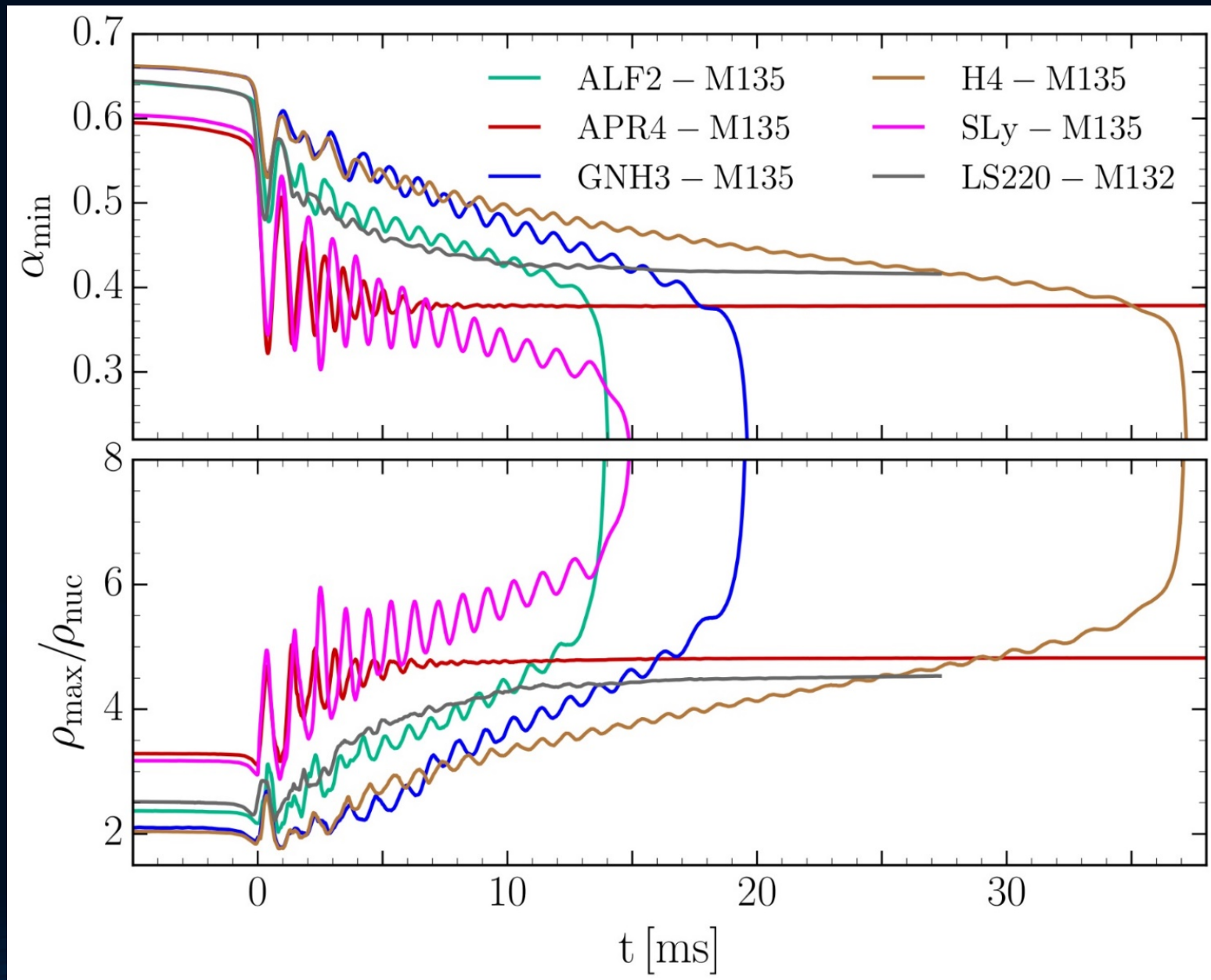
# Measured Mass Ratio of GW170817 (for high and low spin assumption)



# Binary Merger of two Neutron Stars for different EoSs

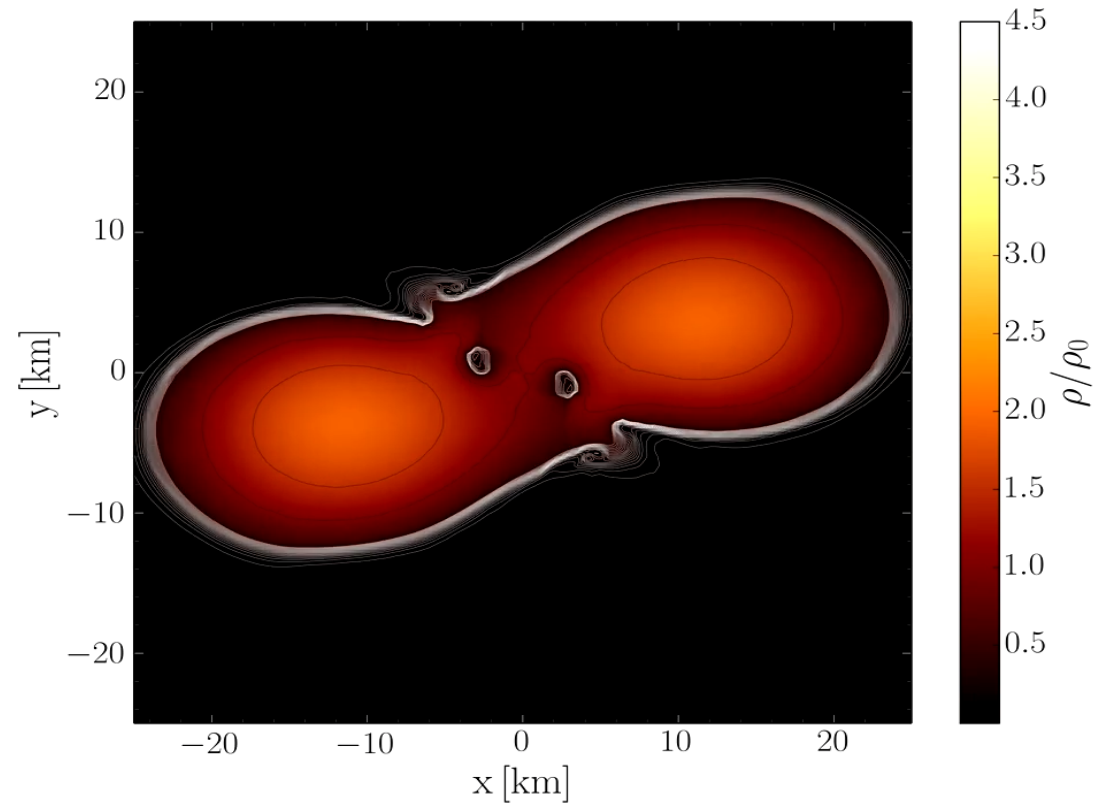
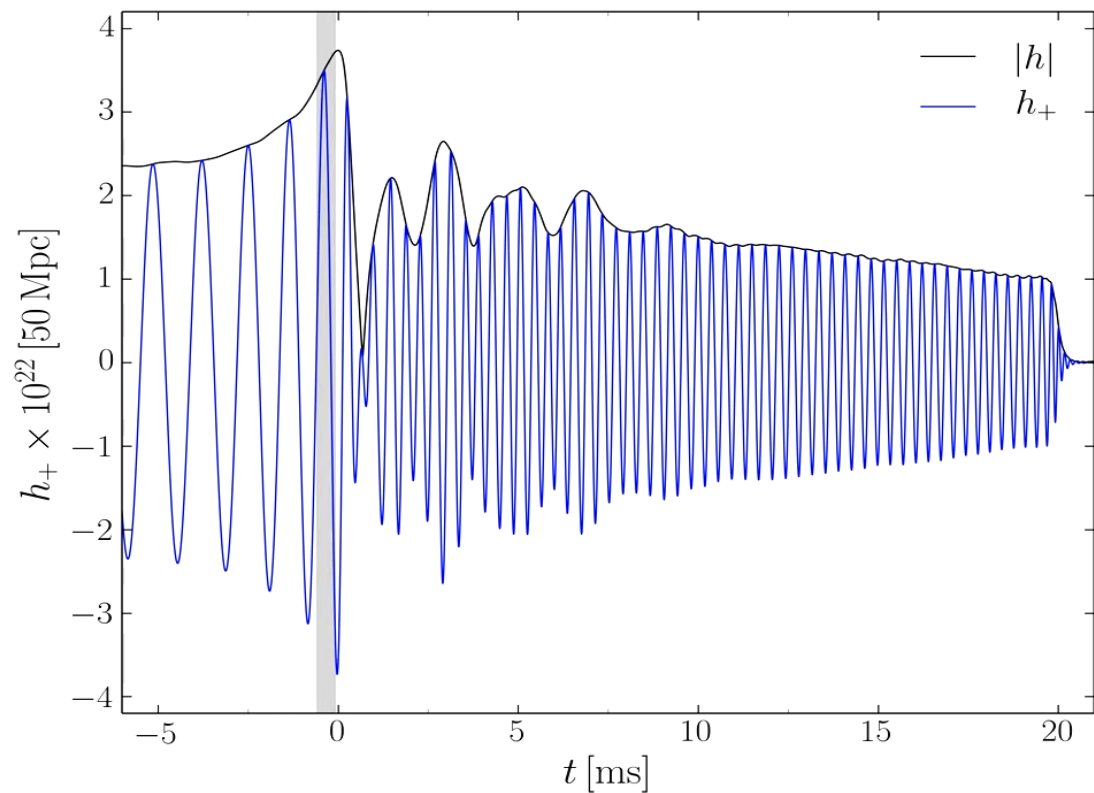
$M=1.35 M_{\text{solar}}$   
for details see Hanauske, et.al.  
PRD, 96(4), 043004 (2017)

Central value of the lapse function  $\alpha_c$  (upper panel) and maximum of the rest mass density  $\rho_{\text{max}}$  in units of  $\rho_0$  (lower panel) versus time for the high mass simulations.



# Evolution of the density in the post-merger phase

GNH3-EOS, initial NS mass:  $1.35 M_{\text{solar}}$

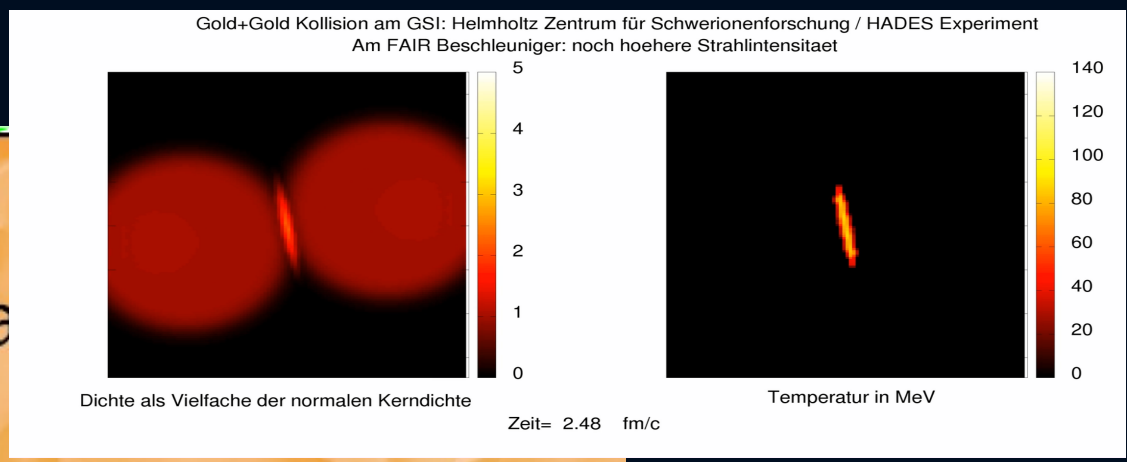
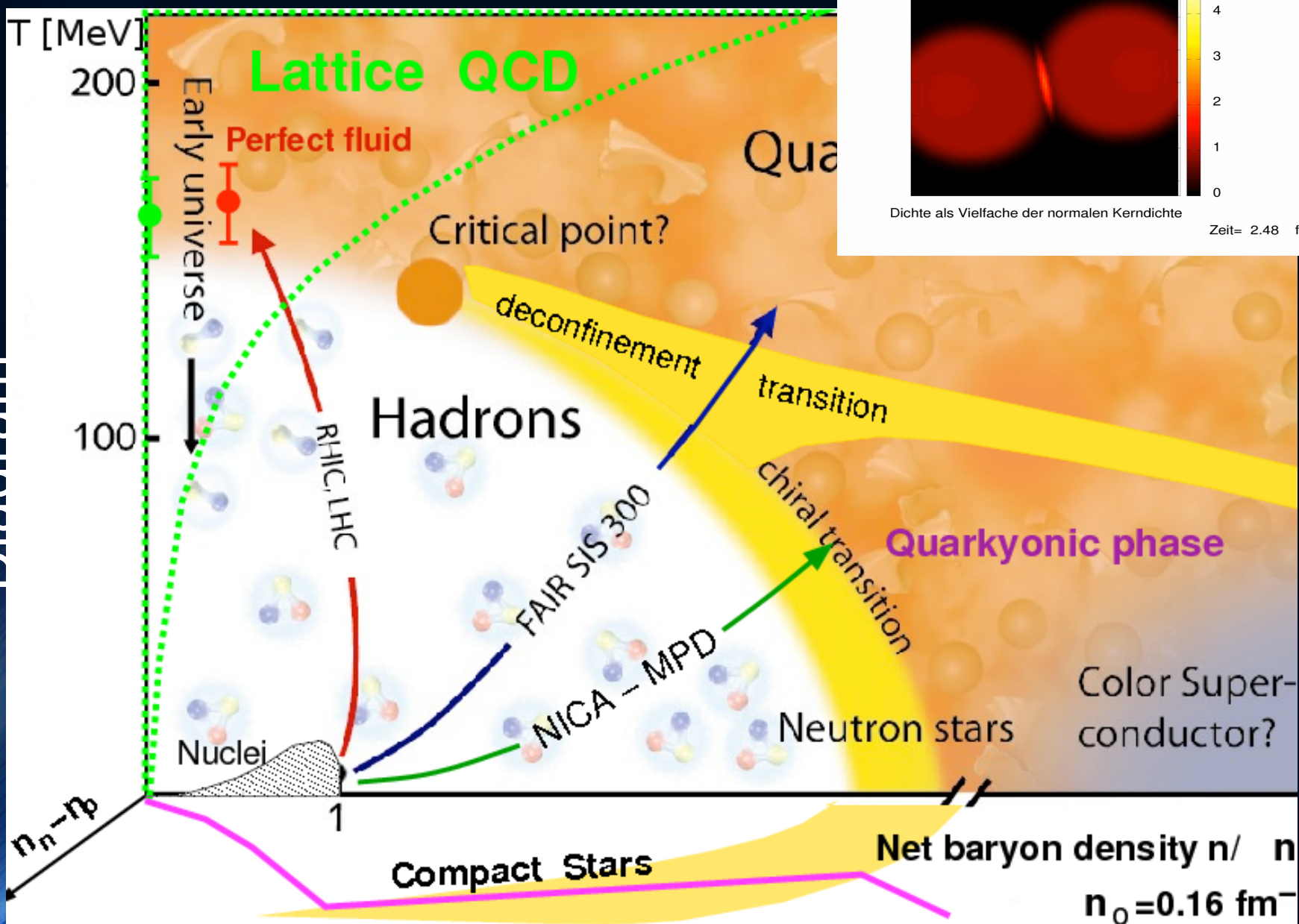


Gravitational wave amplitude  
at a distance of 50 Mpc

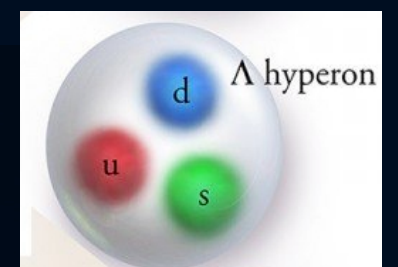
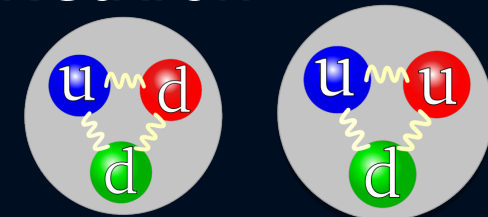
Rest mass density distribution  $\rho(x,y)$  in the equatorial plane  
in units of the nuclear matter density  $\rho_0$

# The Hadron-Quark Phase Transition

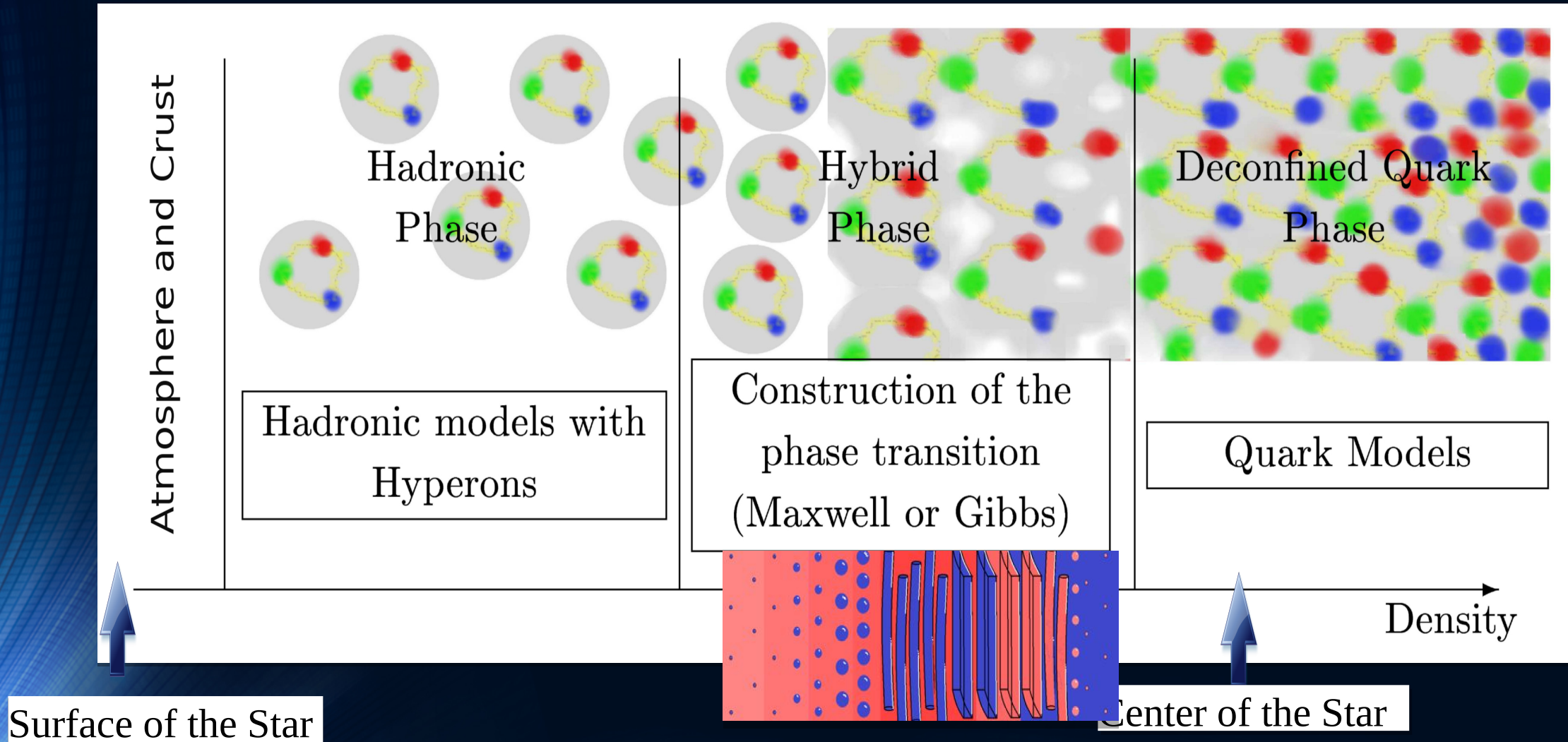
The QCD Phase Diagram



Credits:  
Jan Steinheimer  
Neutron Proton



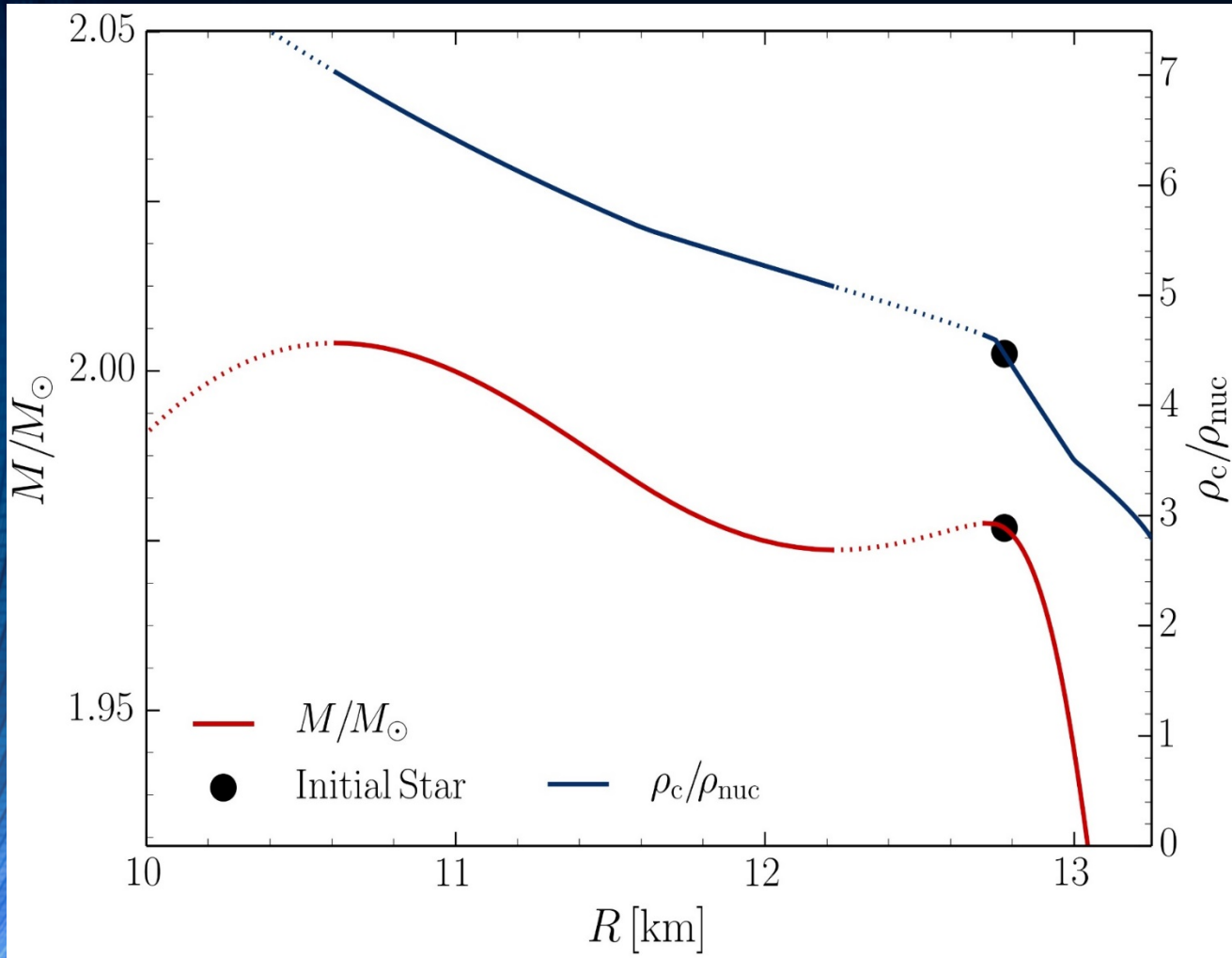
# The QCD - Phase Transition and the Interior of a Hybrid Star



Matthias Hanauske; Doctoral Thesis:

*Properties of Compact Stars within QCD-motivated Models; University Library Publication Frankfurt (2004)*

## The Hadron-Quark Phase Transition and the Third Family of Compact Stars (Twin Stars)



Sarmistha Banik, Matthias Hanauske, Debades Bandyopadhyay and Walter Greiner, Rotating compact stars with exotic matter, Phys.Rev.D 70 (2004) p.12304

I.N. Mishustin, M. Hanauske, A. Bhattacharyya, L.M. Satarov, H. Stöcker, and W. Greiner, Catastrophic rearrangement of a compact star due to quark core formation, Physics Letters B 552 (2003) p.1-8

M.Alford and A. Sedrakian, Compact stars with sequential QCD phase transitions. Physical review letters, 119(16), 161104 (2017)..

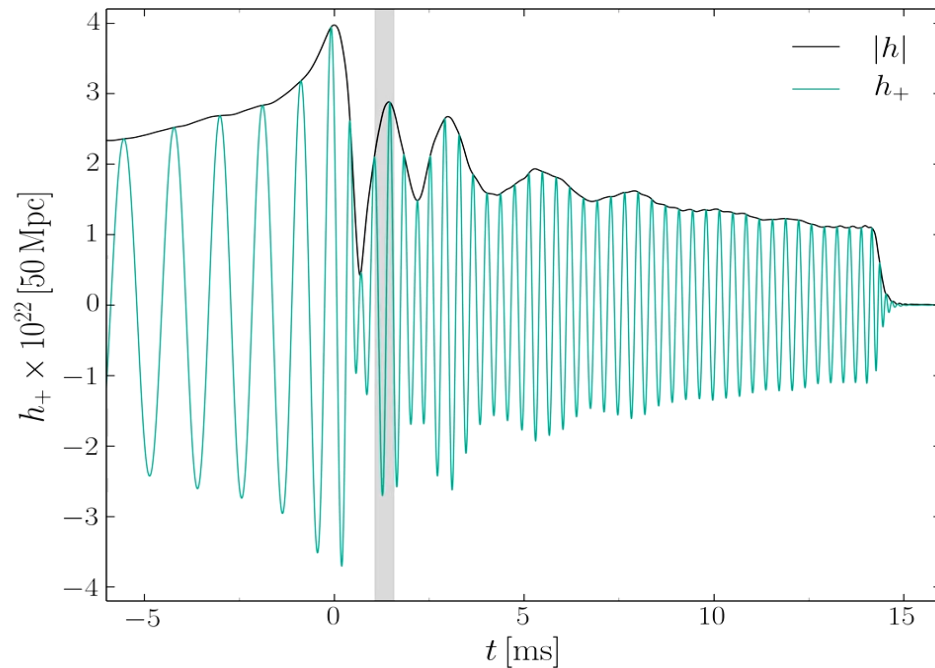
D.Alvarez-Castillo and D.Blaschke, High-mass twin stars with a multipolytrope equation of state. Physical Review C, 96(4), 045809 (2017) .

Glendenning, N. K., & Kettner, C. (1998). Nonidentical neutron star twins. Astron. Astrophys., 352(LR1, 42000) 1-6

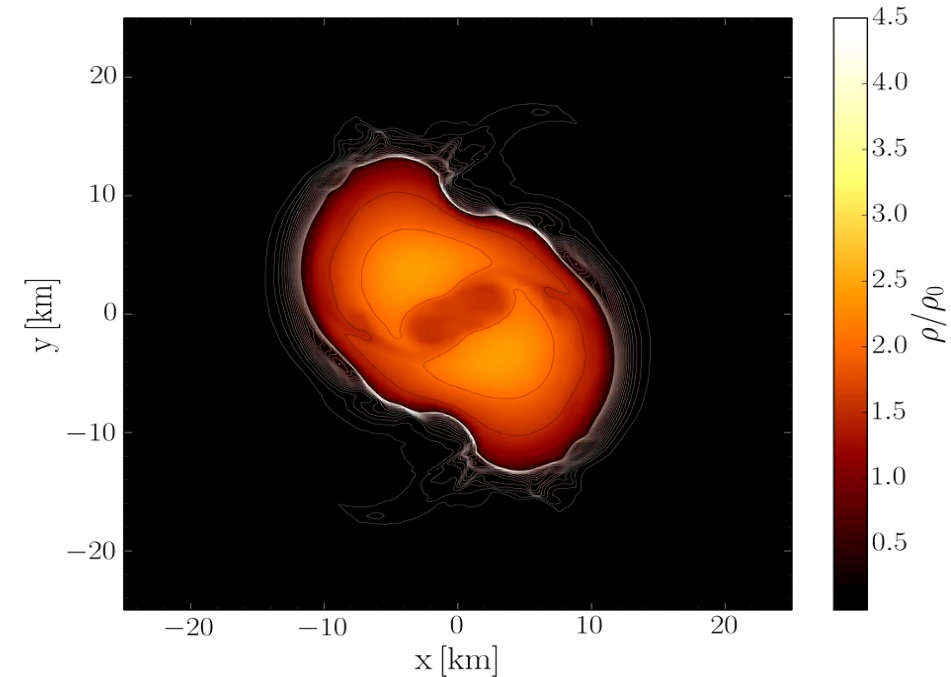
A. Ayriyan, N.-U. Bastian, D. Blaschke, H. Grigorian, K. Maslov, D. N. Voskresensky, How

# Evolution of the density in the post-merger phase

ALF2-EOS: Mixed phase region starts at  $3\rho_0$  (see red curve), initial NS mass:  $1.35 M_{\text{Solar}}$



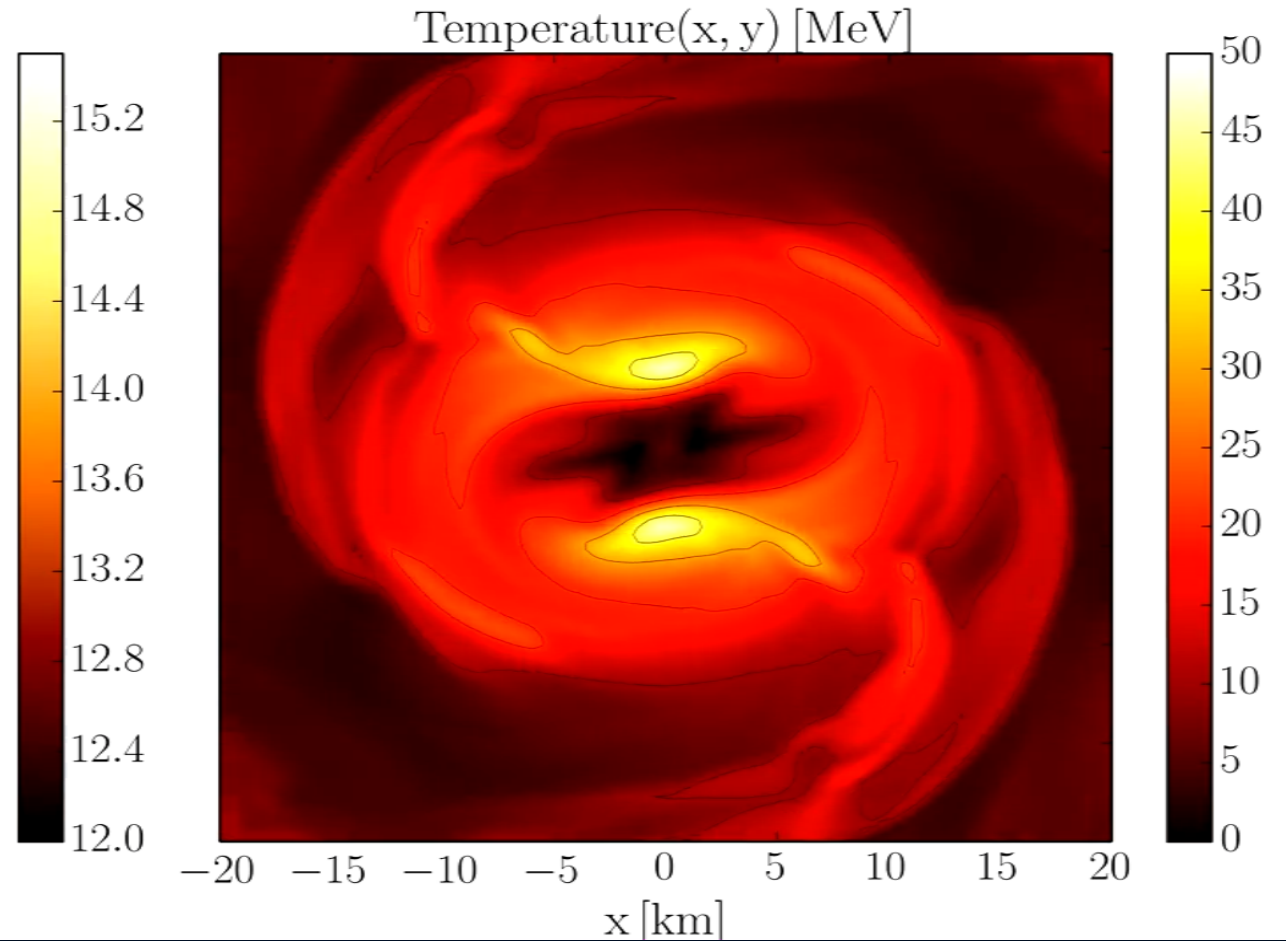
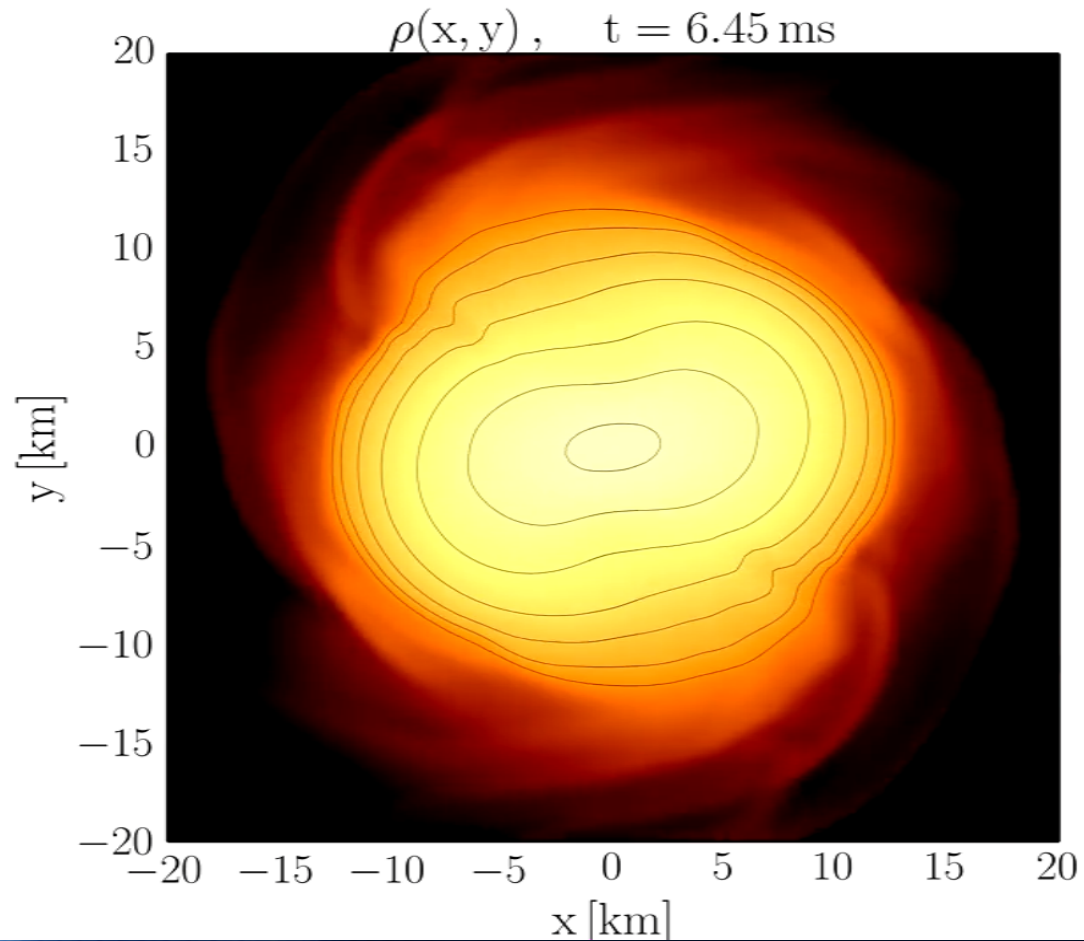
Gravitational wave amplitude  
at a distance of 50 Mpc



Rest mass density distribution  $\rho(x,y)$   
in the equatorial plane  
in units of the nuclear matter density  $\rho_0$

# Density

# Temperature





# The Angular velocity in the (3+1)-Split

The angular velocity  $\Omega$  in the (3+1)-Split is a combination of the lapse function  $\alpha$ , the  $\phi$ -component of the shift vector  $\beta^\phi$  and the 3-velocity  $v^\phi$  of the fluid (spatial projection of the 4-velocity  $\mathbf{u}$ ):

$$\Omega(x, y, z, t) = \frac{u^\phi}{u^t} = \alpha v^\phi - \beta^\phi$$

Angular velocity  
 $\Omega$

Lapse function  
 $\alpha$

$\Phi$ -component of  
3-velocity  $v^\phi$

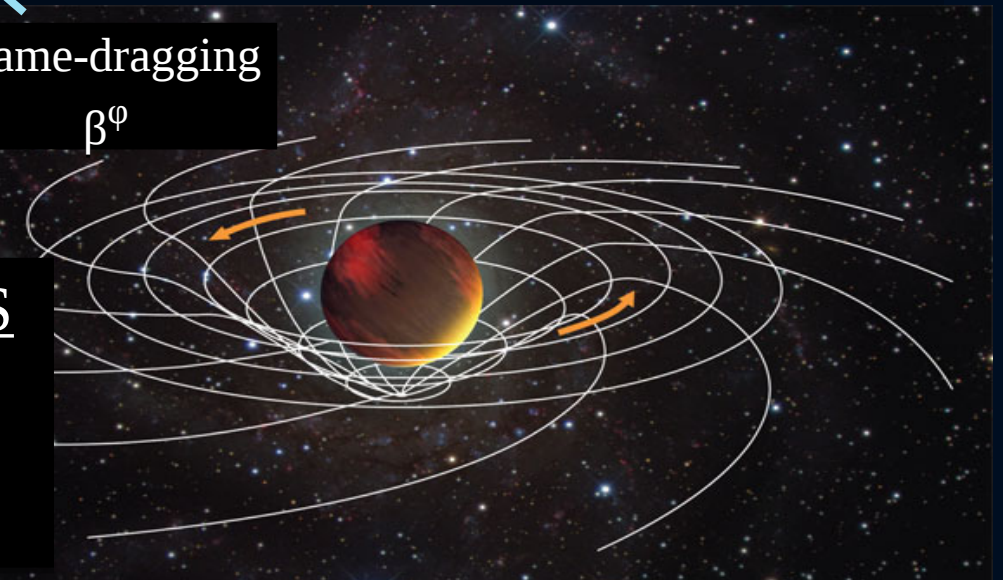
Frame-dragging  
 $\beta^\phi$

(3+1)-decomposition  
of spacetime:

$$g_{\mu\nu} = \begin{pmatrix} -\alpha^2 + \beta_i \beta^i & \beta_i \\ \beta_i & \gamma_{ij} \end{pmatrix}$$

## Focus: Inner core of the differentially rotating HMNS

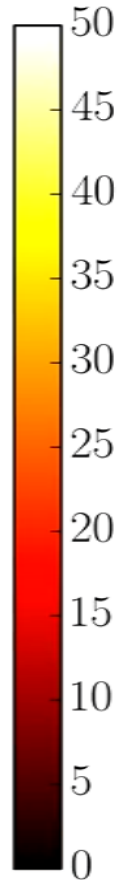
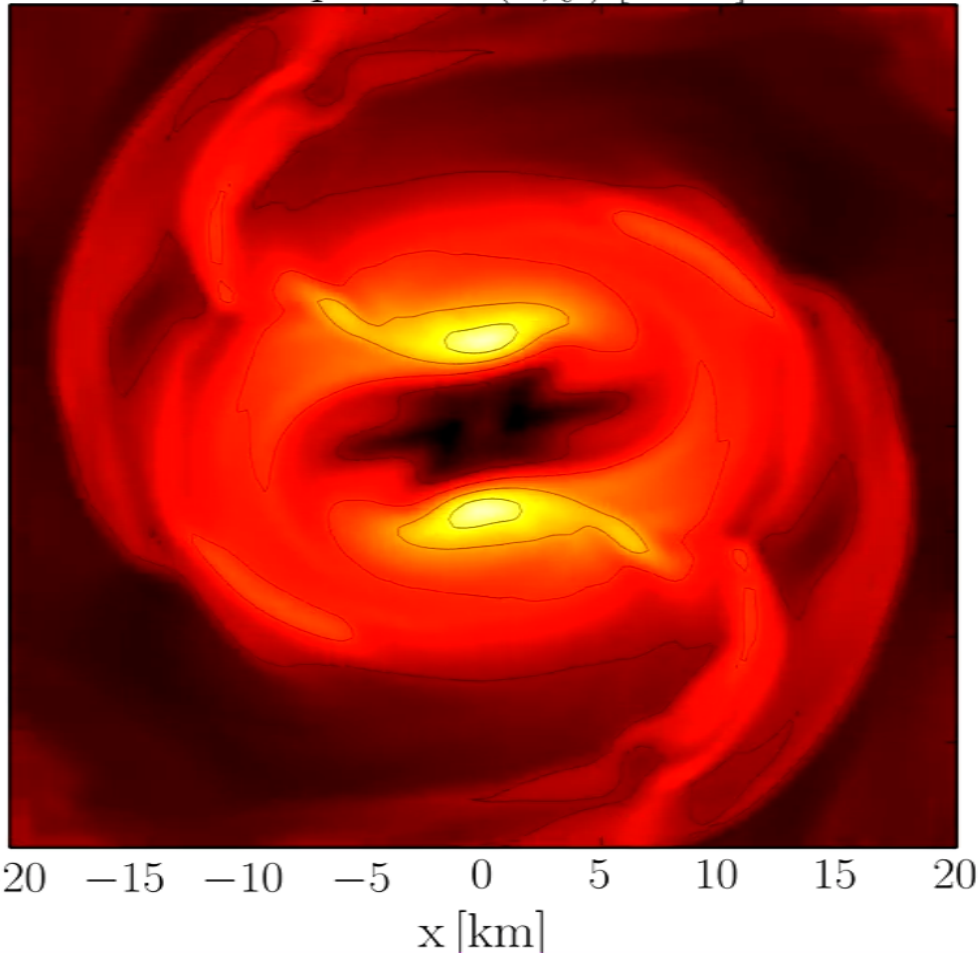
- M. Shibata, K. Taniguchi, and K. Uryu, Phys. Rev. D 71, 084021 (2005)
- M. Shibata and K. Taniguchi, Phys. Rev. D 73, 064027 (2006)
- F. Galeazzi, S. Yoshida and Y. Eriguchi, A&A 541, p. A156 (2012)
- W. Kastaun and F. Galeazzi, Phys. Rev. D 91, p. 064027 (2015)



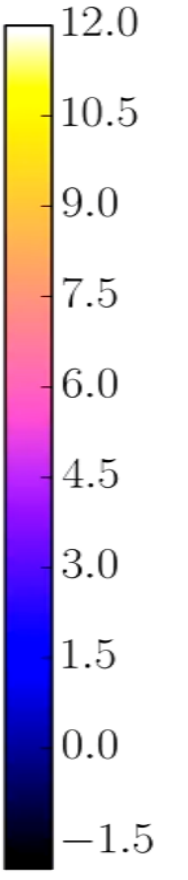
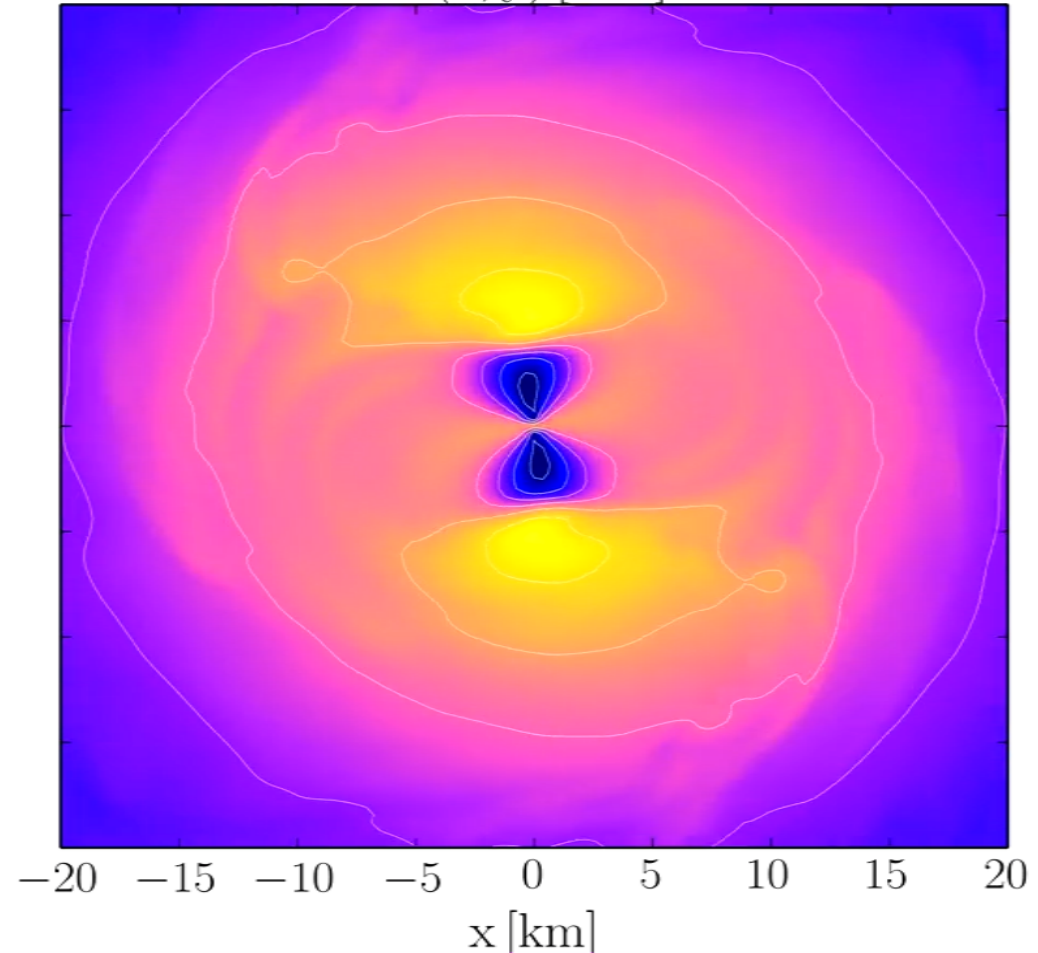
# Temperature

# Angular Velocity

Temperature(x, y) [MeV]

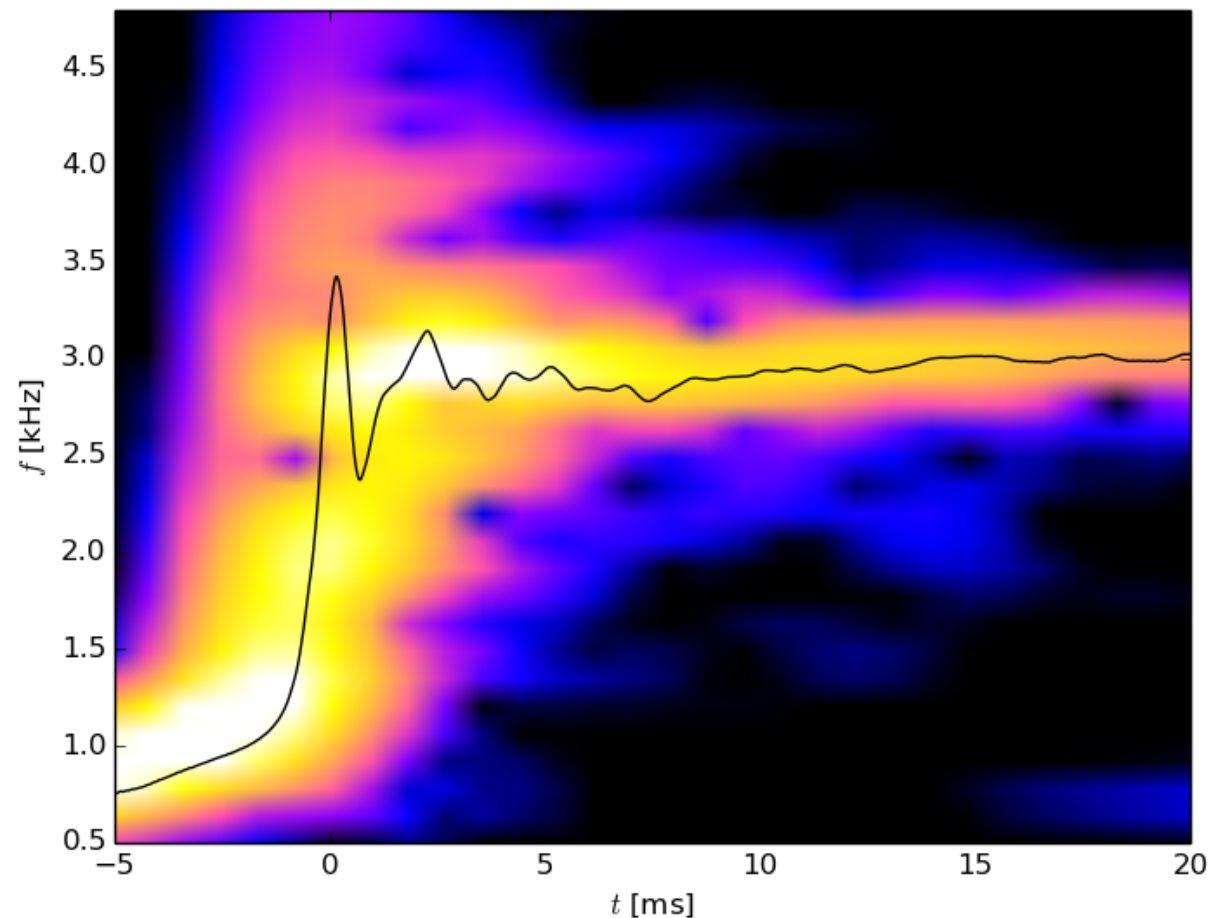
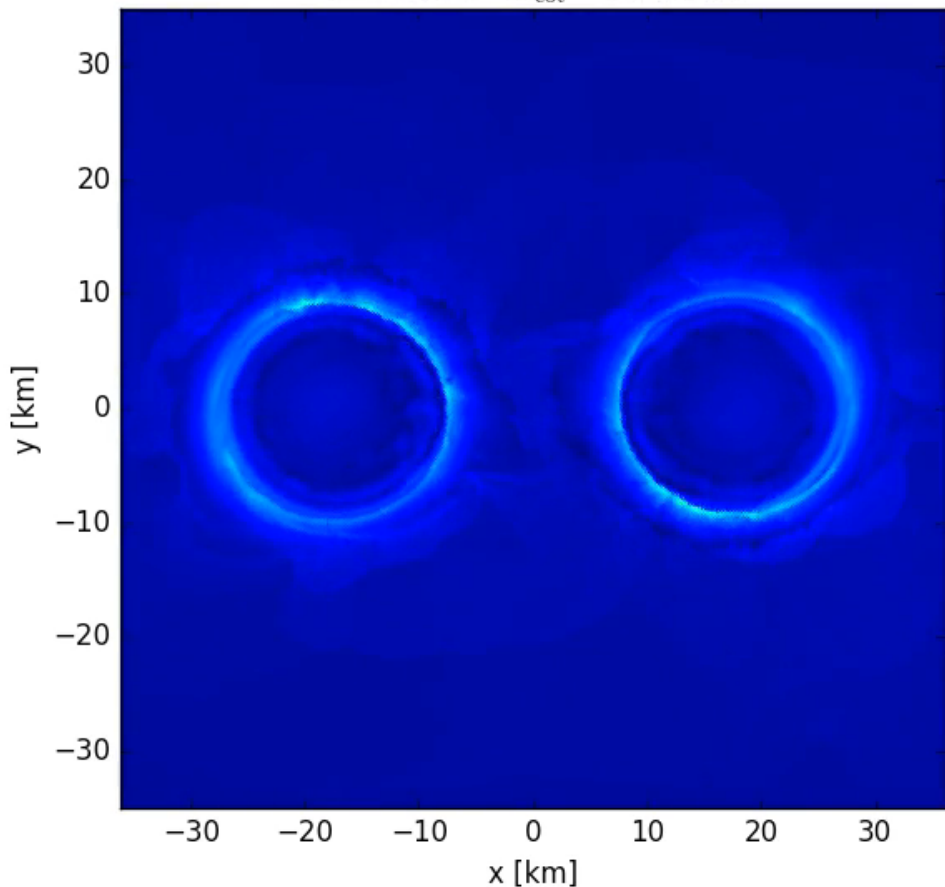


$\Omega(x, y)$  [kHz]



# The Co-Rotating Frame

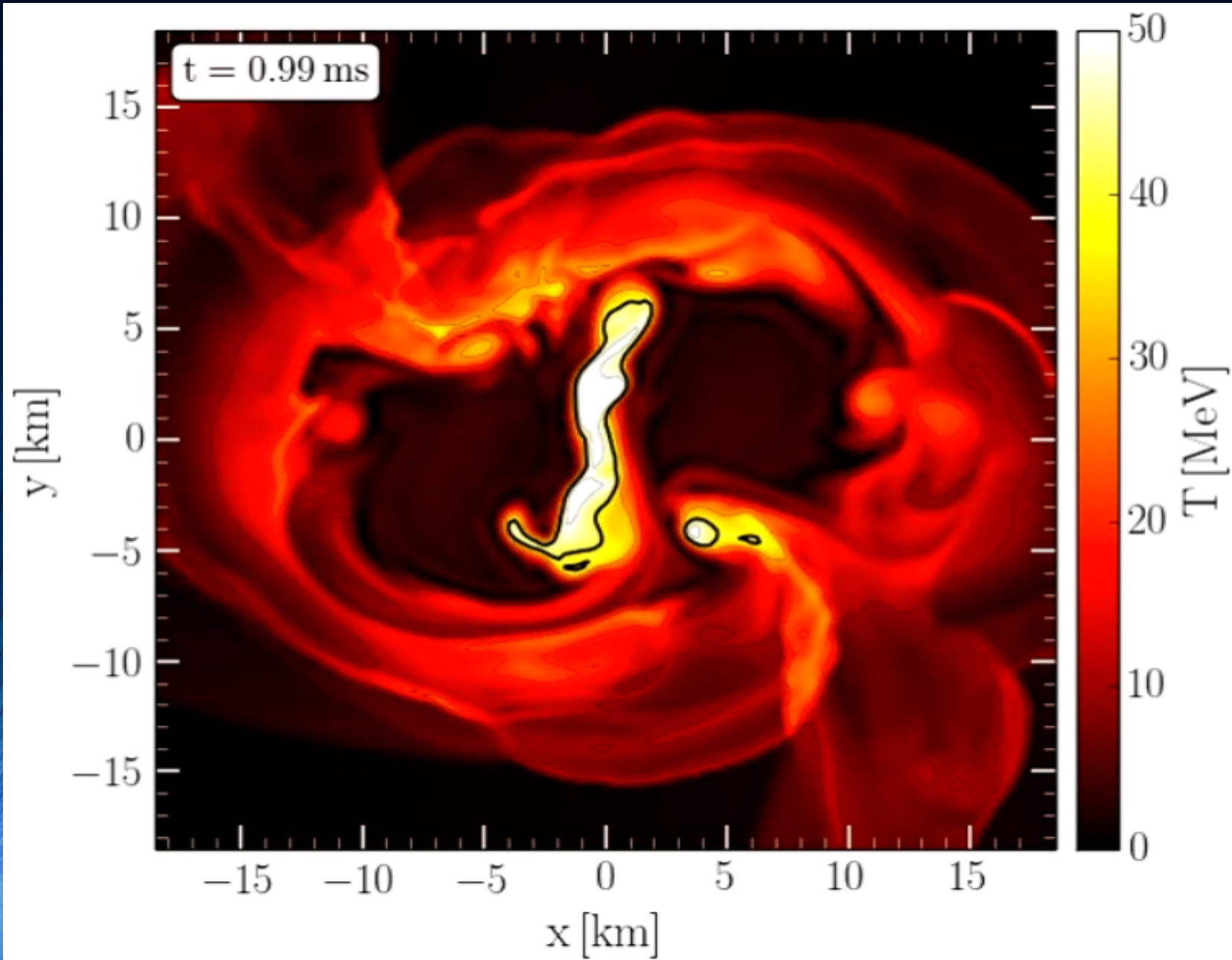
$t = 9.58\text{ms}$   $\Omega_{\text{cot}} = 387.20\text{Hz}$



<sup>2</sup> Note that the angular-velocity distribution in the lower central panel of Fig. 10 refers to the corotating frame and that this frame is rotating at half the angular frequency of the emitted gravitational waves,  $\Omega_{\text{GW}}$ . Because the maximum of the angular velocity  $\Omega_{\text{max}}$  is of the order of  $\Omega_{\text{GW}}/2$  (cf. left panel of Fig. 12), the ring structure in this panel is approximately at zero angular velocity.

Simulation and movie has been produced by Luke Bovard

## Evolution of the Temperature in the post merger phase



Hanuske, M., Takami, K., Bovard, L., Rezzolla, L., Font, J. A., Galeazzi, F., & Stöcker, H. (2017). Rotational properties of hypermassive neutron stars from binary mergers. *Physical Review D*, 96(4), 043004

Kastaun, W., Ciolfi, R., Endrizzi, A., & Giacomazzo, B. (2017). Structure of stable binary neutron star merger remnants: Role of initial spin. *Physical Review D*, 96(4), 043019

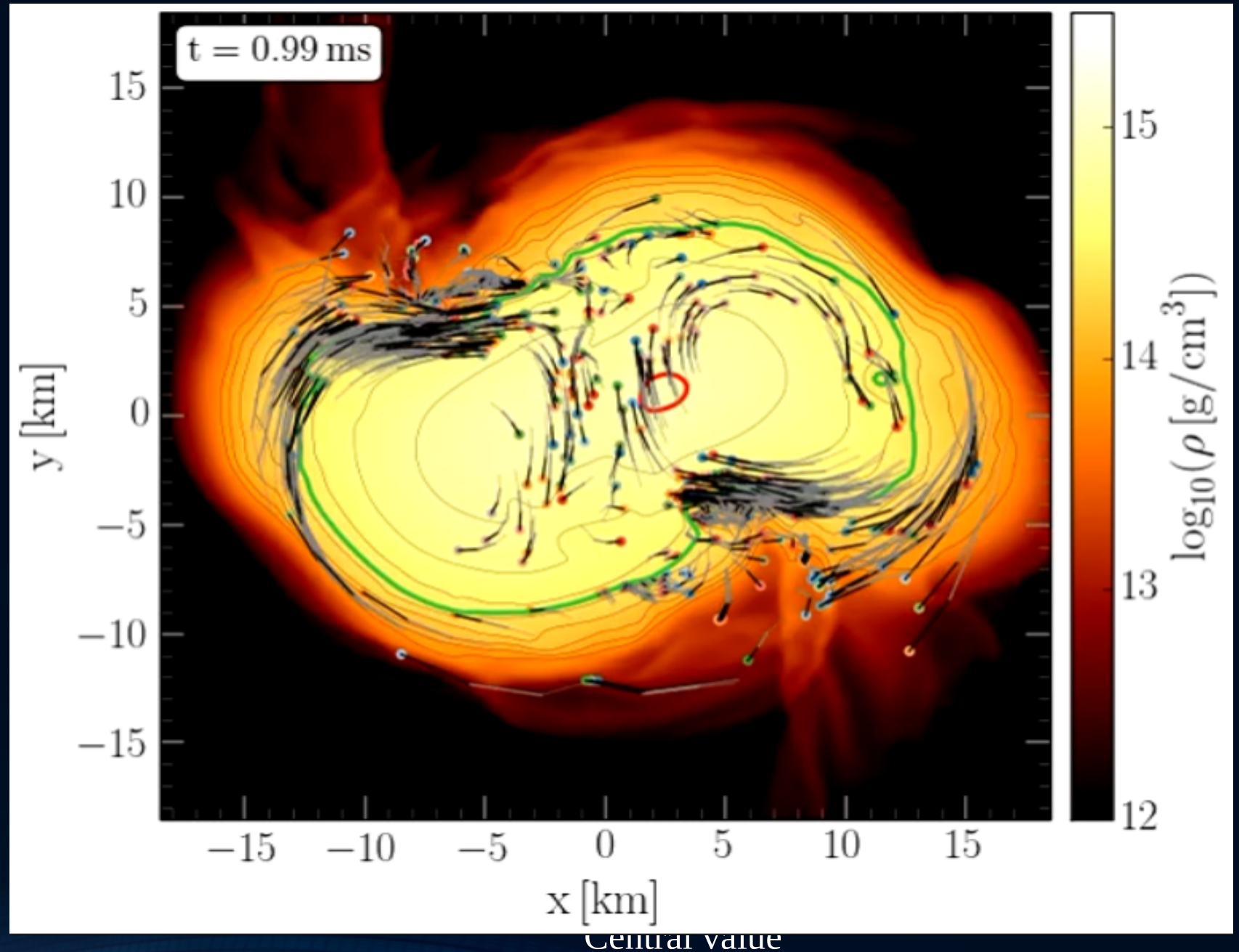
M. Hanuske, et.al., Connecting Relativistic Heavy Ion Collisions and Neutron Star Mergers by the Equation of State of Dense Hadron-and Quark Matter as signalled by Gravitational

particles tracking  
individual fluid  
elements in the  
equatorial plane of the  
HMNS at post-merger  
times

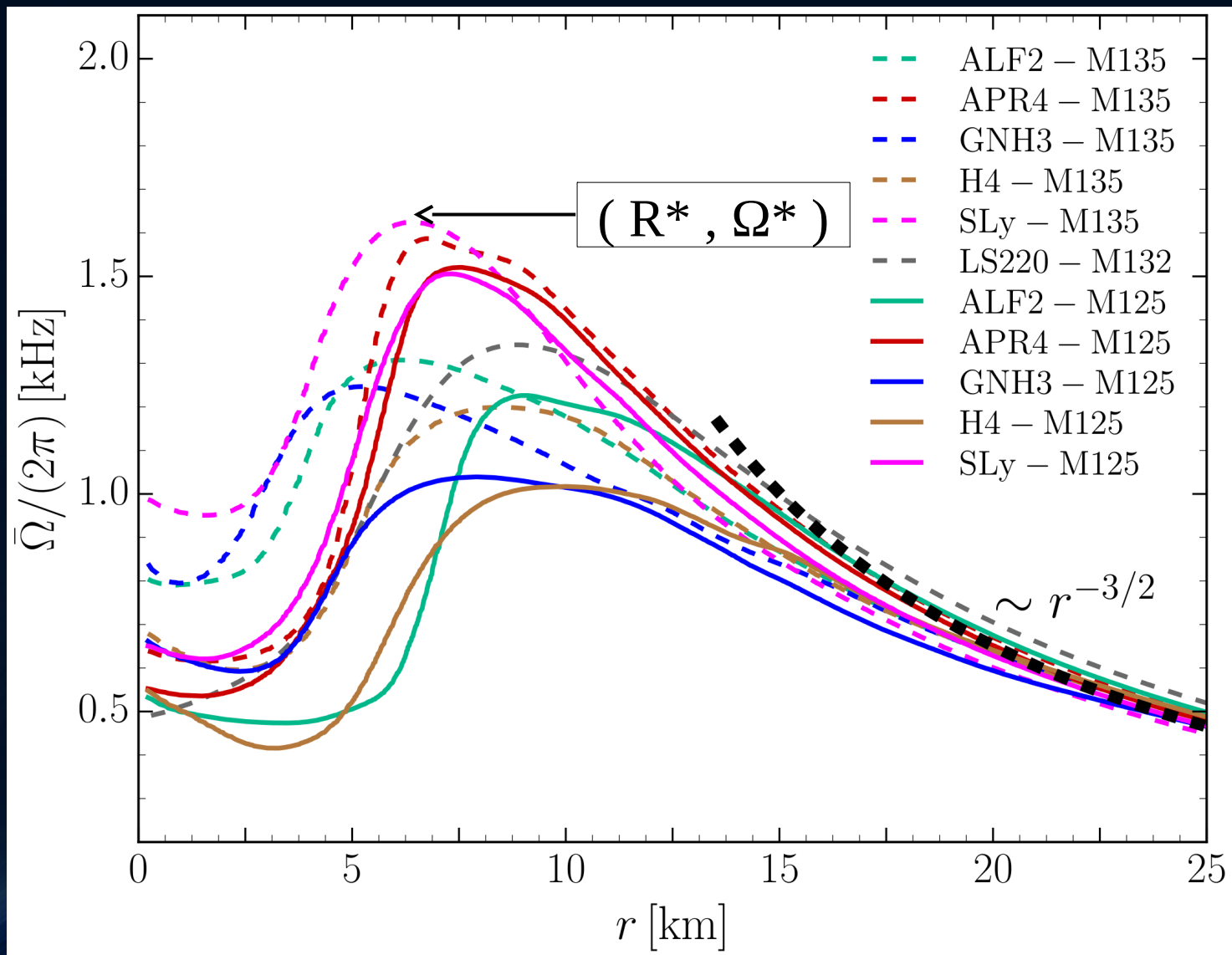
Mark G. Alford, Luke Bovard,  
Matthias Hanauske, Luciano  
Rezzolla, and Kai Schwenzer  
(2018)

Viscous Dissipation and Heat  
Conduction in Binary Neutron-  
Star Mergers. *Phys. Rev. Lett.*  
120, 041101

Different rotational behaviour  
of the quark-gluon-plasma  
produced in non-central ultra-  
relativistic heavy ion collisions  
L. Adamczyk et.al., "Global  
Lambda-hyperon polarization  
in nuclear collisions: evidence  
for the most vortical fluid",  
*Nature* 548, 2017



# Time-averaged Rotation Profiles of the HMNSs



Soft EoSs:

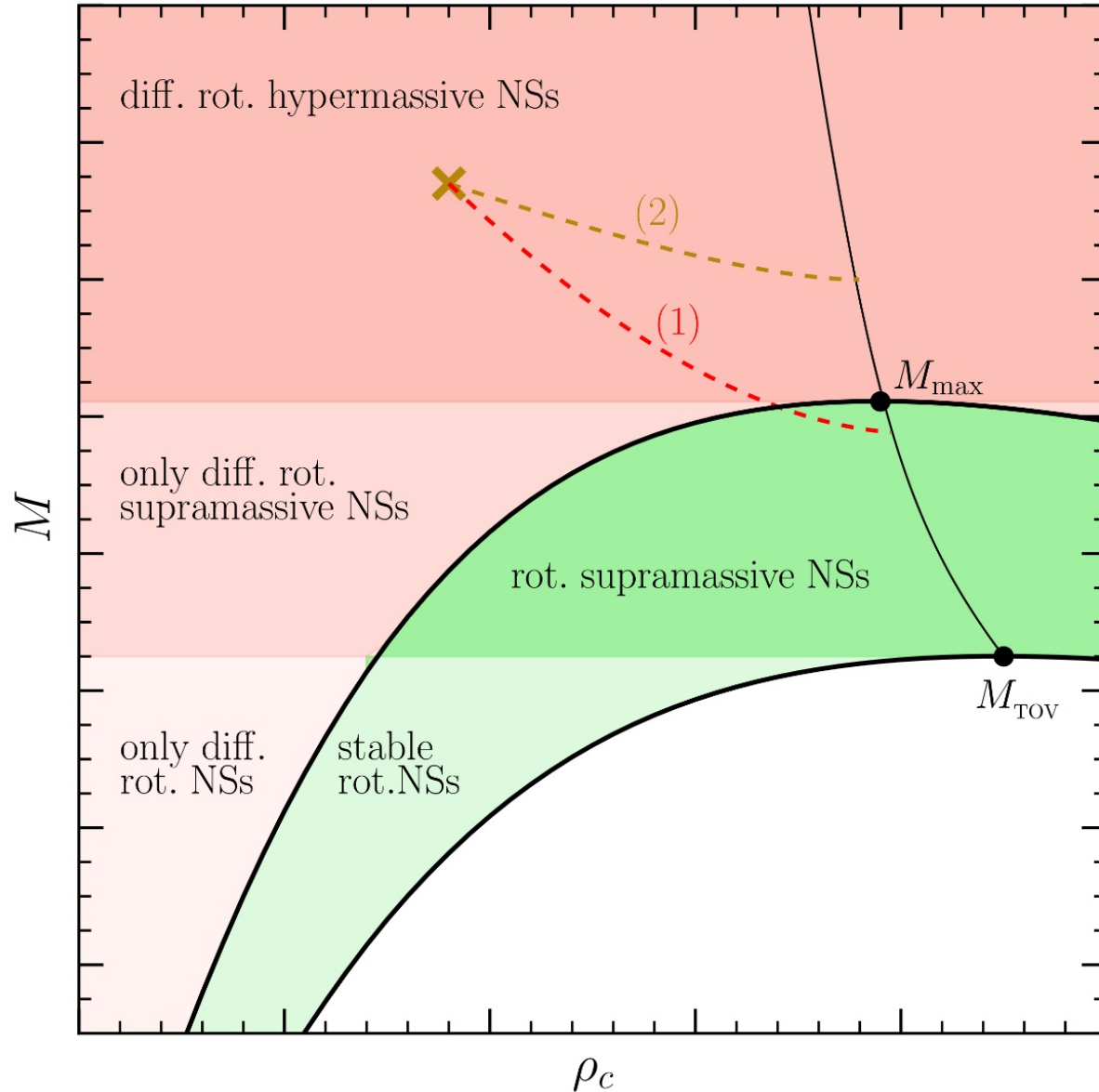
Sly  
APR4

Stiff EoSs:

GNH3  
H4

Time-averaged rotation profiles for different EoS  
Low mass runs (solid curves), high mass runs (dashed curves).

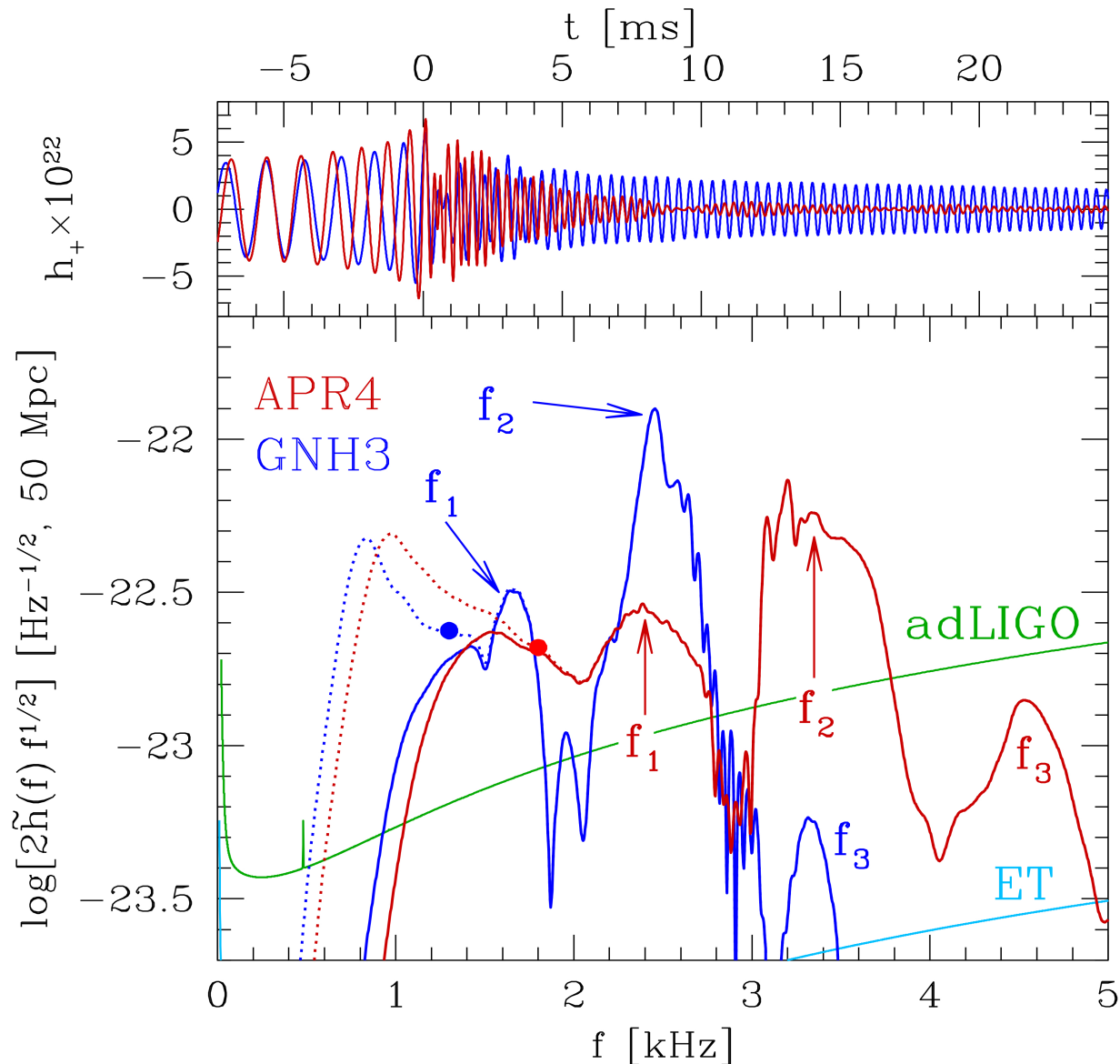
# GW170817: Evolution of the HMNS until BH formation



The highly differentially rotating hypermassive/supramassive neutron star will spin down and redistribute its angular momentum (e.g. due to magnetic braking). After  $\sim 1$  second it will cross the stability line as a uniformly rotating supramassive neutron star (close to  $M_{\max}$ ) and collapse to a black hole. Parts of the ejected matter will fall back into the black hole producing the gamma-ray burst.

L.Rezzolla, E.Most, L.Weih, "Using Gravitational Wave Observations and Quasi-Universal Relations to constrain the maximum Mass of Neutron Stars", arXiv:1711.00314 (accepted in ApJL)  
 $2.01 \pm 0.04 < M_{\max} < 2.16 \pm 0.17$   
E.Most, L.Weih, L.Rezzolla, J. Schaffner-Bielich "New constraints on radii and tidal deformabilities of neutron stars from GW170817", arXiv:1803.00549  
 $12\text{km} < R_{1.4} < 13.45\text{km}$  ,  $\Lambda_{1.4} > 375$

# GW-Spectrum for different EOSs



See:

Kentaro Takami, Luciano Rezzolla, and Luca Baiotti, *Physical Review D* 91, 064001 (2015)

Hotokezaka, K., Kiuchi, K., Kyutoku, K., Muranushi, T., Sekiguchi, Y. I., Shibata, M., & Taniguchi, K. (2013). *Physical Review D*, 88(4), 044026.

Bauswein, A., & Janka, H. T. (2012). *Physical review letters*, 108(1), 011101.

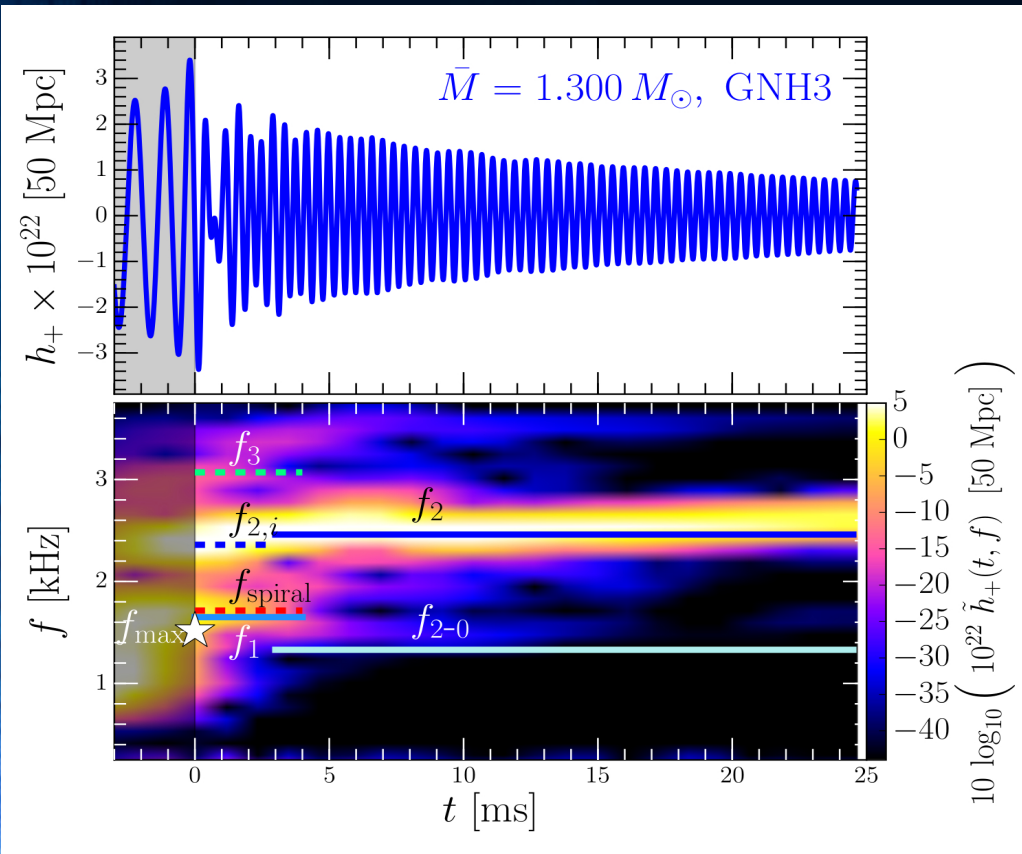
Clark, J. A., Bauswein, A., Stergioulas, N., & Shoemaker, D. (2015). *arXiv:1509.08522*.

Bernuzzi, S., Dietrich, T., & Nagar, A. (2015). *Physical review letters*, 115(9), 091101.

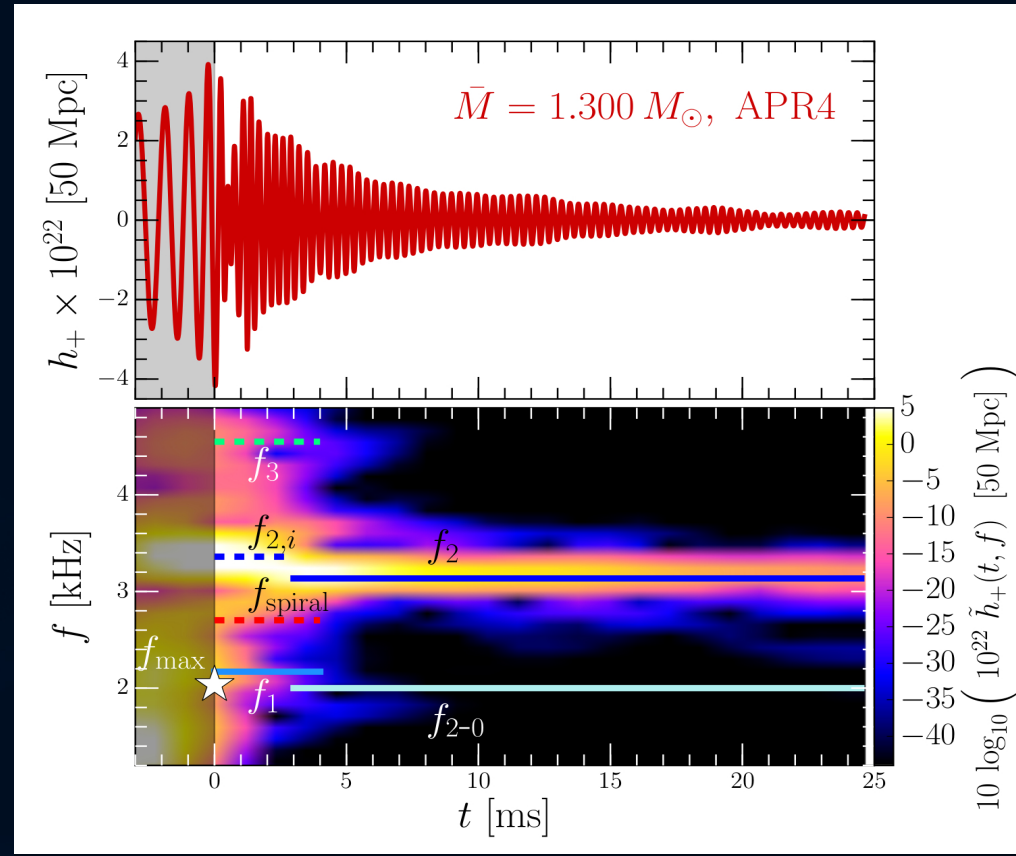


# Time Evolution of the GW-Spectrum

The power spectral density profile of the post-merger emission is characterized by several distinct frequencies. After approximately 5 ms after merger, the only remaining dominant frequency is the  $f_2$ -frequency (See e.g. L.Rezzolla and K.Takami, PRD, 93(12), 124051 (2016))



Stiff EOS

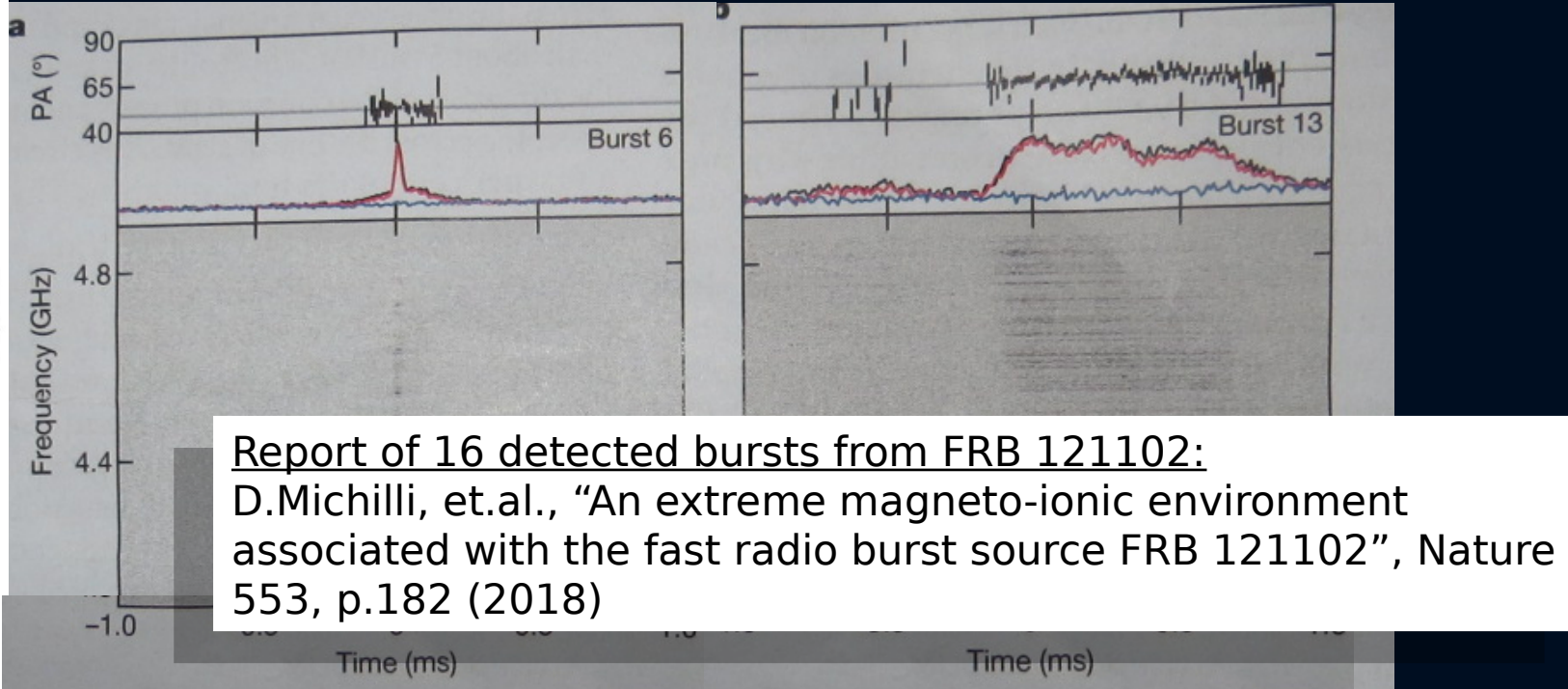
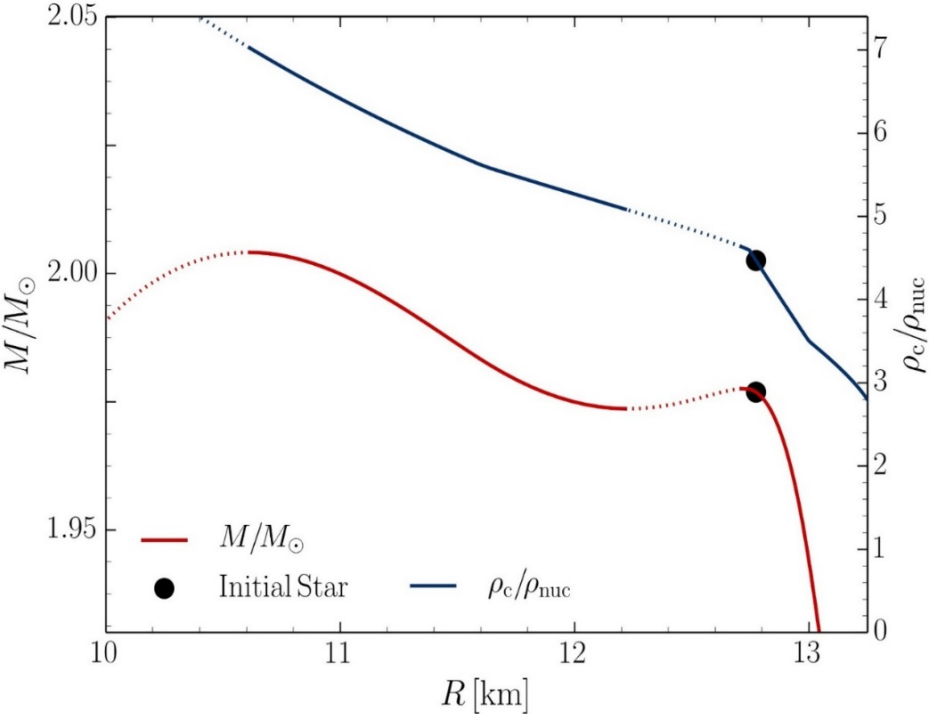


Soft EOS

Unfortunately, due to the low sensitivity at high gravitational wave frequencies, no post-merger signal has been found in GW170817.

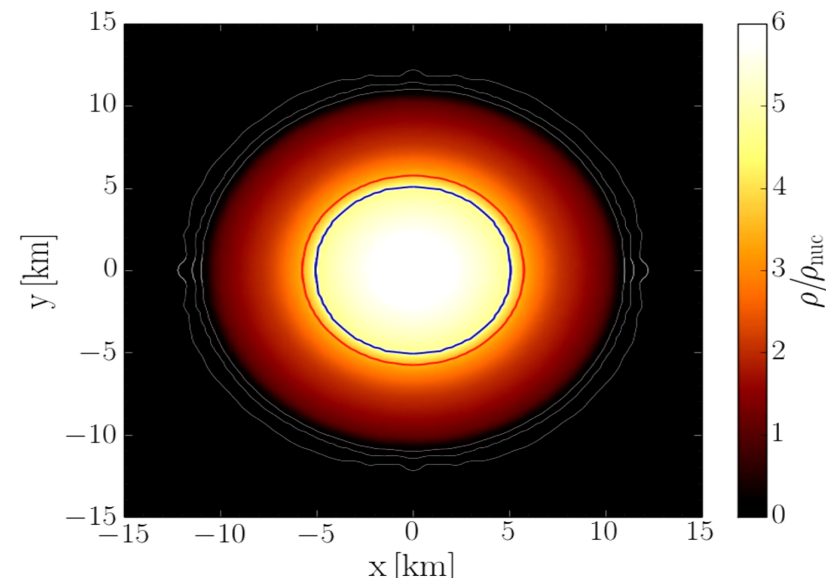
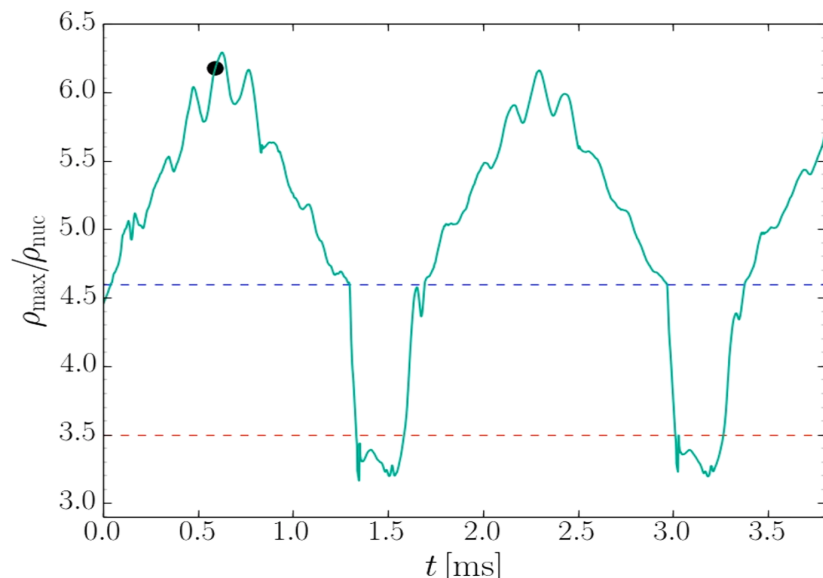
But advanced detectors / next-generation detectors might be able to detect!!!

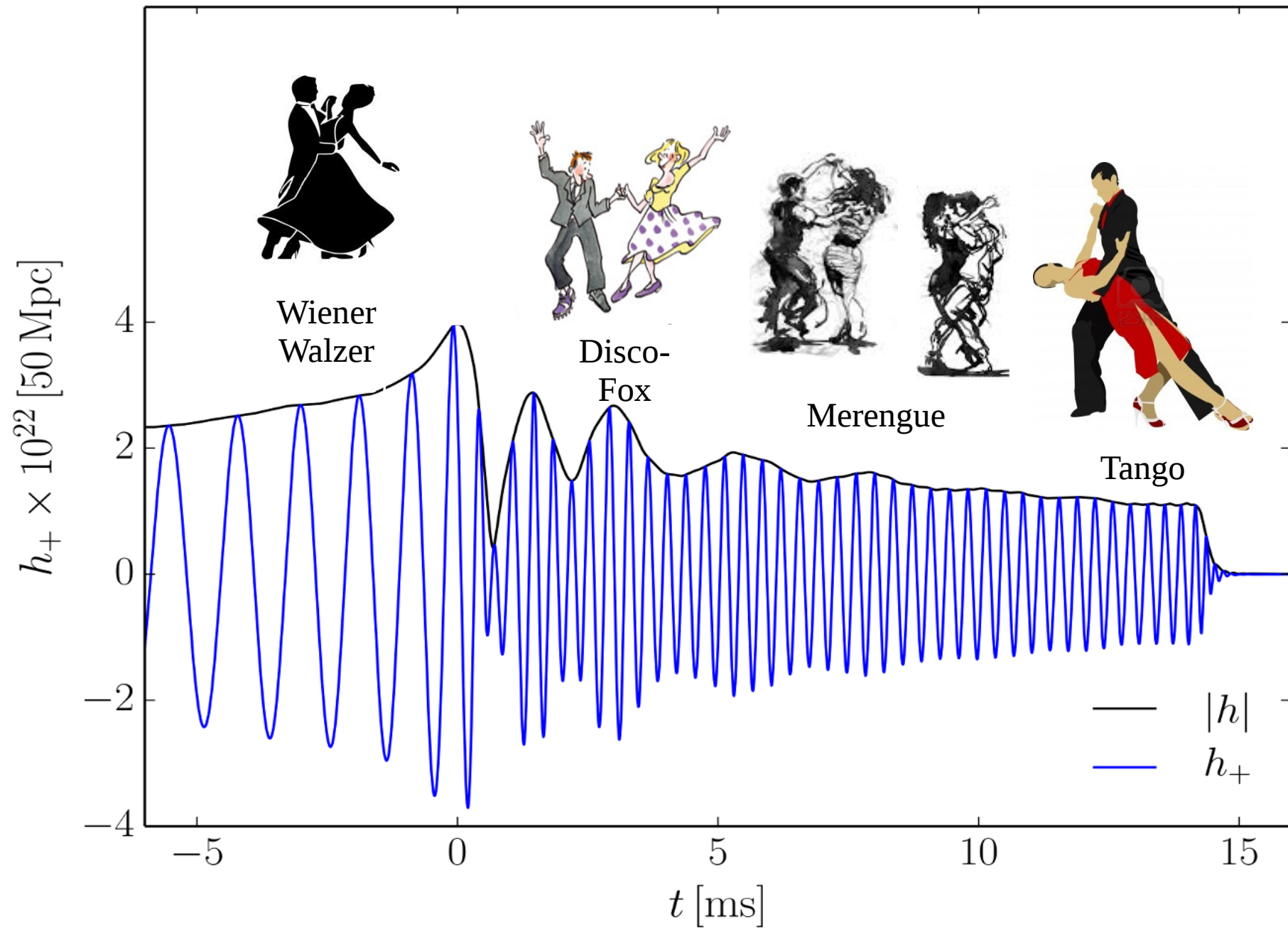
Evolution of the frequency spectrum of the emitted gravitational waves for the stiff GNH3 (left) and soft APR4 (right) EOS.

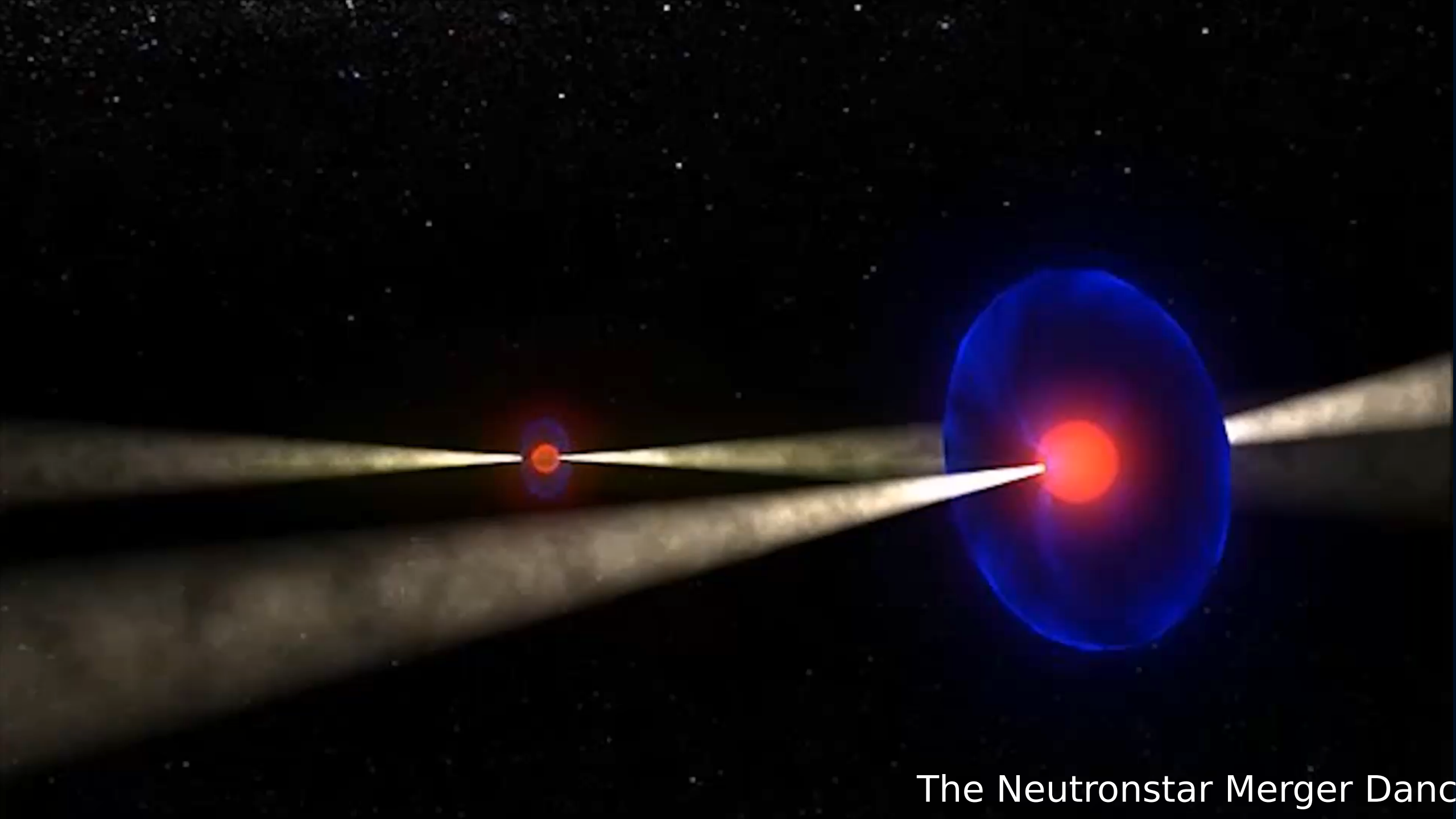


Report of 16 detected bursts from FRB 121102:  
 D.Michilli, et.al., "An extreme magneto-ionic environment associated with the fast radio burst source FRB 121102", Nature 553, p.182 (2018)

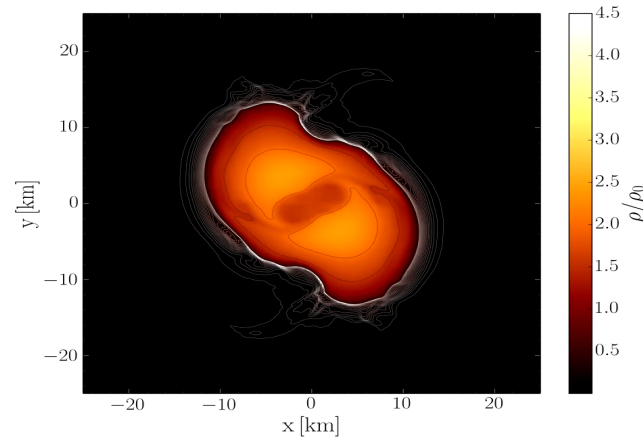
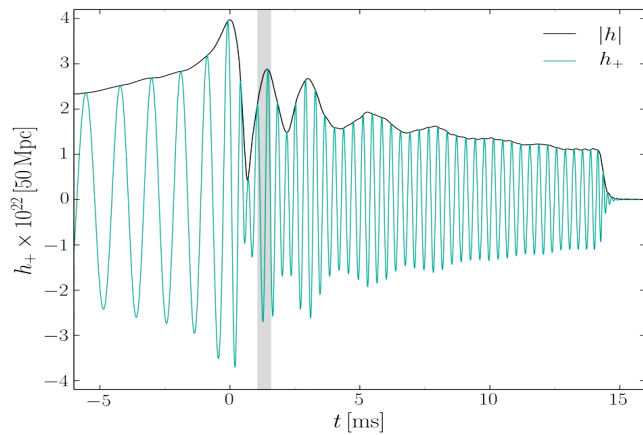
M.Hanauske, et.al.,  
 "Twin Star Oscillations"  
 (in preparation)







The Neutronstar Merger Dance



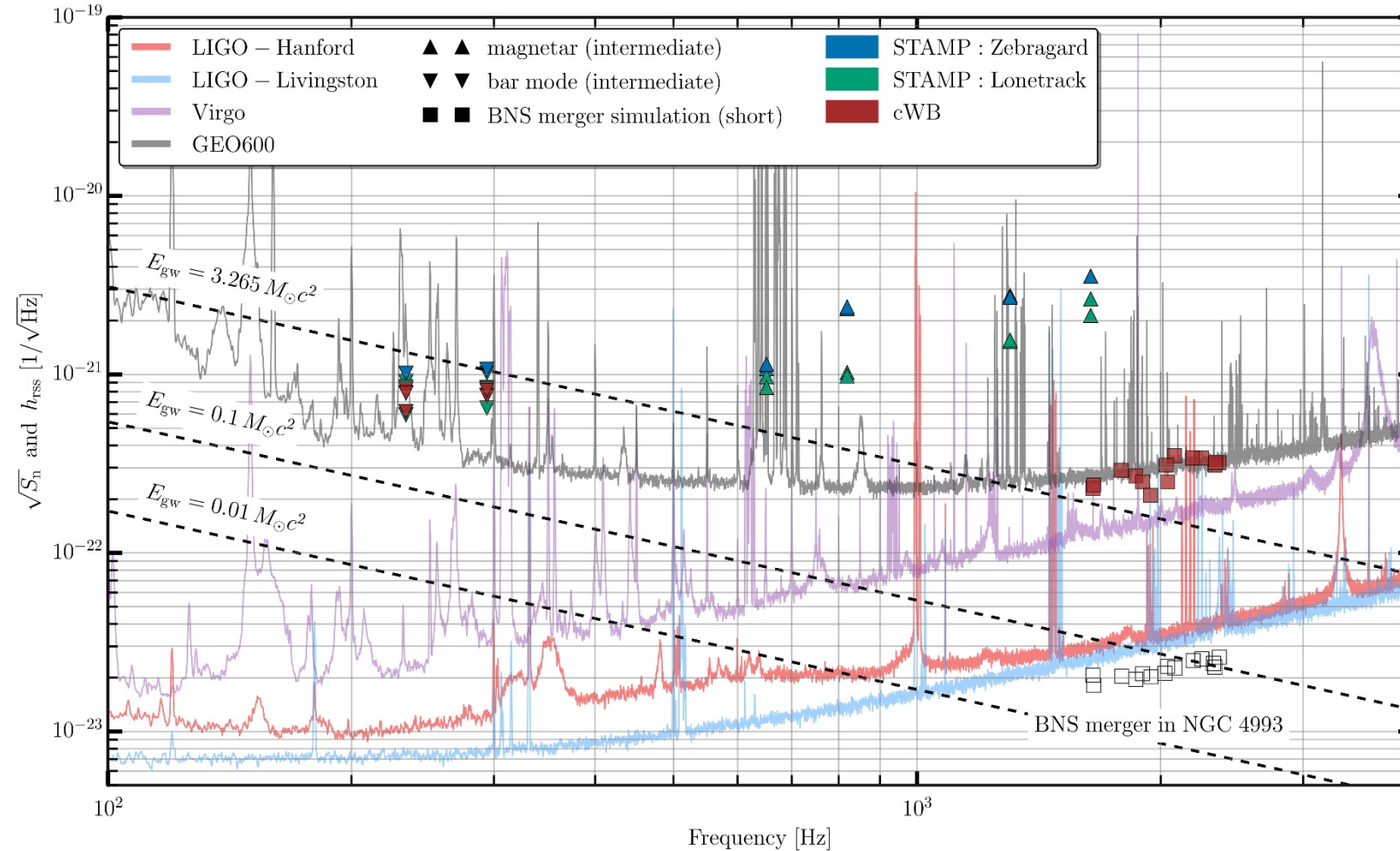
# Summary and Discussions

ALF2-EOS: Mixed phase region starts at  $3\rho_0$  (see red curve)

- In the post-merger phase of a binary neutron star merger, the density and temperature will reach extreme values and it is expected that a hadron-quark phase transition will be present in the interior region of the supramassive or hypermassive neutron star.
- Astrophysical observables of the hadron-quark phase transition:
  - If such a twin star collapse would happen during the postmerger phase it will be imprinted in the GW-signal
  - If the unstable twin star region is reached during the "post-transient" phase, the f2-frequency peak of the GW signal will change rapidly due to the sudden speed up of the differentially rotating HMNS

# Additional Slides

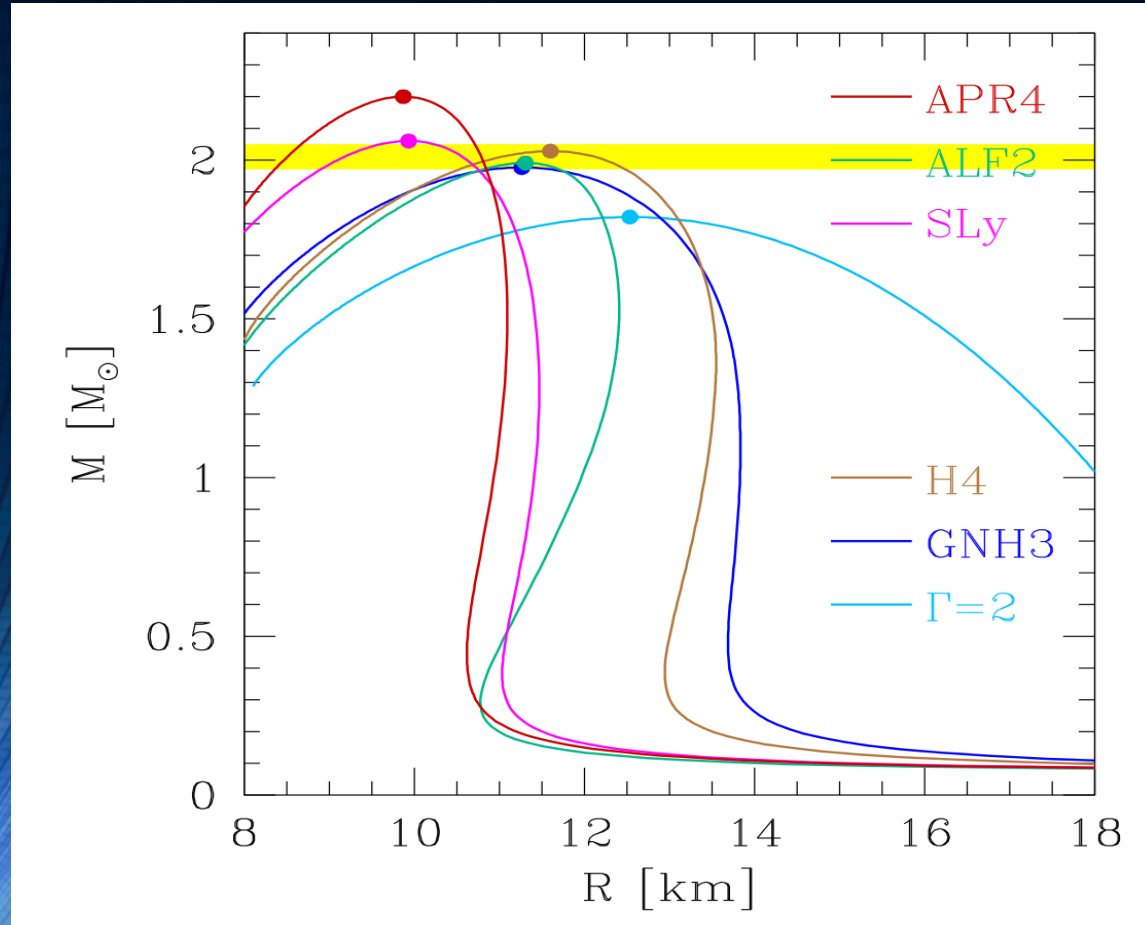
# SEARCH FOR POST-MERGER GRAVITATIONAL WAVES FROM THE REMNANT OF THE BINARY NEUTRON STAR MERGER GW170817 (see arXiv:1710.09320v1)



Unfortunately, due to the low sensitivity at high gravitational wave frequencies, no post-merger signal has been found in GW170817.

But, the results indicate that post-merger emission from a similar event may be detectable when advanced detectors reach design sensitivity or with next-generation detectors.

**Several different EOSs** : ALF2, APR4, GNH3, H4 and SLy, approximated by piecewise polytopes. Thermal ideal fluid component ( $\Gamma=2$ ) added to the nuclear-physics EOSs.



# EOSs

composed of a “cold” nuclear-physics part and of a “thermal” ideal-fluid component<sup>1</sup> [56]

$$p = p_c + p_{\text{th}}, \quad \epsilon = \epsilon_c + \epsilon_{\text{th}}, \quad (6)$$

where  $p$  and  $\epsilon$  are the pressure and specific internal energy,

The “cold” nuclear-physics contribution to each EOS is obtained after expressing the pressure and specific internal energy  $\epsilon_c$  in the rest-mass density range  $\rho_{i-1} \leq \rho < \rho_i$  as (for details see [36, 64–66])

$$p_c = K_i \rho^{\Gamma_i}, \quad \epsilon_c = \epsilon_i + K_i \frac{\rho^{\Gamma_i-1}}{\Gamma_i - 1}. \quad (7)$$

( $\Gamma_1 = 4.070$  and  $\Gamma_2 = 2.411$ ). Finally, the “thermal” part of the EOS is given by

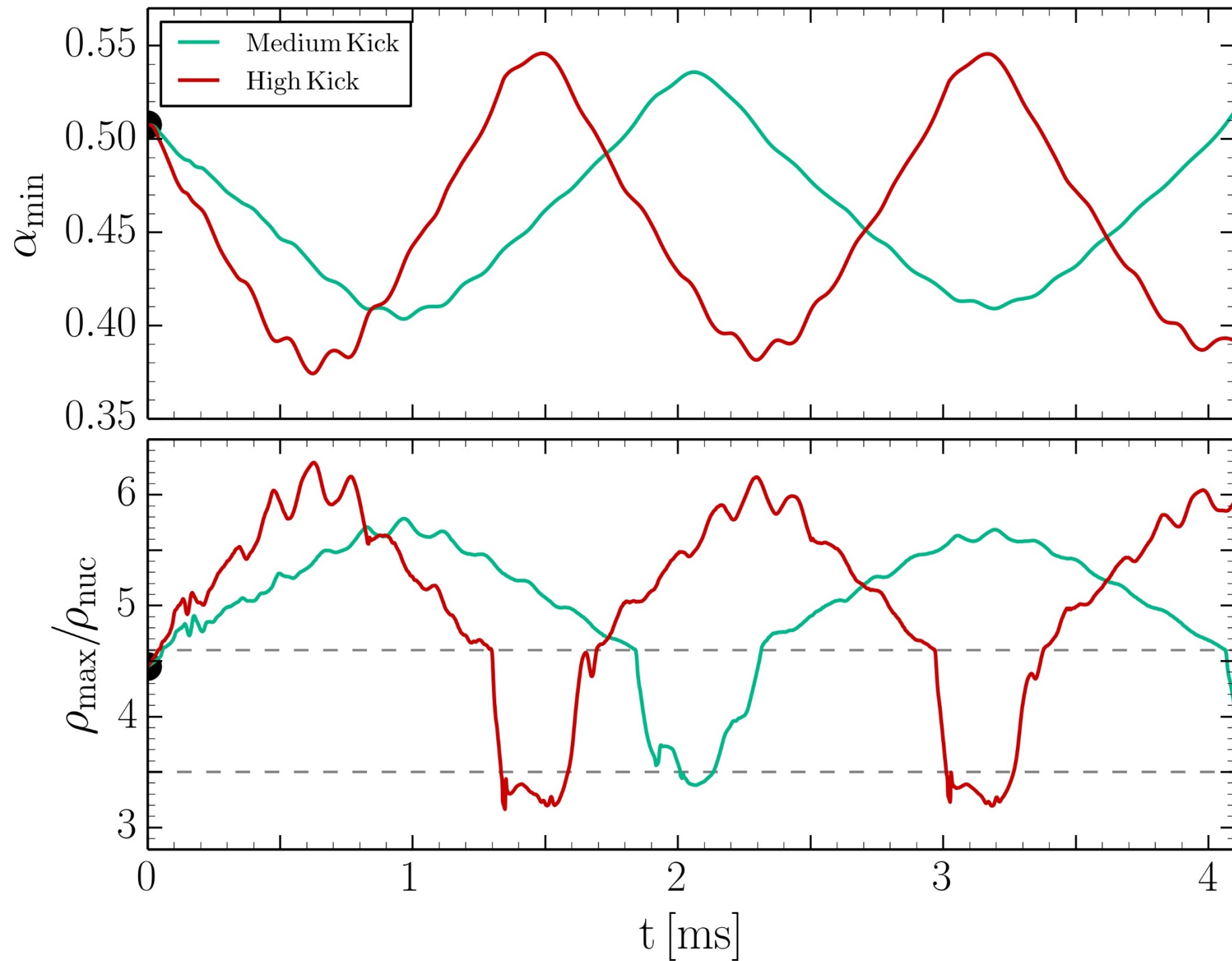
$$p_{\text{th}} = \rho \epsilon_{\text{th}} (\Gamma_{\text{th}} - 1), \quad \epsilon_{\text{th}} = \epsilon - \epsilon_c. \quad (8)$$

where the last equality in (8) is really a definition, since  $\epsilon$  refers to the computed value of the specific internal energy. In all of the simulations reported hereafter we use  $\Gamma_{\text{th}} = 2.0$

Additionally LS220-EOS used: Density and Temperature dependent EOS-table (Lattimer-Swesty)



# Twin Star Oscillations

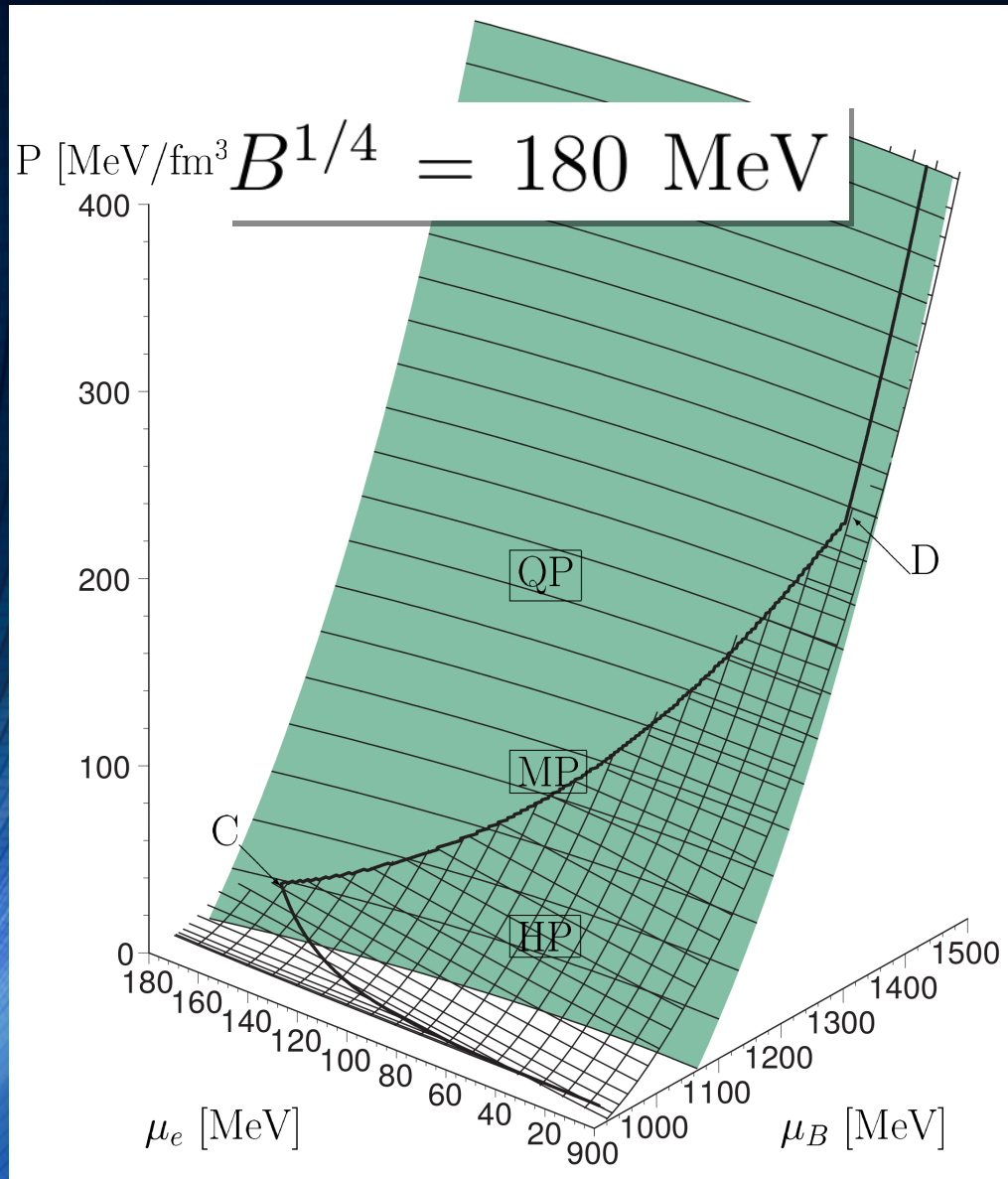


Yamasaki, S., Totani, T., & Kiuchi, K. (2017).  
Repeating and Non-repeating Fast Radio  
Bursts from Binary  
Neutron Star Mergers.  
arXiv preprint  
arXiv:1710.02302.

Michilli, D, et.al. (2018).  
An extreme magneto-ionic  
environment associated

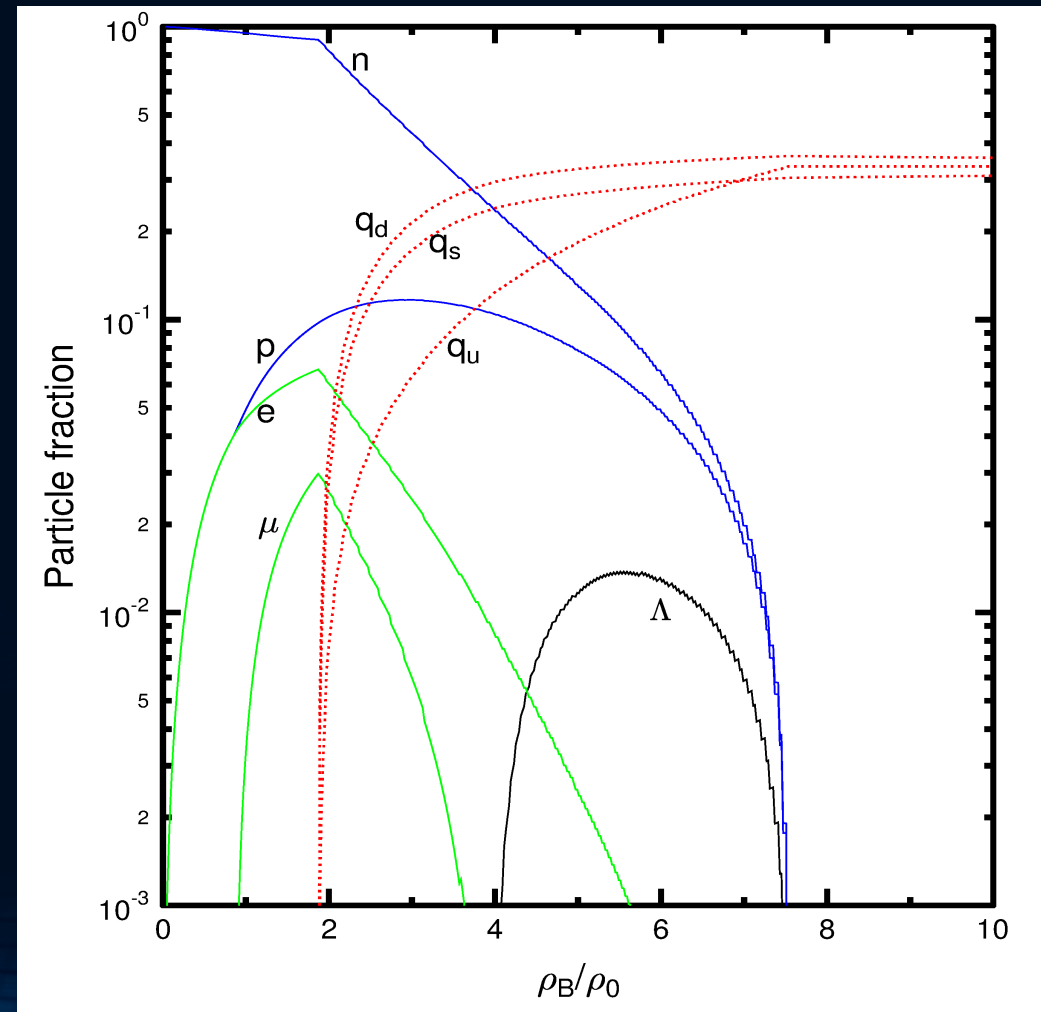
# The Gibbs Construction

Hadronic and quark surface:



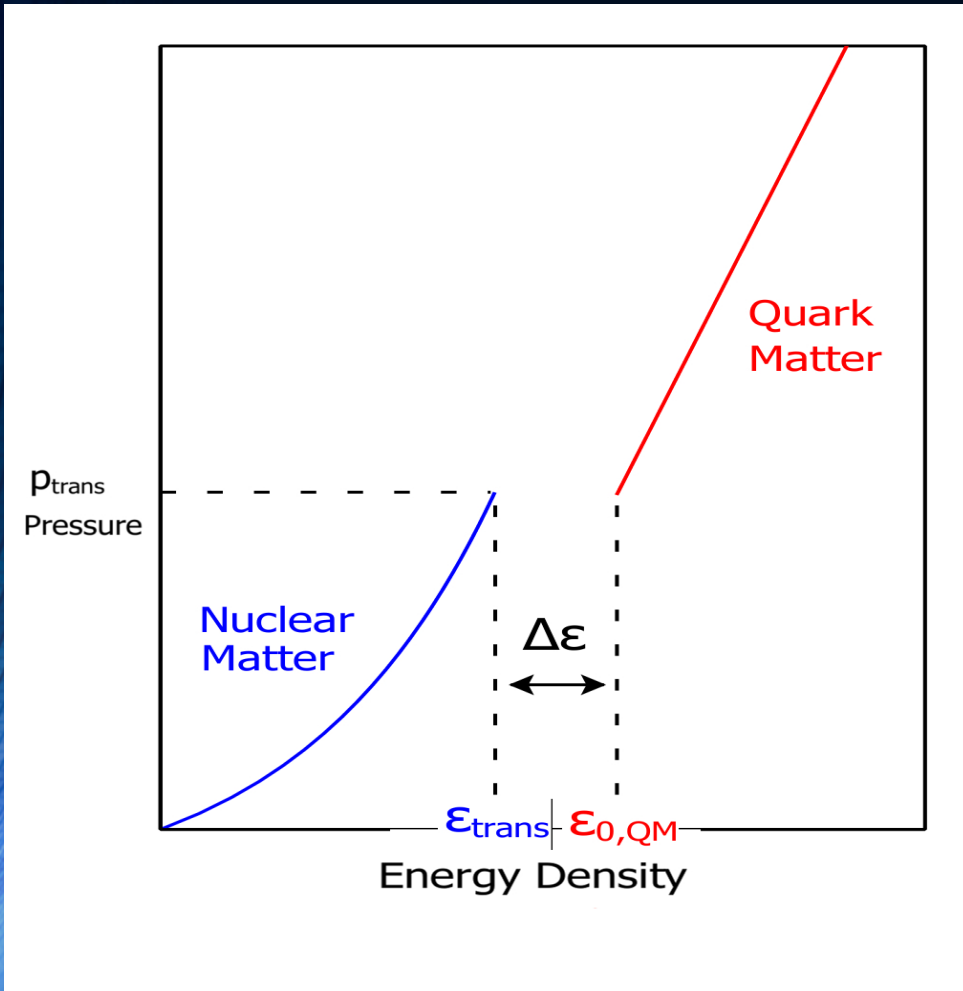
Charge neutrality condition is only globally realized

$$\rho_e := (1 - \chi) \rho_e^H(\mu_B, \mu_e) + \chi \rho_e^Q(\mu_B, \mu_e) = 0.$$

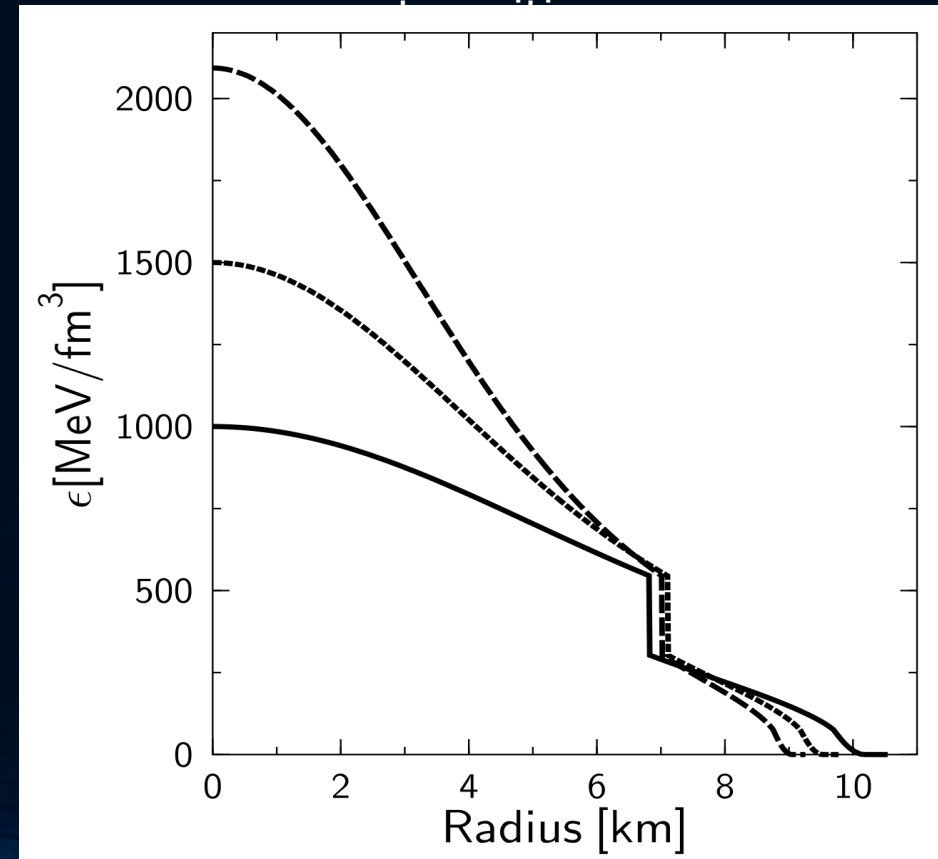


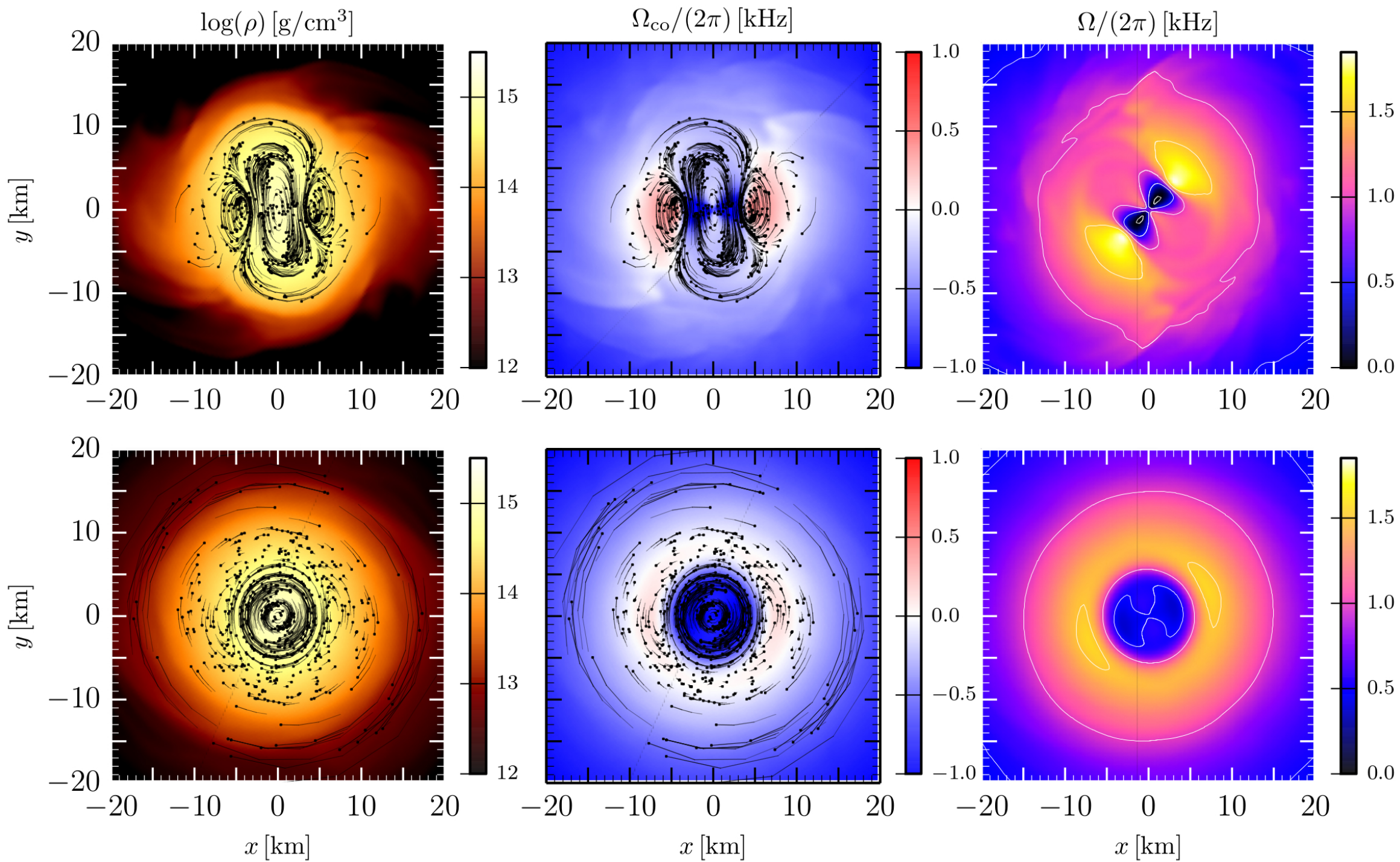
# The Maxwell Construction

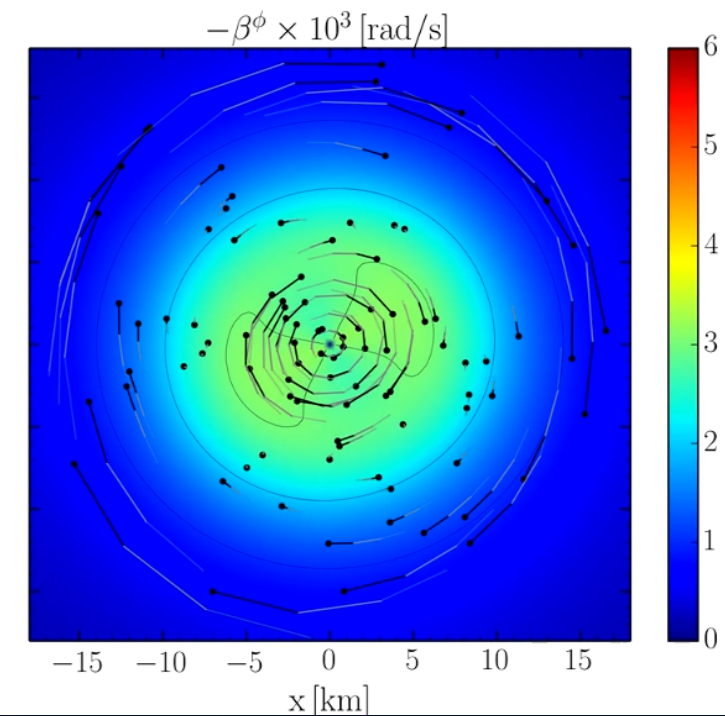
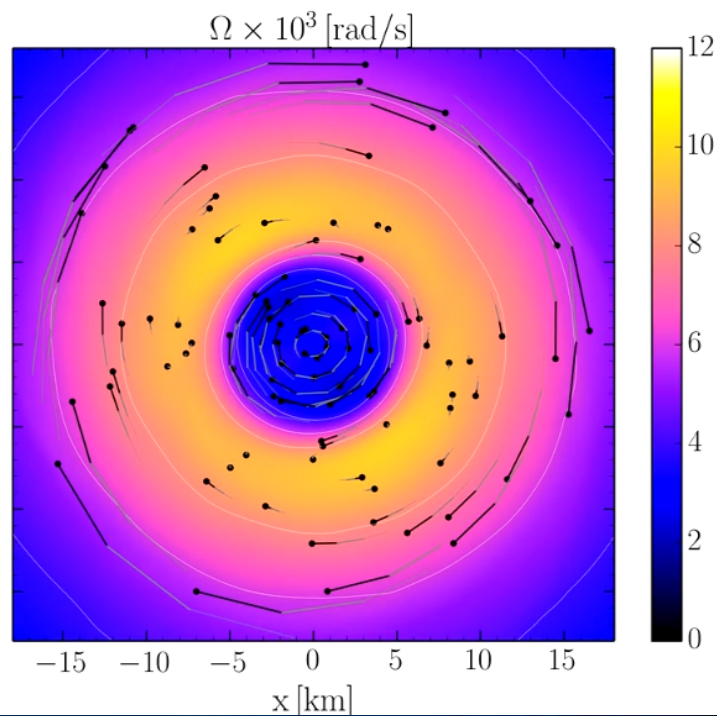
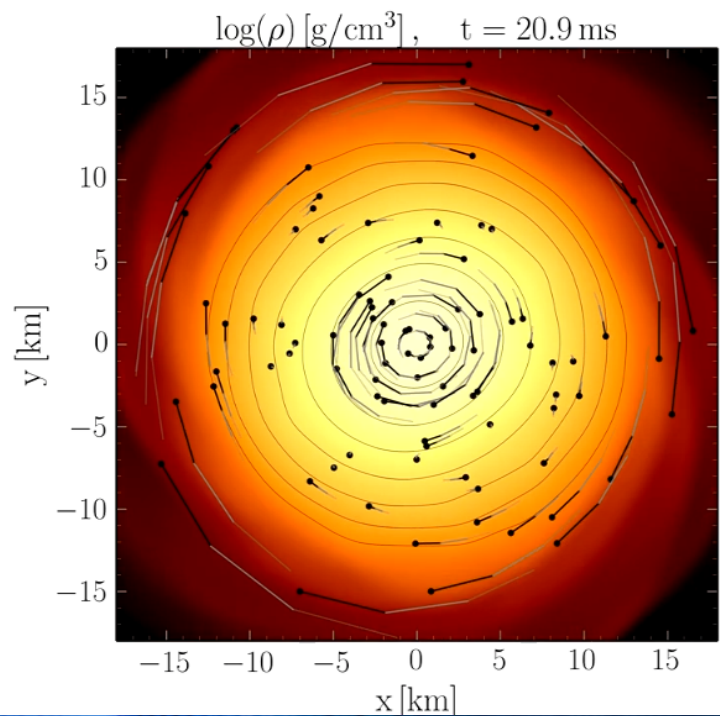
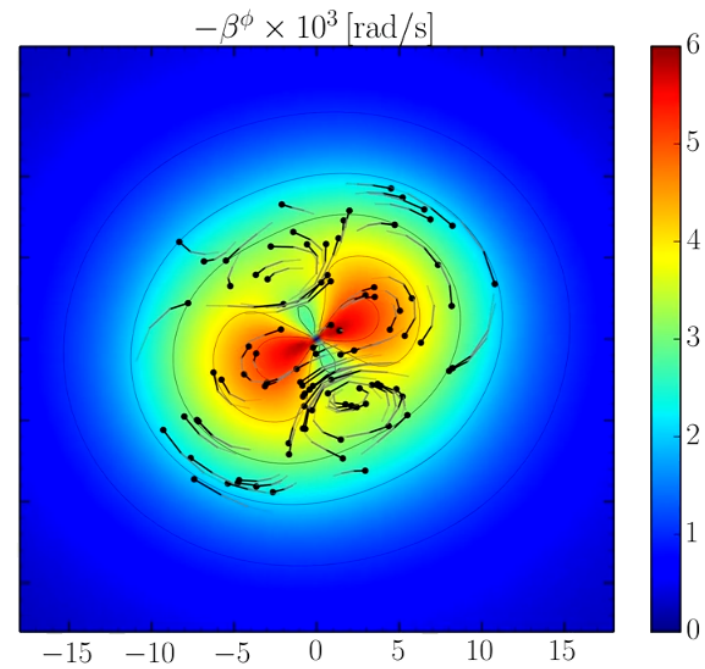
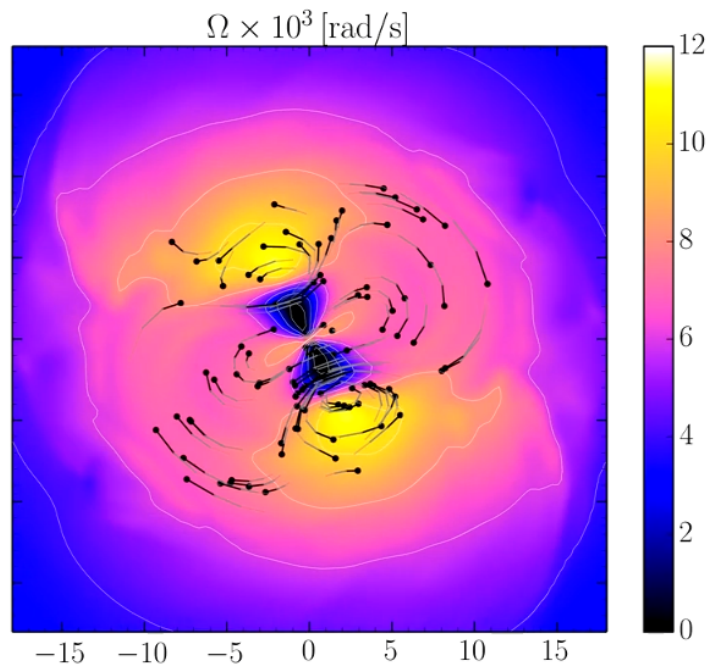
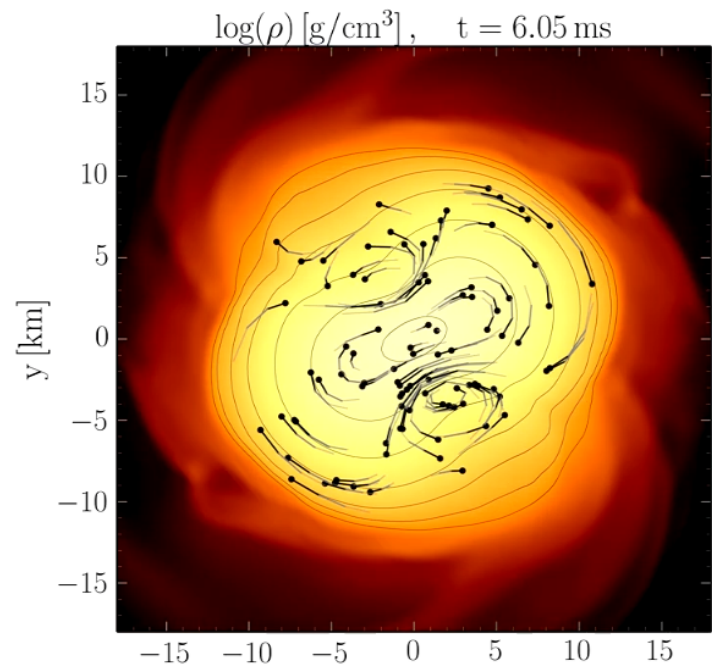
If the surface tension between the hadron and quark phase is large, the mixed phase could completely disappear -> sharp boundary between hadronic and quark. The Hadron-quark phase transition is then described using a Maxwell construction.



Pressure and baryon chemical potential stays constant, while the density and the charge chemical potential jump discontinuously during the phase





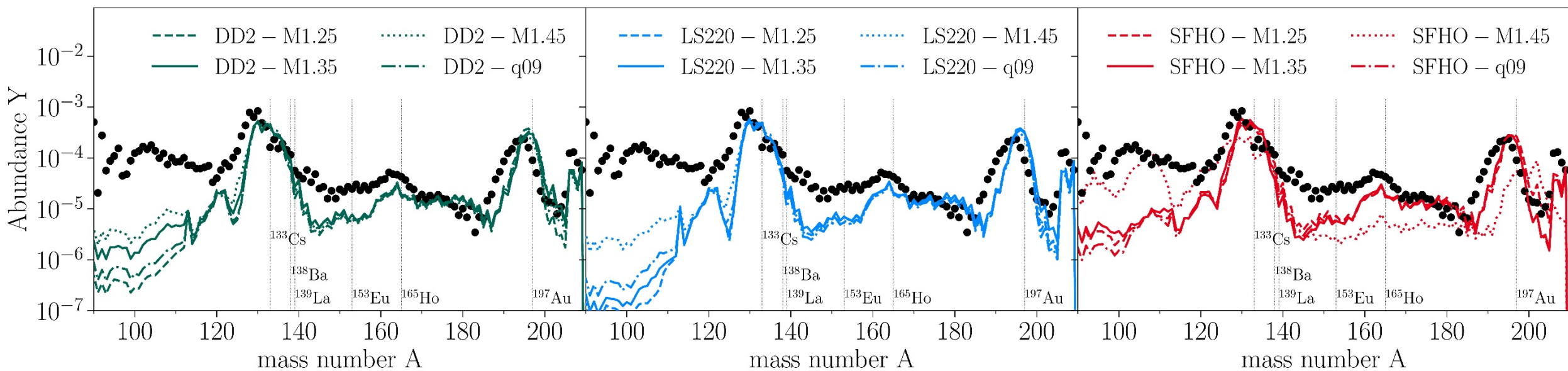
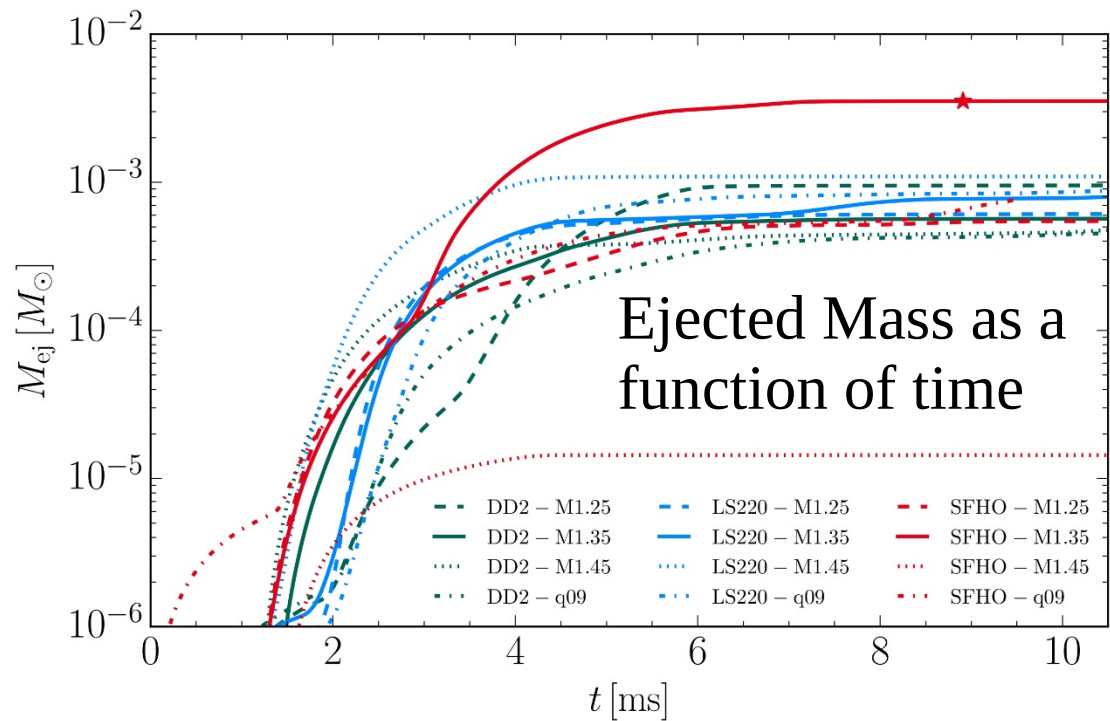


# r-process nucleosynthesis in binary neutron star mergers







Luke Bovard, Dirk Martin, Federico Guercilena, Almudena Arcones, Luciano Rezzolla and Oleg Korobkin

arXiv:1709.09630v1 [gr-qc] 27 Sep 2017

Simulation of the relative abundances of heavy elements produced in a binary neutron star merger.



# The Origin of the Solar System Elements

1 H	big bang fusion 										cosmic ray fission 					2 He						
3 Li	4 Be	merging neutron stars? 										exploding massive stars 					5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg	dying low mass stars 										exploding white dwarfs 					13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr					
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe					
55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn					
87 Fr	88 Ra																					
		57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu						
		89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	Very radioactive isotopes; nothing left from stars														

Graphic created by Jennifer Johnson  
<http://www.astronomy.ohio-state.edu/~jaj/nucleo/>

Astronomical Image Credits:  
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# Merger Product from an eccentric colliding Neutron Star Binaries

