



Jets in QCD media: From Coherence to Decoherence

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In collaboration with C. Salgado and K. Tywoniuk

arXiv:1009.2965, arXiv:1102.4317 [hep-ph]

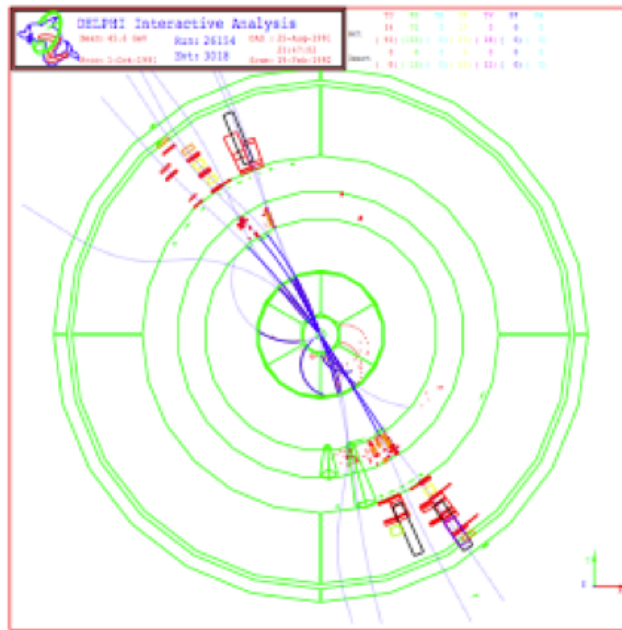
Excited QCD 2011

20-25 February

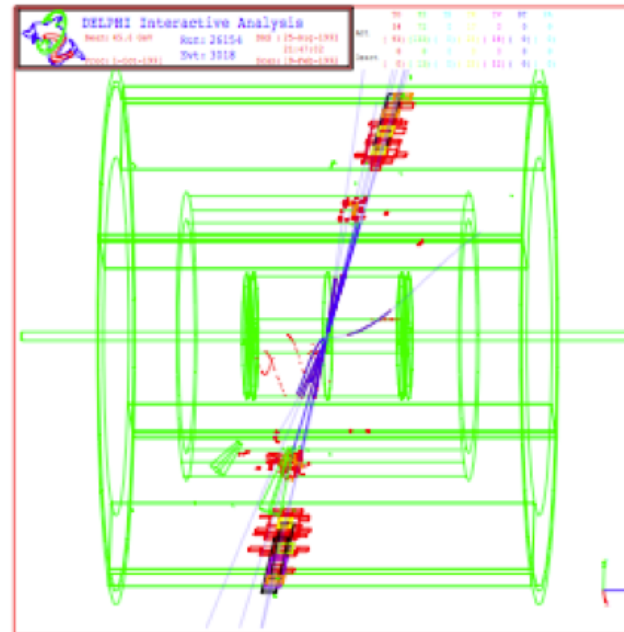
Ecole des Houches

What is a Jet?

“A collimated and energetic bunch of hadrons produced in a hard process”



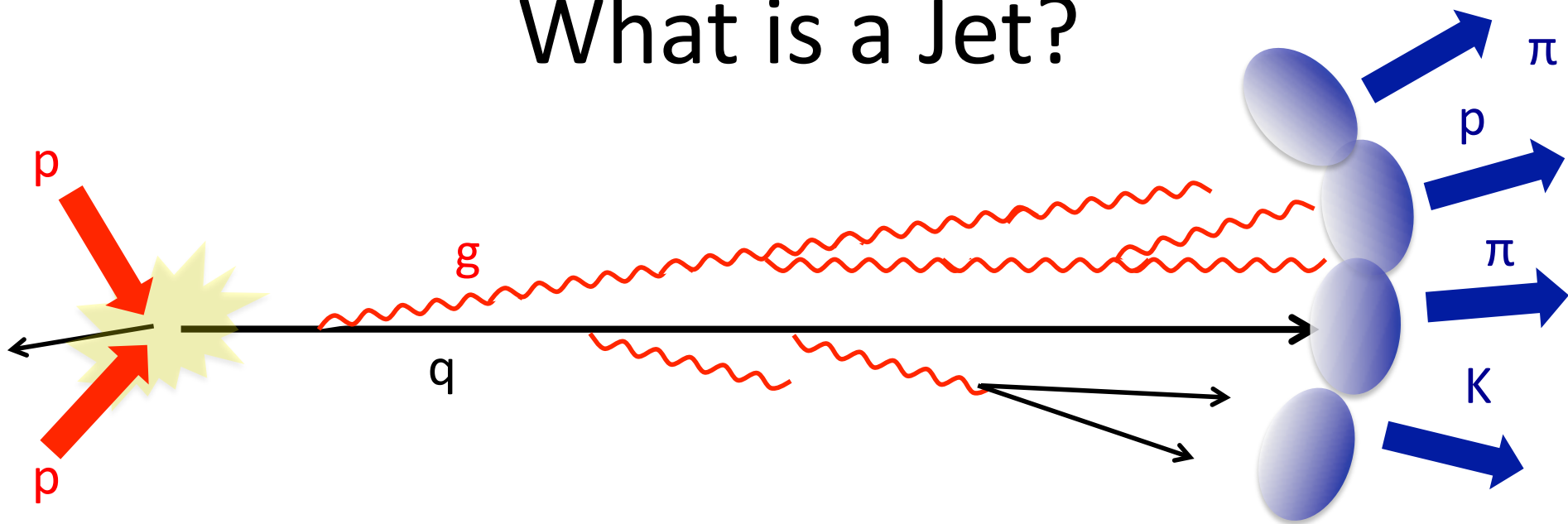
x-y plane



z-y plane

[2-jet event at LEP]

What is a Jet?

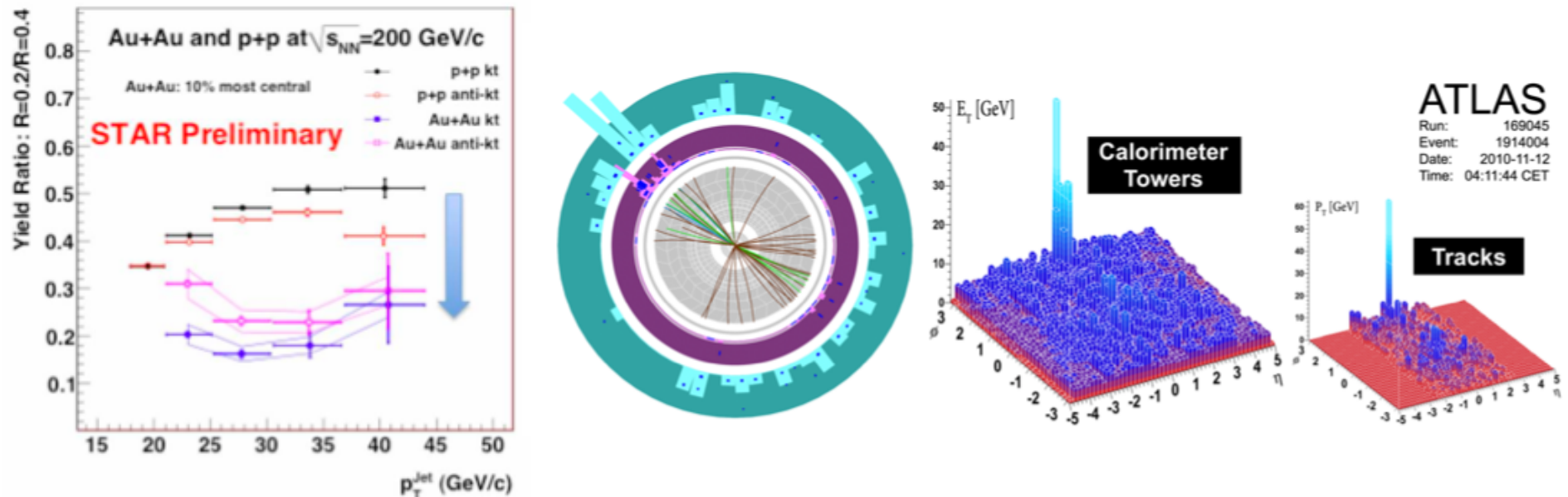


- Originally a jet is born as a **hard parton** (quark/gluon) which fragments into many partons when the time goes by with decreasing virtuality down to a non-perturbative scale where **hadronization** takes place
- Parton shower is well described within pQCD
- **LPHD**: Hadronization does not affect exclusive observables: Jet shape, energy distribution, etc.

How about jets in HIC?

- Jets in vacuum is a “*fine tuned technology*”. Once the hard parton is produced it fragments in **vacuum** without any further interaction in the final state as an **independent object** : energy and charge conservation, etc.
- With **HIC**: Jets do not propagate in vacuum but instead traverse a hot and **colored** (partonic) **medium** produced after the collision.

First jet measurements @ RHIC, LHC



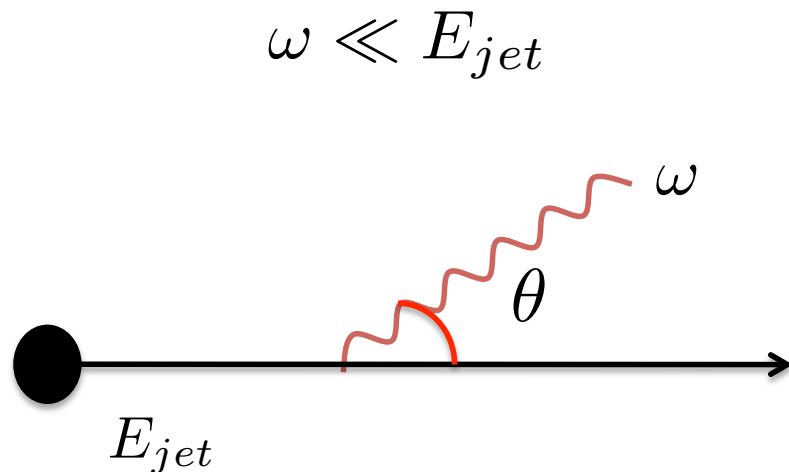
- Qualitative features: energy conservation not ensured, Jets in HIC are broader (less collimated).
- Issue: **Need for theoretical control!** To probe and characterize the produced **QGP**

Jets in vacuum (basics)

Dynamics of an energetic parton produced in a hard collision

- QCD bremsstrahlung : an accelerated charge radiates soft gluons

Double logarithmic divergence (DLA): **collinear and soft**



$$dN \propto \alpha_S \frac{d\omega}{\omega} \frac{d\theta}{\theta} \rightarrow \alpha_S \ln^2 E_{jet}$$

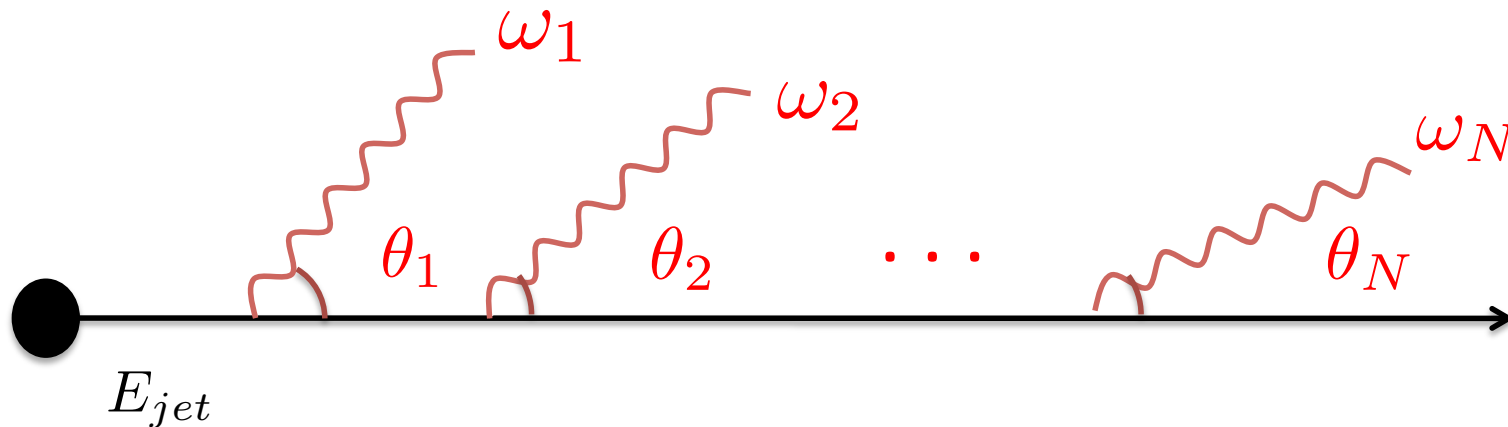
What happens when $\alpha_S \ln^2 E_{jet} \sim \mathcal{O}(1)$?

QCD coherence

- ✓ DLA: Successive gluon emissions are ordered in energies and angles

$$E_{jet} \gg \omega_1 \gg \dots \gg \omega_N$$

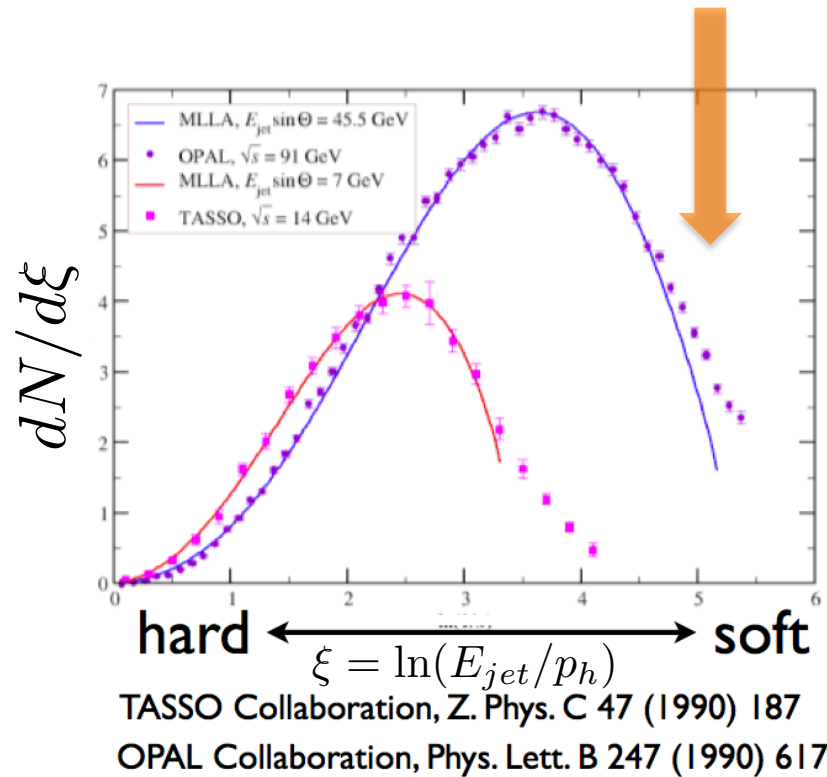
$$\theta_1 \gg \theta_2 \gg \dots \gg \theta_N$$



- ✓ MLLA: energy conservation, running of the coupling, etc.

DLA: Let's have a closer look...

QCD coherence leads to the depletion of soft gluons!



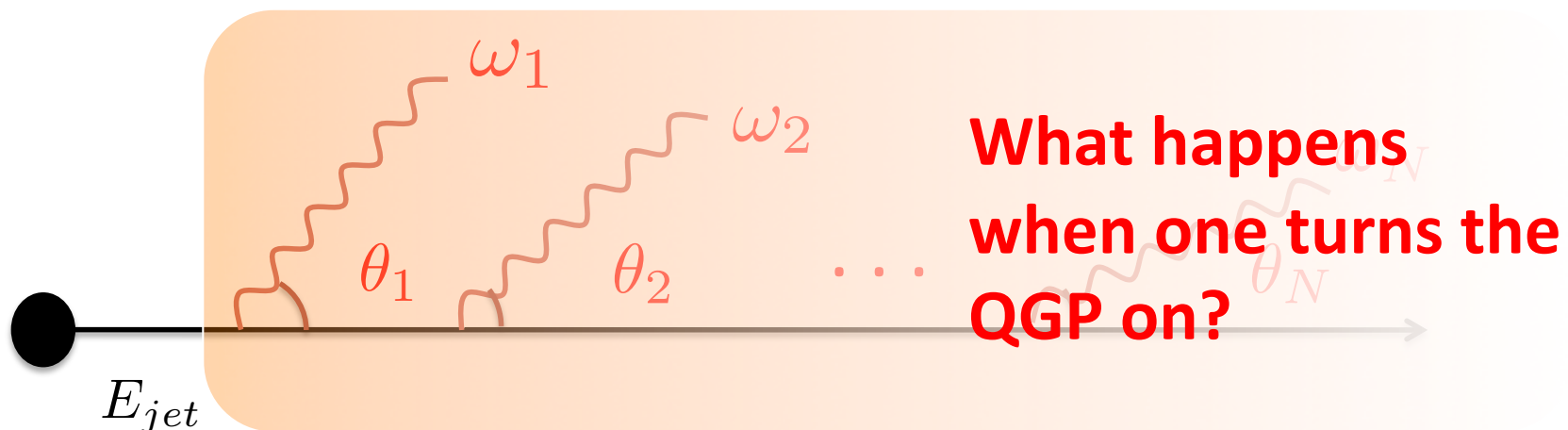
The “Hump-backed” plateau

QCD coherence

- ✓ Successive gluon emissions are ordered in **energy** and **angle**

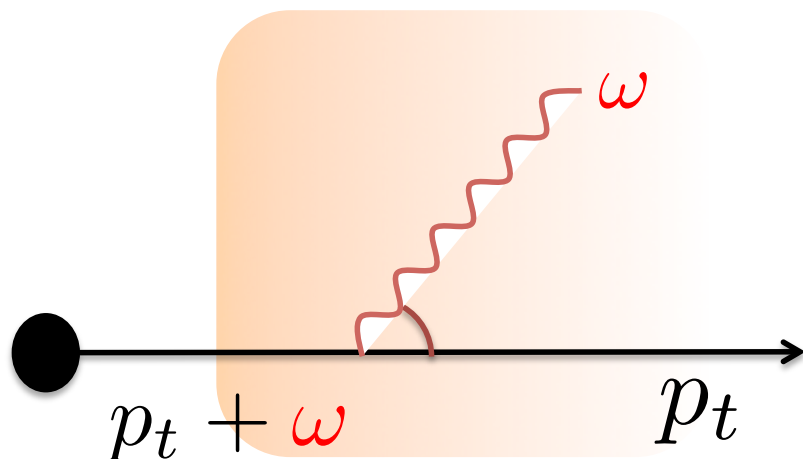
$$E_{jet} \gg \omega_1 \gg \dots \gg \omega_N$$

$$\theta_1 \gg \theta_2 \gg \dots \gg \theta_N$$



From Jet-Quenching to Jets?

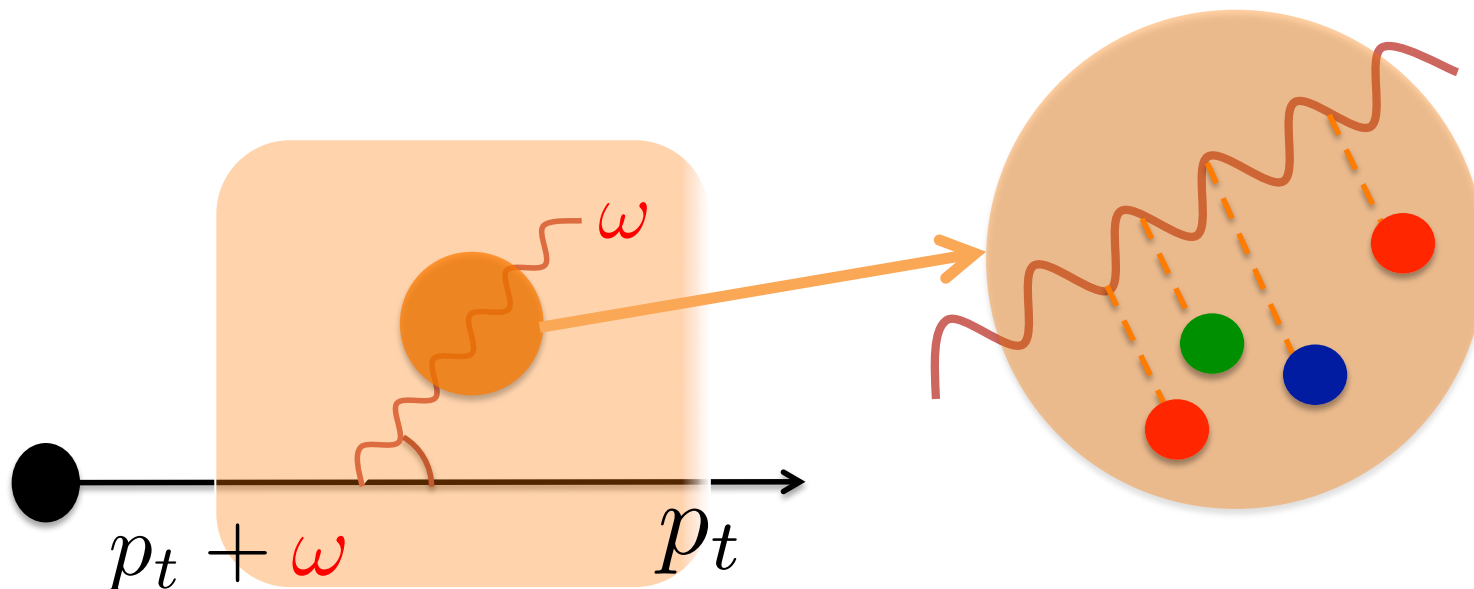
- Radiative parton energy loss: inclusive 1-gluon spectrum
- Remember! Need 2 gluon emissions to see QCD coherence (angular-ordering)



The hard quark loses energy by medium-induced gluon radiation

From Jet-Quenching to Jets?

- Radiative parton energy loss: inclusive 1-gluon spectrum.
- The emitted gluon undergoes multiple scattering in the medium (BDMPS-ZW-GLV picture (1997-2001))



Collinear and infrared finite spectrum!

QCD coherence in medium

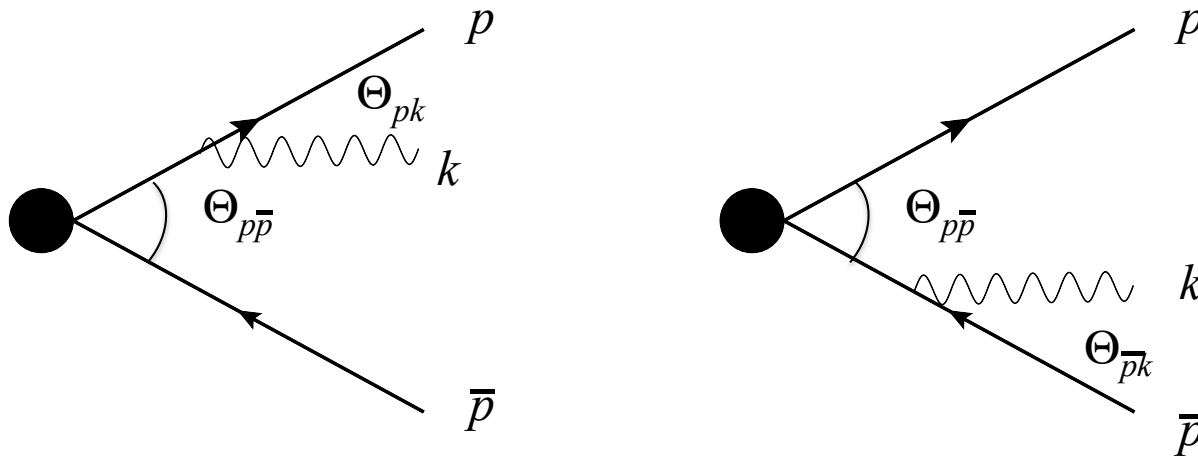
A missing piece...

- **On the market:** in-medium jet calculus are performed by enhancing the vacuum emission by the BDMPS/GLV spectrum: **No coherence!**

[QPYTHIA, QHERWIG, JEWEL...]

- Are medium modified jets mainly determined by the BDMPS/GLV radiation pattern?
- We know from studying the gluon cascade in vacuum that the **1-gluon emission spectrum is not enough** to build up the N-gluon cascade: **Interferences, angular ordering**, etc, play a role at higher orders

A simple exercise: QCD coherence from the quark-antiquark antenna



- Probabilistic interpretation $dN = dN_q + dN_{\bar{q}}$

$$dN_q \propto \alpha_s \frac{d\omega}{\omega} \frac{d\theta_{pk}}{\theta_{pk}} \Theta(\theta_{p\bar{p}} - \theta_{pk}),$$

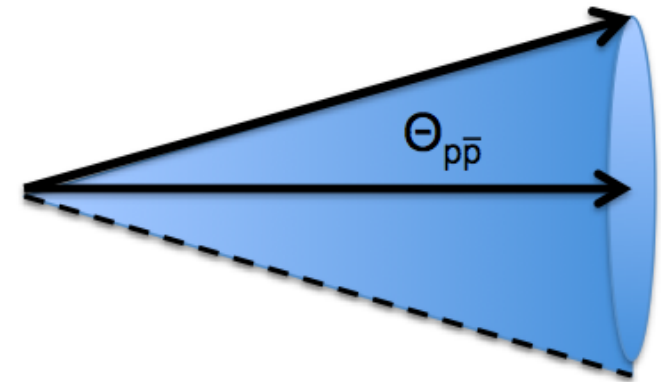
- Quantum interferences lead to a probabilistic picture!

A simple exercise: QCD coherence from the quark-antiquark antenna

- Radiation off the quark (dN_q)
- No radiation outside the cone
- **Why?**

gluons emitted at larger angles than the pair opening angle can not resolve the internal structure of the pair and thus are suppressed

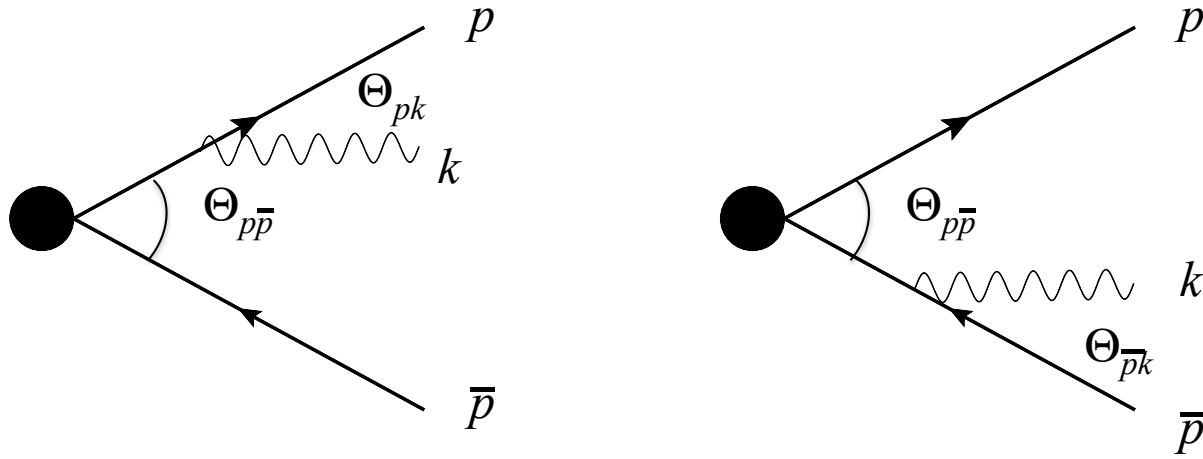
$$\lambda_{\perp} \sim \frac{1}{k_{\perp}} \sim t_{form} \theta > t_{form} \theta_{p\bar{p}} = r_{\perp}$$



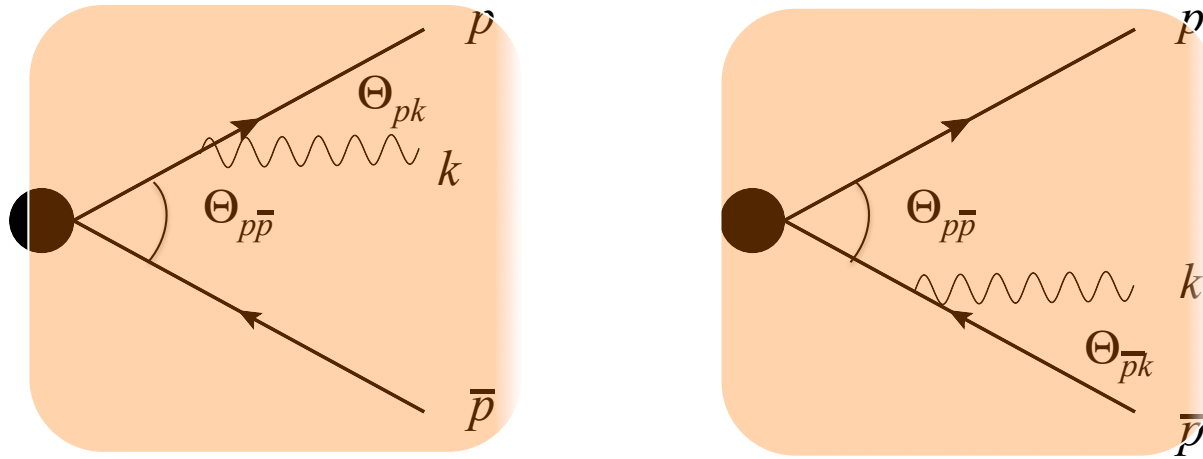
Angular ordering in vacuum

$$(t_{form} = \omega/k_{\perp}^2)$$

A simple exercise: QCD coherence from the quark-antiquark antenna

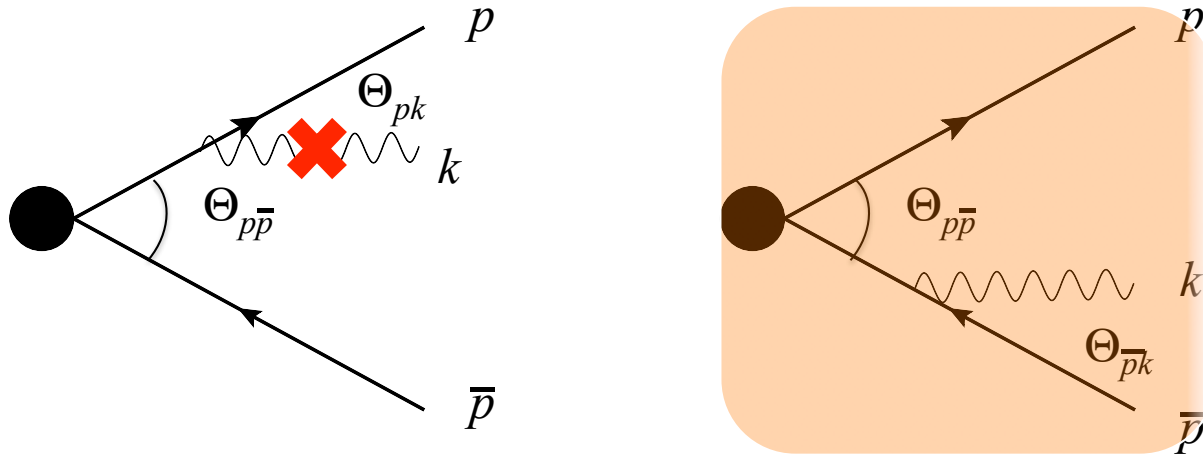


A simple exercise: QCD coherence from the quark-antiquark antenna



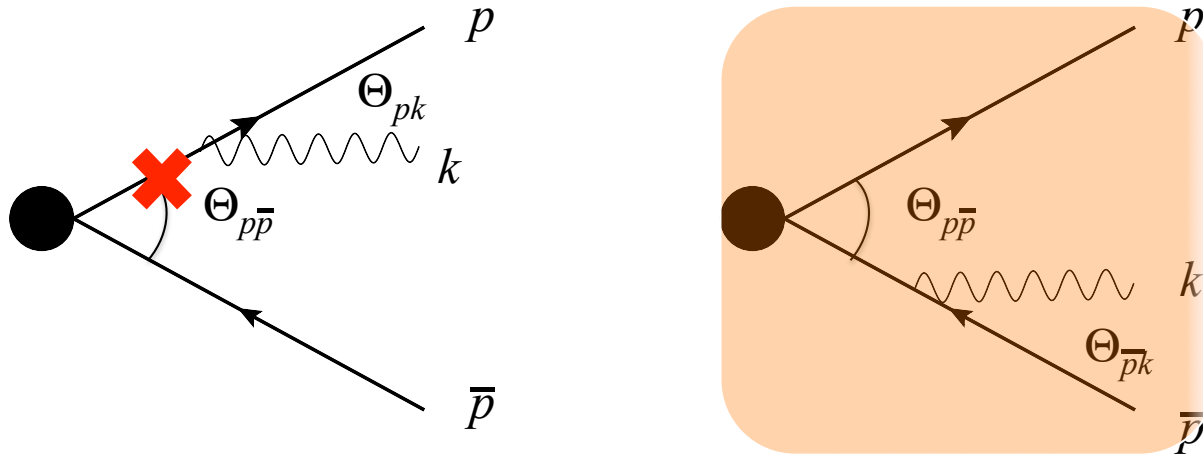
- Let's switch on the medium

A simple exercise: QCD coherence from the quark-antiquark antenna



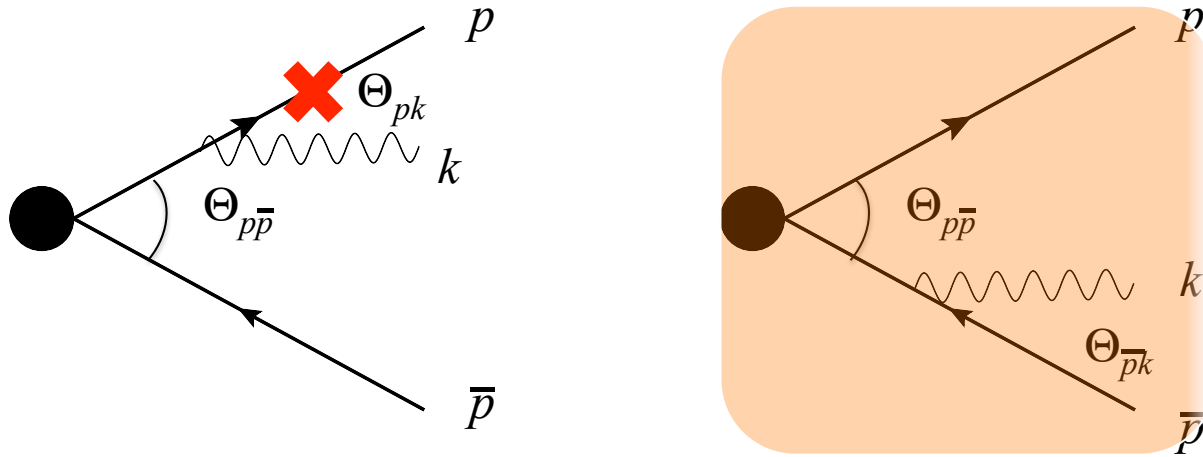
- Let's switch on the medium
- single interaction: **one gluon exchange** with the medium

A simple exercise: QCD coherence from the quark-antiquark antenna



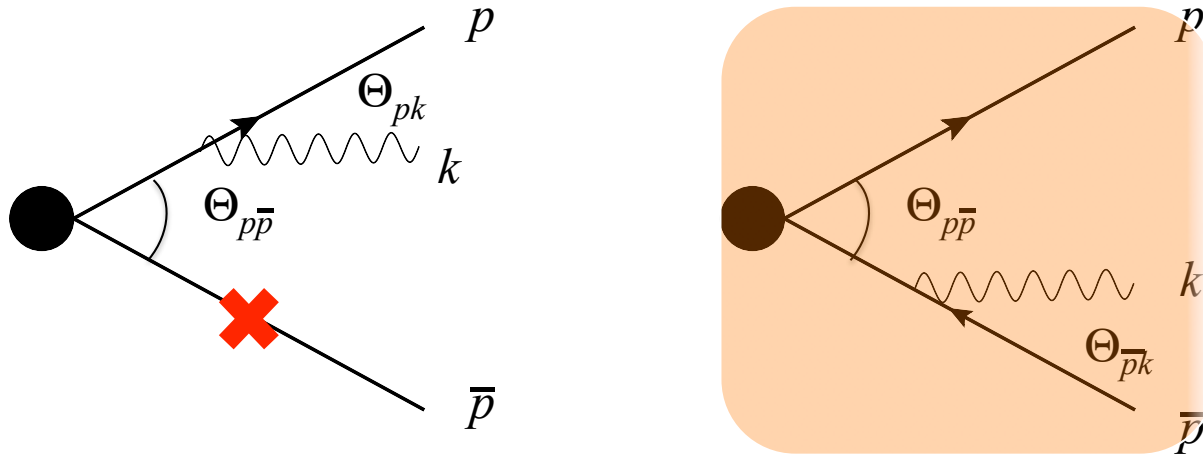
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A simple exercise: QCD coherence from the quark-antiquark antenna



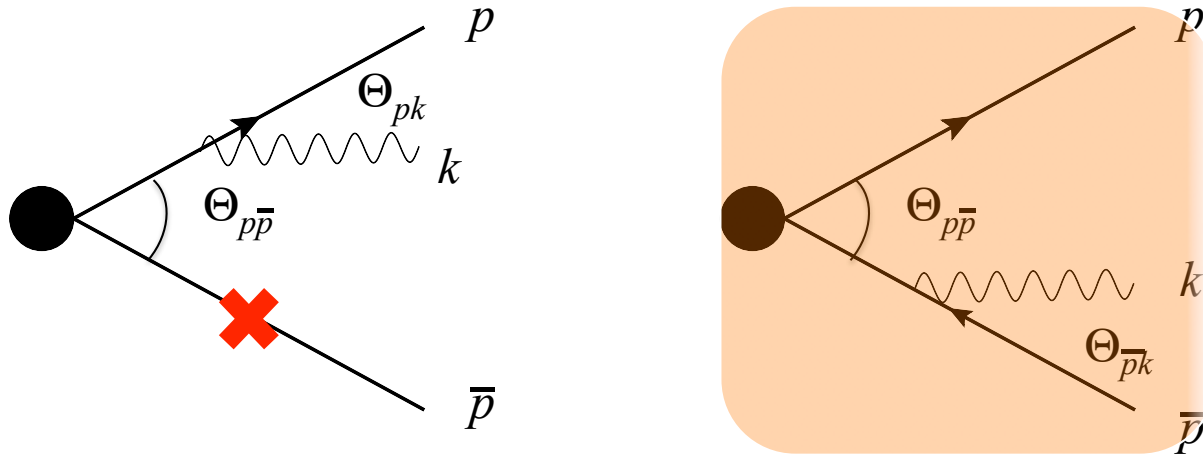
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A simple exercise: QCD coherence from the quark-antiquark antenna



- Let's switch on the medium
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A simple exercise: QCD coherence from the quark-antiquark antenna



- Let's switch on the medium
- single interaction: **one gluon exchange** with the medium
- **QGP**: classical background field $A_0^\mu(\vec{x})$

Classical picture: Yang-Mills equations

- **Input:** the classical current $J_{pair} = J_q + J_{\bar{q}}$

$$J_q^\mu = g \frac{p^\mu}{E} \delta^{(3)}(\vec{x} - \frac{\vec{p}}{E}t) \Theta(t) C^a t^a$$

- **limit:** $E \rightarrow \infty$, $\theta_{p\bar{p}} \rightarrow 0$, **gauge:** $A^+ = 0$

- The gluon radiation amplitude off the quark

$$\mathcal{M}_{1(q)}^{i,a} = ig^2 f^{abc} C^c \int \frac{d^2 q_\perp}{(2\pi)^2} \int_{t_1}^{t_2} dt \mathcal{A}_0^b(t, \mathbf{q}_\perp) \left[\frac{\nu_\perp^i}{p \cdot v} \left(1 - e^{i \frac{p \cdot v}{E} t}\right) + \frac{\kappa_\perp^i}{p \cdot k} e^{i \frac{p \cdot v}{E} t} \right]$$

q_\perp Is the quark-medium momentum exchange

- where

$$v \equiv \left(k^+, \frac{(\mathbf{k} - \mathbf{q})_\perp^2}{2k^+}, (k - q)^i \right)$$

$$\nu_\perp = \frac{p^+}{k^+} (\mathbf{k} - \mathbf{q})_\perp - \mathbf{p}_\perp$$

$$\kappa_\perp = \frac{p^+}{k^+} \mathbf{k}_\perp - \mathbf{p}_\perp$$

Classical picture: Yang-Mills equations

- The gluon radiation amplitude off the quark

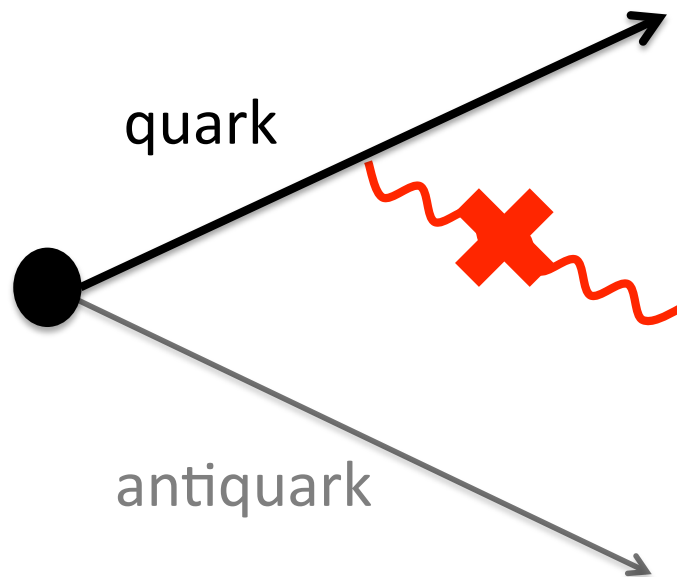
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gluon interaction with
the medium

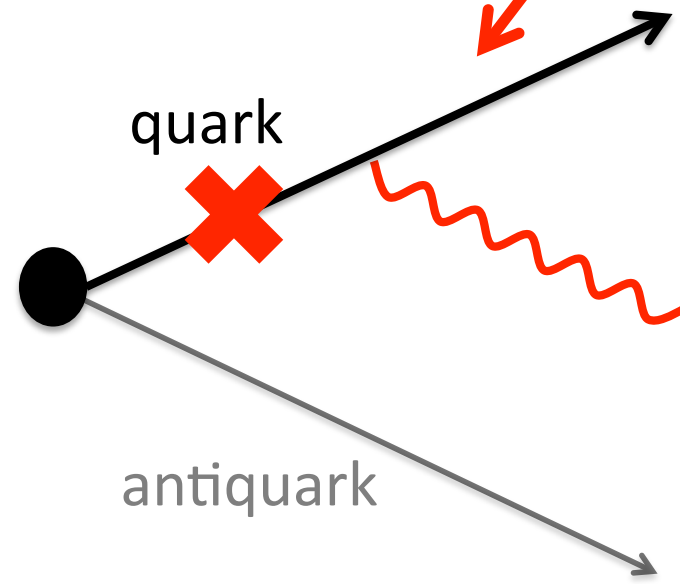
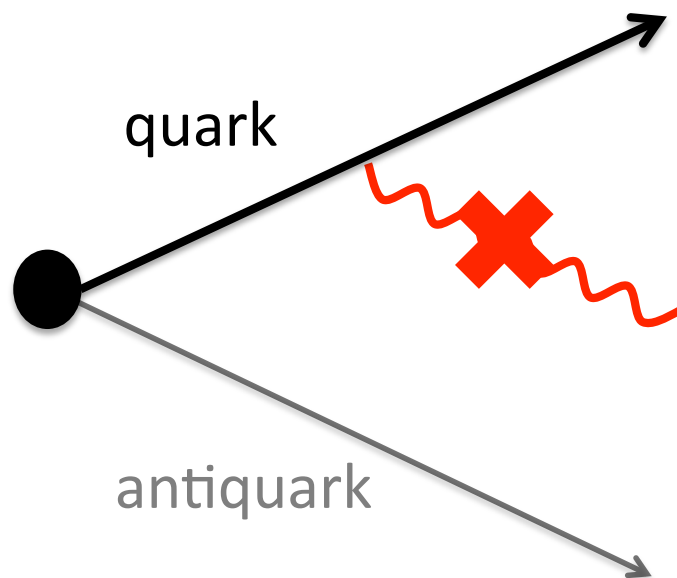


Classical picture: Yang-Mills equations

- The gluon radiation amplitude off the quark

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gluon bremsstrahlung

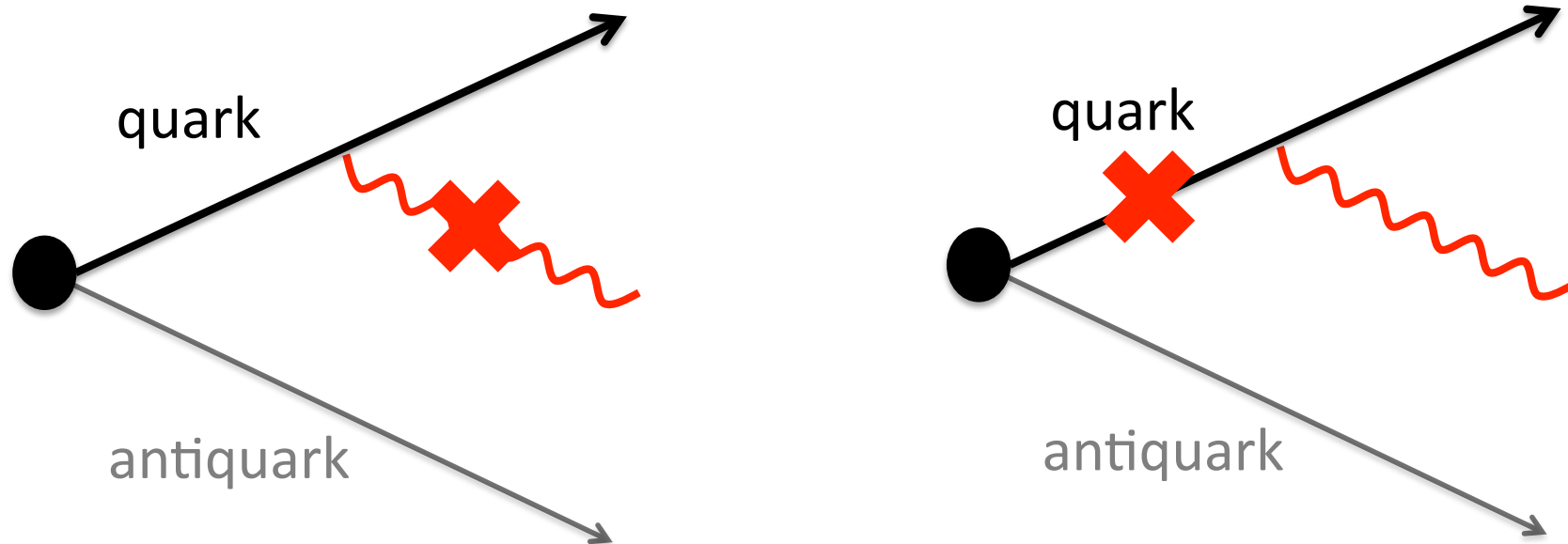


Classical picture: Yang-Mills equations

- The gluon radiation amplitude off the quark

$$\mathcal{M}_{1(q)}^{i,a} = ig^2 f^{abc} C^c \int \frac{d^2 q_{\perp}}{(2\pi)^2} \int_{t_1}^{t_2} dt \mathcal{A}_0^b(t, \mathbf{q}_{\perp}) \left[\frac{\mathbf{v}_{\perp}^i}{p \cdot v} \left(1 - e^{i \frac{p \cdot v}{E} t} \right) + \frac{\mathbf{\kappa}_{\perp}^i}{p \cdot k} e^{i \frac{p \cdot v}{E} t} \right]$$

Similarly for the antiquark



Induced gluon radiation spectrum

- Squaring the amplitude

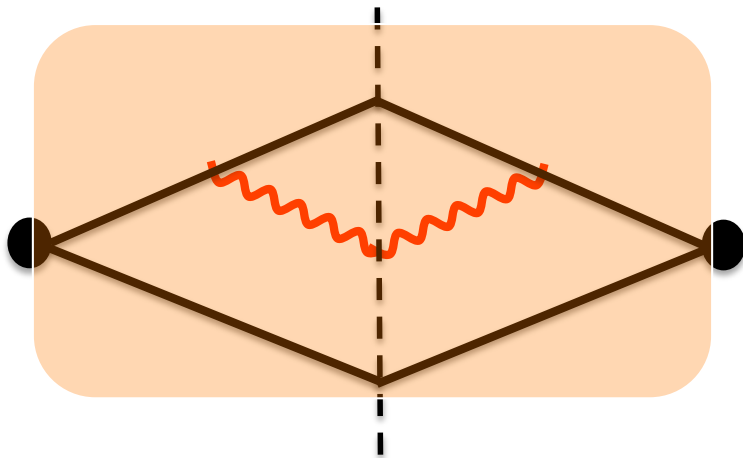
$$|\mathcal{M}|^2 \equiv |\mathcal{M}_q + \mathcal{M}_{\bar{q}}|^2 = |\mathcal{M}_q|^2 + |\mathcal{M}_{\bar{q}}|^2 + 2\text{Re}\mathcal{M}_q\mathcal{M}_{\bar{q}}^*$$

Induced gluon radiation spectrum

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BDMPS/GLV (1-scattering)

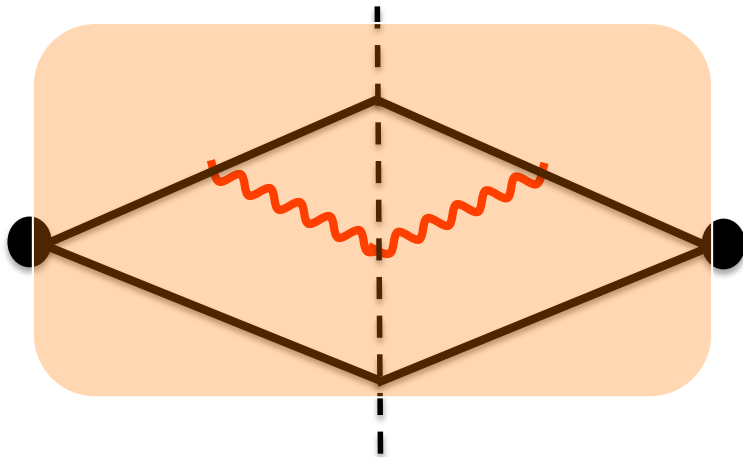


Induced gluon radiation spectrum

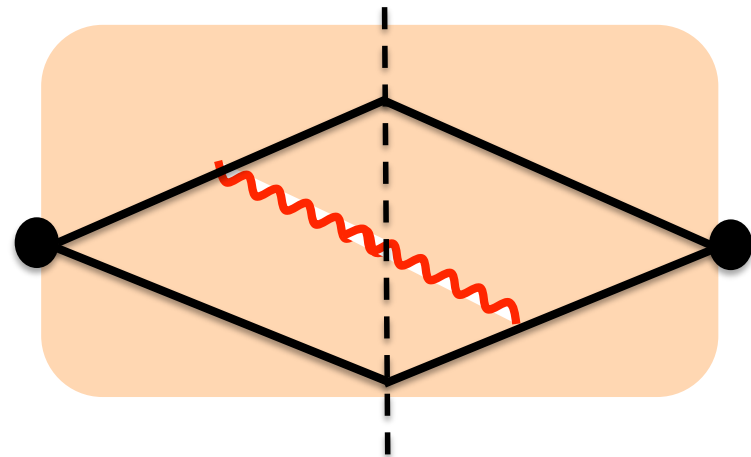
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BDMPS/GLV (1-scattering)



Interference term

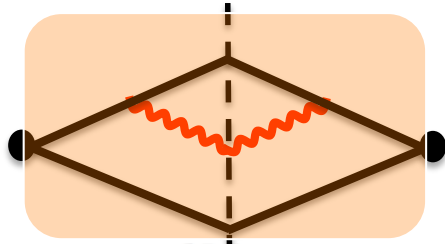


The spectrum

$$\begin{aligned}
 (2\pi)^2 E \frac{dN}{d^3k} &= 8\pi C_A C_F \alpha_s^2 \int \frac{d^2 \mathbf{q}_\perp}{(2\pi)^2} \int_0^L dt n(t) \mathcal{V}(\mathbf{q}_\perp) \\
 &\left[\left(\frac{\boldsymbol{\nu}_\perp^2}{(p \cdot v)^2} - \frac{\boldsymbol{\nu}_\perp \cdot \boldsymbol{\kappa}_\perp}{(p \cdot v)(p \cdot k)} \right) (1 - \cos \Omega_1 t) \right. \\
 &+ \left(\frac{\bar{\boldsymbol{\nu}}_\perp^2}{(\bar{p} \cdot v)^2} - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(\bar{p} \cdot v)(\bar{p} \cdot k)} \right) (1 - \cos \Omega_2 t) \\
 &- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\nu}}_\perp}{(p \cdot v)(\bar{p} \cdot v)} (1 + \cos \Omega_{12} t - \cos \Omega_1 t - \cos \Omega_2 t) \\
 &- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot v)(\bar{p} \cdot k)} (\cos \Omega_2 t - \cos \Omega_{12} t) - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \boldsymbol{\kappa}_\perp}{(\bar{p} \cdot v)(p \cdot k)} (\cos \Omega_1 t - \cos \Omega_{12} t) \\
 &\left. - \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} (\cos \Omega_{12} t - 1) \right]
 \end{aligned}$$

where

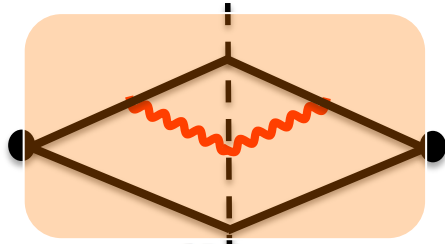
$$\Omega_1 = \frac{p \cdot v}{E}, \quad \Omega_2 = \frac{\bar{p} \cdot v}{\bar{E}}, \quad \Omega_{12} = \Omega_1 - \Omega_2$$



The spectrum

GLV (quark)

$$\begin{aligned}
 (2\pi)^2 E \frac{dN}{d^3k} &= 8\pi C_A C_F \alpha_s^2 \int \frac{d^2 \mathbf{q}_\perp}{(2\pi)^2} \int_0^L dt n(t) \mathcal{V}(\mathbf{q}_\perp) \\
 &\left[\left(\frac{\boldsymbol{\nu}_\perp^2}{(p \cdot v)^2} - \frac{\boldsymbol{\nu}_\perp \cdot \boldsymbol{\kappa}_\perp}{(p \cdot v)(p \cdot k)} \right) (1 - \cos \Omega_1 t) \right. \\
 &+ \left(\frac{\bar{\boldsymbol{\nu}}_\perp^2}{(\bar{p} \cdot v)^2} - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(\bar{p} \cdot v)(\bar{p} \cdot k)} \right) (1 - \cos \Omega_2 t) \\
 &- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\nu}}_\perp}{(p \cdot v)(\bar{p} \cdot v)} (1 + \cos \Omega_{12} t - \cos \Omega_1 t - \cos \Omega_2 t) \\
 &- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot v)(\bar{p} \cdot k)} (\cos \Omega_2 t - \cos \Omega_{12} t) - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \boldsymbol{\kappa}_\perp}{(\bar{p} \cdot v)(p \cdot k)} (\cos \Omega_1 t - \cos \Omega_{12} t) \\
 &\left. - \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} (\cos \Omega_{12} t - 1) \right]
 \end{aligned}$$



The spectrum

$$(2\pi)^2 E \frac{dN}{d^3k} = 8\pi C_A C_F \alpha_s^2 \int \frac{d^2 \mathbf{q}_\perp}{(2\pi)^2} \int_0^L dt n(t) \mathcal{V}(\mathbf{q}_\perp)$$

$$\left[\left(\frac{\boldsymbol{\nu}_\perp^2}{(p \cdot v)^2} - \frac{\boldsymbol{\nu}_\perp \cdot \boldsymbol{\kappa}_\perp}{(p \cdot v)(p \cdot k)} \right) (1 - \cos \Omega_1 t) \right.$$

$$+ \left(\frac{\bar{\boldsymbol{\nu}}_\perp^2}{(\bar{p} \cdot v)^2} - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(\bar{p} \cdot v)(\bar{p} \cdot k)} \right) (1 - \cos \Omega_2 t)$$

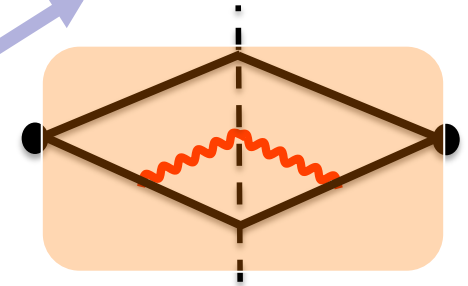
$$- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\nu}}_\perp}{(p \cdot v)(\bar{p} \cdot v)} (1 + \cos \Omega_{12} t - \cos \Omega_1 t - \cos \Omega_2 t)$$

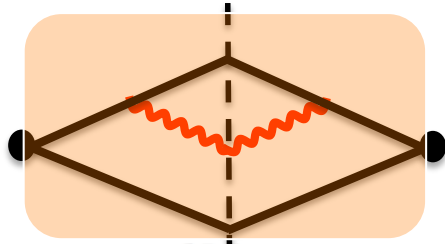
$$- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot v)(\bar{p} \cdot k)} (\cos \Omega_2 t - \cos \Omega_{12} t) - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \boldsymbol{\kappa}_\perp}{(\bar{p} \cdot v)(p \cdot k)} (\cos \Omega_1 t - \cos \Omega_{12} t)$$

$$\left. - \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} (\cos \Omega_{12} t - 1) \right]$$

GLV (quark)

GLV (antiquark)





The spectrum

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$$\left. + \left(\frac{\bar{\boldsymbol{\nu}}_\perp^2}{(\bar{p} \cdot v)^2} - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(\bar{p} \cdot v)(\bar{p} \cdot k)} \right) (1 - \cos \Omega_2 t) \right.$$

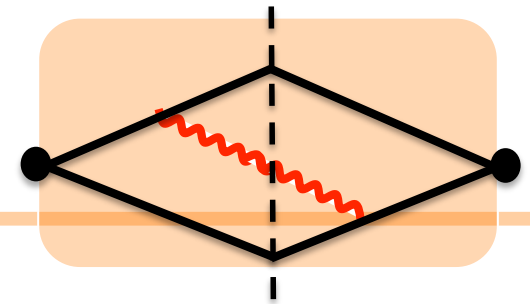
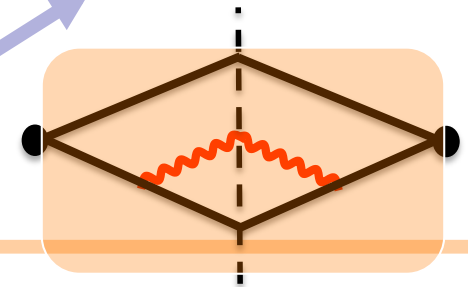
$$\left. - \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\nu}}_\perp}{(p \cdot v)(\bar{p} \cdot v)} (1 + \cos \Omega_{12} t - \cos \Omega_1 t - \cos \Omega_2 t) \right.$$

$$\left. - \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot v)(\bar{p} \cdot k)} (\cos \Omega_2 t - \cos \Omega_{12} t) - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \boldsymbol{\kappa}_\perp}{(\bar{p} \cdot v)(p \cdot k)} (\cos \Omega_1 t - \cos \Omega_{12} t) \right.$$

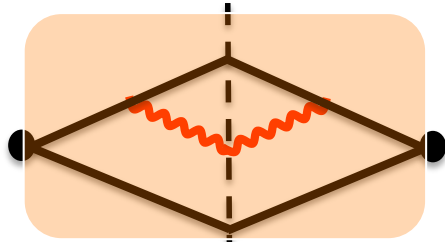
$$\left. - \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} (\cos \Omega_{12} t - 1) \right]$$

GLV (quark)

GLV (antiquark)



Interferences



The spectrum

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$$\left[\left(\frac{\boldsymbol{\nu}_\perp^2}{(p \cdot v)^2} - \frac{\boldsymbol{\nu}_\perp \cdot \boldsymbol{\kappa}_\perp}{(p \cdot v)(p \cdot k)} \right) (1 - \cos \Omega_1 t) \right]$$

$$+ \left(\frac{\bar{\boldsymbol{\nu}}_\perp^2}{(\bar{p} \cdot v)^2} - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(\bar{p} \cdot v)(\bar{p} \cdot k)} \right) (1 - \cos \Omega_2 t)$$

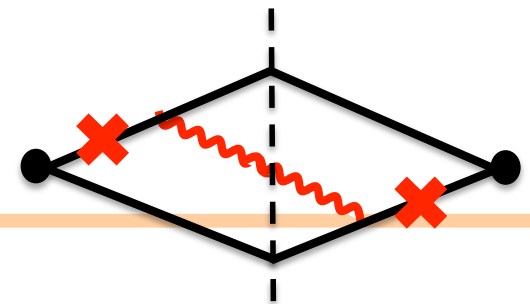
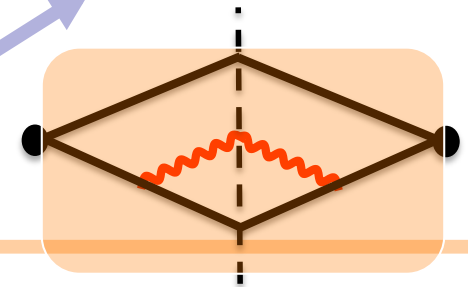
$$- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\nu}}_\perp}{(p \cdot v)(\bar{p} \cdot v)} (1 + \cos \Omega_{12} t - \cos \Omega_1 t - \cos \Omega_2 t)$$

$$- \frac{\boldsymbol{\nu}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot v)(\bar{p} \cdot k)} (\cos \Omega_2 t - \cos \Omega_{12} t) - \frac{\bar{\boldsymbol{\nu}}_\perp \cdot \boldsymbol{\kappa}_\perp}{(\bar{p} \cdot v)(p \cdot k)} (\cos \Omega_1 t - \cos \Omega_{12} t)$$

$$\left[- \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} (\cos \Omega_{12} t - 1) \right]$$

GLV (quark)

GLV (antiquark)



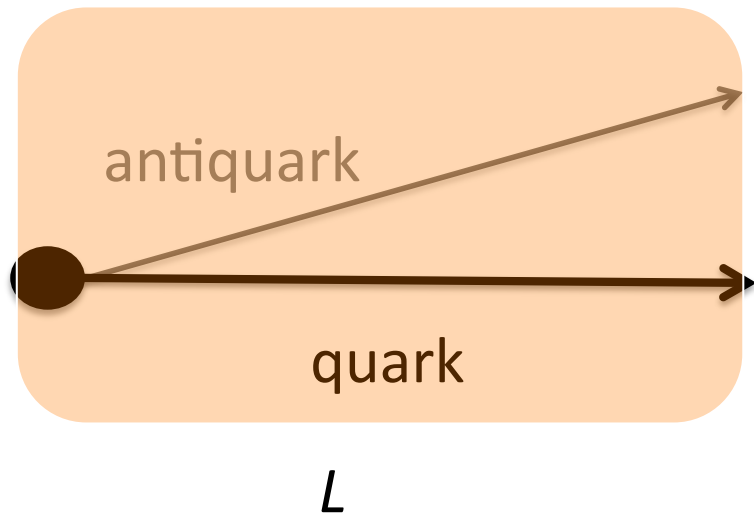
Interferences

Bremsstrahlung interference
(soft divergence)

The soft limit and anti-angular ordering

$\omega \rightarrow 0$, the quark on the z axis

$$(2\pi)^2 \omega \frac{dN^{\text{soft}}}{d^3k} \propto \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} \int_0^L dt \int \frac{d^2q_\perp}{(2\pi)^2} V(\mathbf{q}_\perp) \left(1 - \cos \frac{\bar{\mathbf{p}}_\perp \cdot \mathbf{q}_\perp}{\bar{E}} t\right)$$



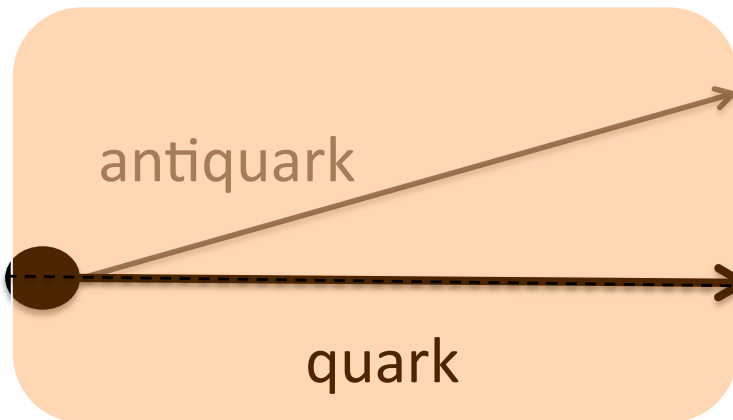
The soft limit and anti-angular ordering

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$$(2\pi)^2 \omega \frac{dN^{\text{soft}}}{d^3k} \propto \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} \int_0^L dt \int \frac{d^2q_\perp}{(2\pi)^2} V(\mathbf{q}_\perp) \left(1 - \cos \frac{\bar{\mathbf{p}}_\perp \cdot \mathbf{q}_\perp t}{\bar{E}}\right)$$

$$A_{\text{med}} \propto \hat{q} L r_\perp^2 \ln \frac{1}{r_\perp m_D}$$

→ Dipole scattering amplitude



$$r_\perp \equiv \frac{\bar{p}_\perp}{\bar{E}} L \approx \theta_{p\bar{p}} L$$

L

The soft limit and anti-angular ordering

$\omega \rightarrow 0$, the quark on the z axis

$$(2\pi)^2 \omega \frac{dN^{\text{soft}}}{d^3k} \propto \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} \int_0^L dt \int \frac{d^2q_\perp}{(2\pi)^2} V(\mathbf{q}_\perp) \left(1 - \cos \frac{\bar{\mathbf{p}}_\perp \cdot \mathbf{q}_\perp}{\bar{E}} t\right)$$

- Integrating over the azimuth

$$\frac{dN}{d\omega d\theta} \propto \frac{1}{\omega} \frac{\sin \theta}{1 - \cos \theta} \Theta(\cos \theta_{p\bar{p}} - \cos \theta) A_{\text{med}}(\theta_{p\bar{p}})$$

The soft limit and anti-angular ordering

$\omega \rightarrow 0$, the quark on the z axis

$$(2\pi)^2 \omega \frac{dN^{\text{soft}}}{d^3k} \propto \frac{\boldsymbol{\kappa}_\perp \cdot \bar{\boldsymbol{\kappa}}_\perp}{(p \cdot k)(\bar{p} \cdot k)} \int_0^L dt \int \frac{d^2q_\perp}{(2\pi)^2} V(\mathbf{q}_\perp) \left(1 - \cos \frac{\bar{\mathbf{p}}_\perp \cdot \mathbf{q}_\perp}{\bar{E}} t\right)$$

- Integrating over the azimuth

$$\frac{dN}{d\omega d\theta} \propto \frac{1}{\omega} \frac{\sin \theta}{1 - \cos \theta} \Theta(\cos \theta_{p\bar{p}} - \cos \theta) A_{\text{med}}(\theta_{p\bar{p}})$$

→ No emissions inside the pair!

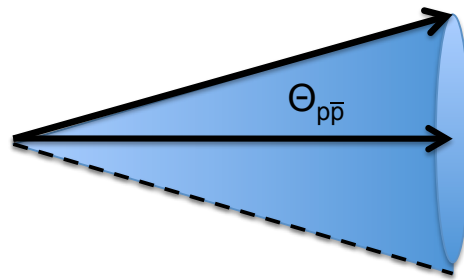
The soft limit and anti-angular ordering

- Soft divergence and **anti-angular ordering**
- vacuum+medium: ($\omega \rightarrow 0$)

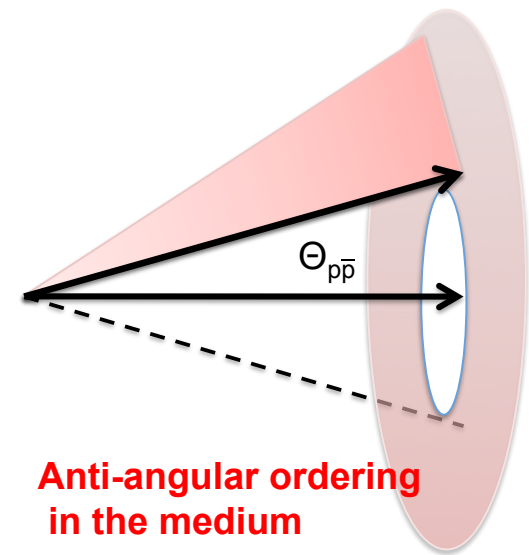
$$dN_q = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + A_{\text{med}}(\theta_{p\bar{p}}) \Theta(\cos \theta_{p\bar{p}} - \cos \theta)]$$

Vacuum emission:
inside the cone

Medium
emissions:
outside the cone



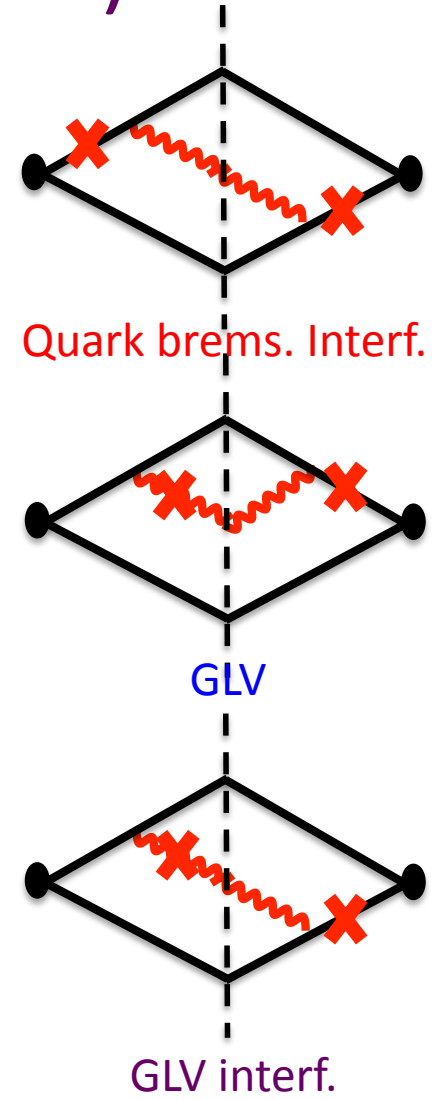
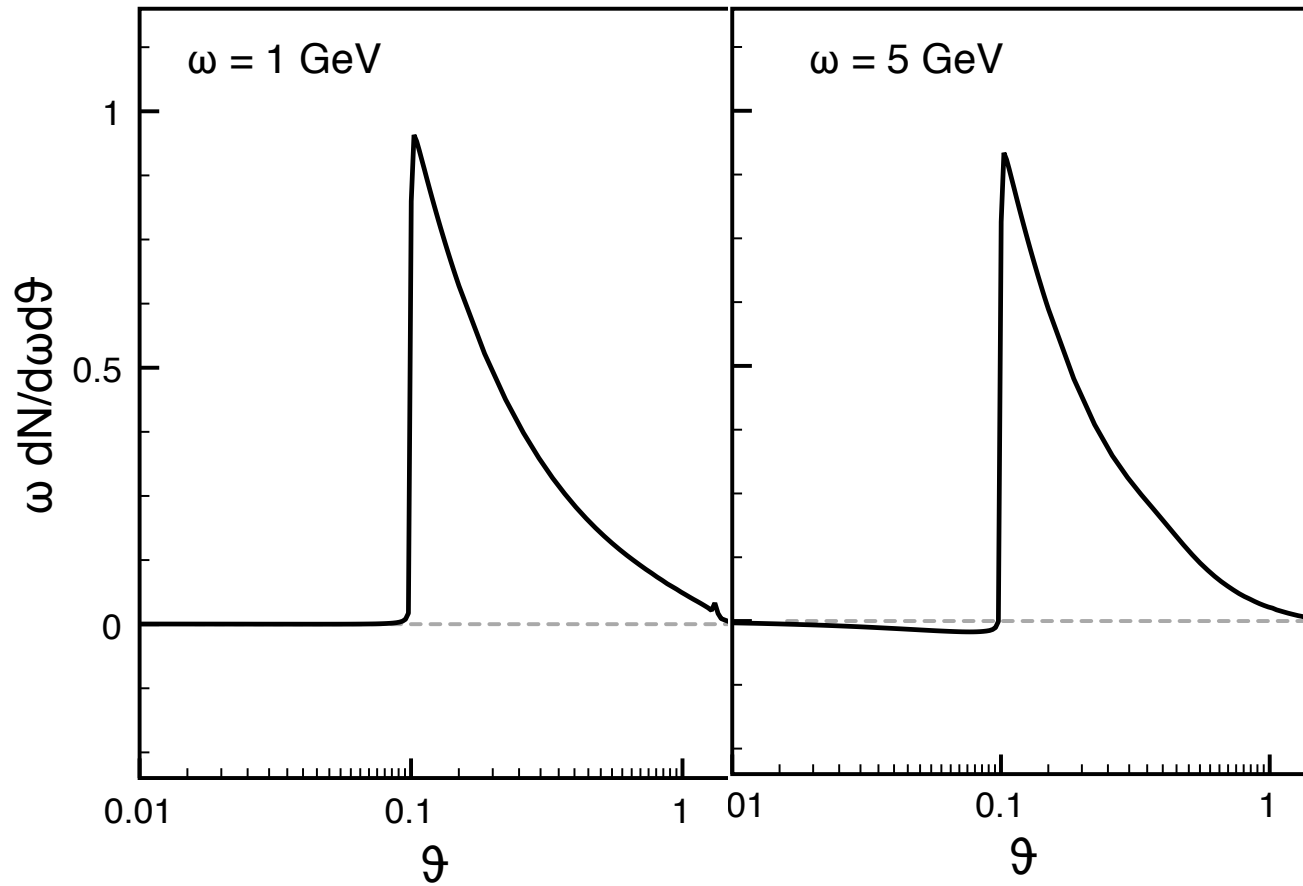
Angular ordering in vacuum



Anti-angular ordering
in the medium

Full spectrum (some numerics)

$L=20 \text{ GeV}^{-1} = 4 \text{ fm}$

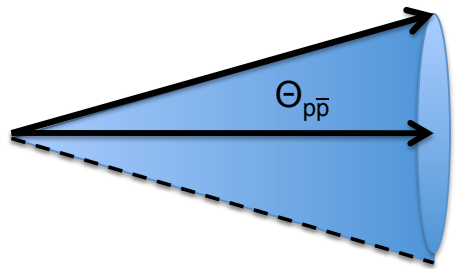
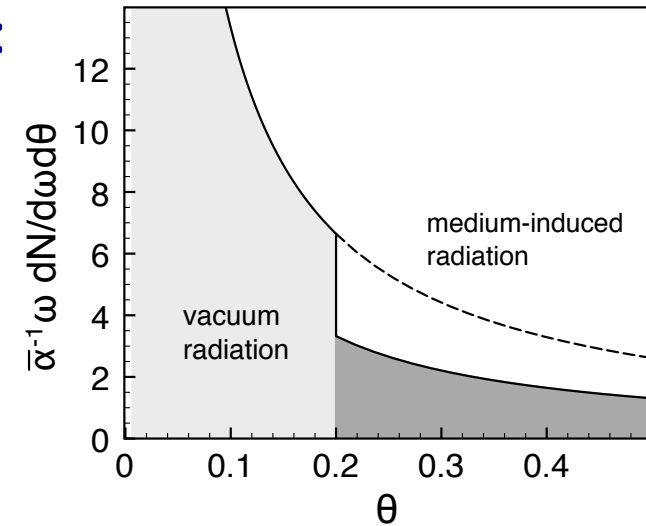


“Decoherence” in Opaque media

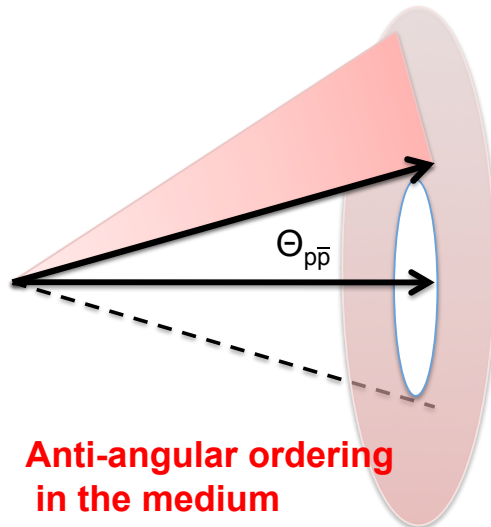
$$dN_q = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + A_{\text{med}}(\theta_{p\bar{p}}) \Theta(\cos \theta_{p\bar{p}} - \cos \theta)]$$

- First order in the scattering center density:

$$A_{\text{med}} = \hat{q} L r_{\perp}^2 \ln \frac{1}{r_{\perp} m_D}$$



Angular ordering in vacuum



Anti-angular ordering in the medium

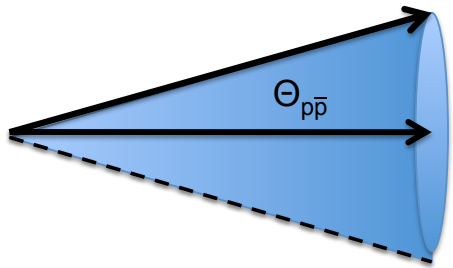
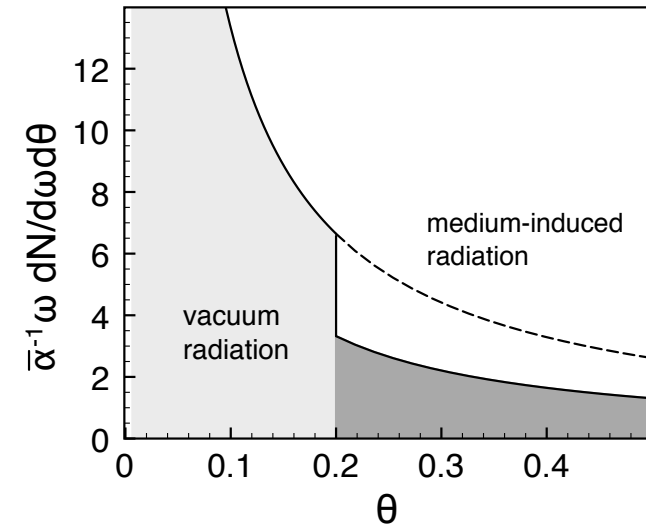
$$r_{\perp} \equiv \frac{\bar{p}_{\perp}}{\bar{E}} L \approx \theta_{p\bar{p}} L$$

“Decoherence” in Opaque media

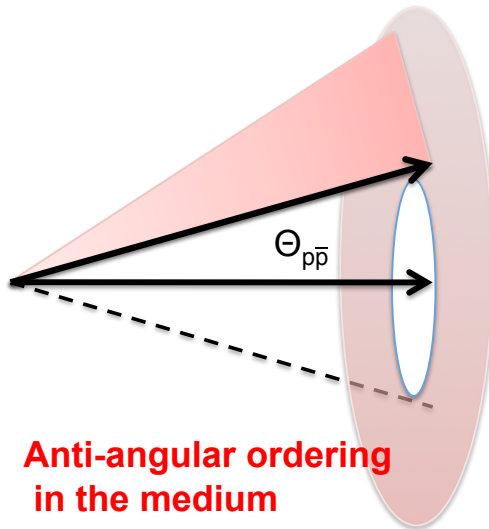
$$dN_q = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + A_{\text{med}}(\theta_{p\bar{p}}) \Theta(\cos \theta_{p\bar{p}} - \cos \theta)]$$

- Resumming multiple scatterings:

$$A_{\text{med}} = 1 - e^{-\hat{q}L} r_{\perp}^2 \ln \frac{1}{r_{\perp} m_D}$$



Angular ordering in vacuum



Anti-angular ordering in the medium

$$r_{\perp} \equiv \frac{\bar{p}_{\perp}}{\bar{E}} L \approx \theta_{p\bar{p}} L$$

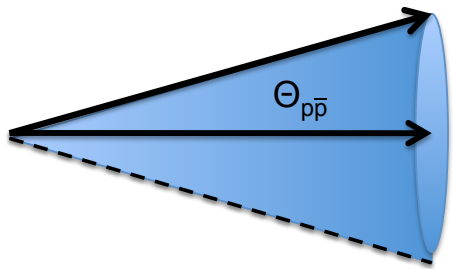
“Decoherence” in Opaque media

$$dN_q = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + A_{\text{med}}(\theta_{p\bar{p}}) \Theta(\cos \theta_{p\bar{p}} - \cos \theta)]$$

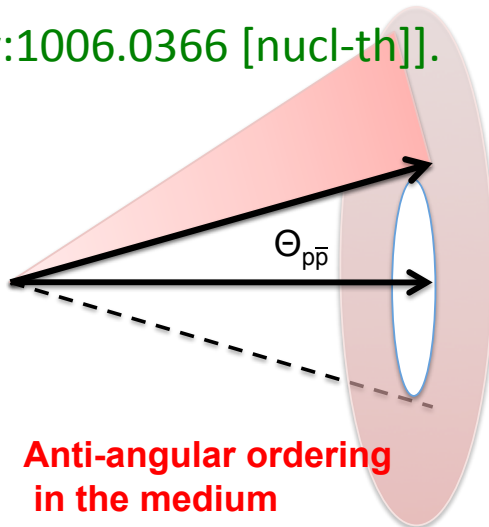
- In the high density limit $A_{\text{med}} \rightarrow 1$

$$dN_q \rightarrow \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta}$$

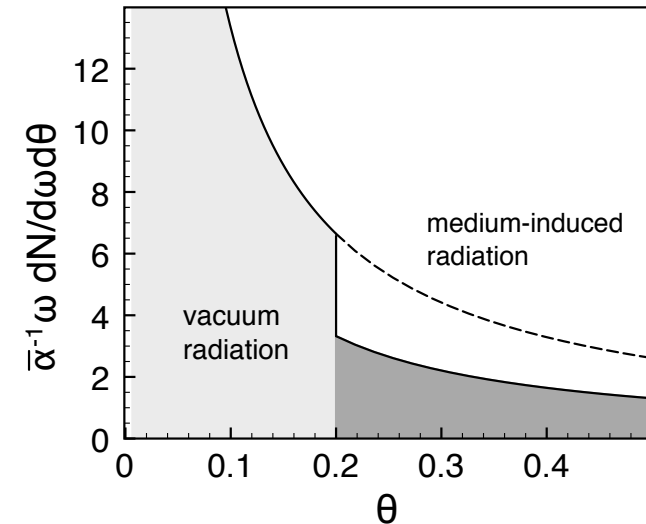
A. Leonidov, V. Nechitailo, [arXiv:1006.0366 [nucl-th]].



Angular ordering in vacuum



Anti-angular ordering in the medium



$$r_{\perp} \equiv \frac{\bar{p}_{\perp}}{\bar{E}} L \approx \theta_{p\bar{p}} L$$

“Decoherence” in Opaque media

- Antenna in a singlet state

$$dN_q^{\gamma*} = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} \Theta(\cos \theta - \cos \theta_{p\bar{p}})$$

- Colored antenna (g^* to qq or gg)

$$dN_q^{g*} = \frac{1}{2\pi} \alpha_s \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} \left(C_F \Theta(\cos \theta - \cos \theta_{p\bar{p}}) + C_A \Theta(\cos \theta_{p\bar{p}} - \cos \theta) \right)$$

- Extra piece: large angle emissions of the total charge of the pair (C_A for a gluon)

“Decoherence” in Opaque media

- Antenna in a singlet state (in-medium)

$$dN_q^{\gamma*} = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + A_{\text{med}}(\theta_{p\bar{p}}) \Theta(\cos \theta_{p\bar{p}} - \cos \theta)]$$

- Colored antenna (g* to qq or gg) (in-medium)

$$dN_q^{g*} = \frac{1}{2\pi} \alpha_s \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} \left(C_F [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + \Theta(\cos \theta_{p\bar{p}} - \cos \theta) A_{\text{med}}(\theta_{p\bar{p}})] \right. \\ \left. + C_A \Theta(\cos \theta_{p\bar{p}} - \cos \theta) (1 - A_{\text{med}}(\theta_{p\bar{p}})) \right)$$

“Decoherence” in Opaque media

- Antenna in a singlet state (in-medium)

$$dN_q^{\gamma*} = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + A_{\text{med}}(\theta_{p\bar{p}}) \Theta(\cos \theta_{p\bar{p}} - \cos \theta)]$$

- Colored antenna (g* to qq or gg) (in-medium)

$$dN_q^{g*} = \frac{1}{2\pi} \alpha_s \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta} \left(C_F [\Theta(\cos \theta - \cos \theta_{p\bar{p}}) + \Theta(\cos \theta_{p\bar{p}} - \cos \theta) A_{\text{med}}(\theta_{p\bar{p}})] \right. \\ \left. + C_A \Theta(\cos \theta_{p\bar{p}} - \cos \theta) (1 - A_{\text{med}}(\theta_{p\bar{p}})) \right)$$

- Memory loss in the opaque limit $A_{\text{med}} \rightarrow 1$

$$dN_q^{g*} = dN_q^{\gamma*} = \frac{1}{2\pi} \alpha_s C_F \frac{d\omega}{\omega} \frac{\sin \theta d\theta}{1 - \cos \theta}$$

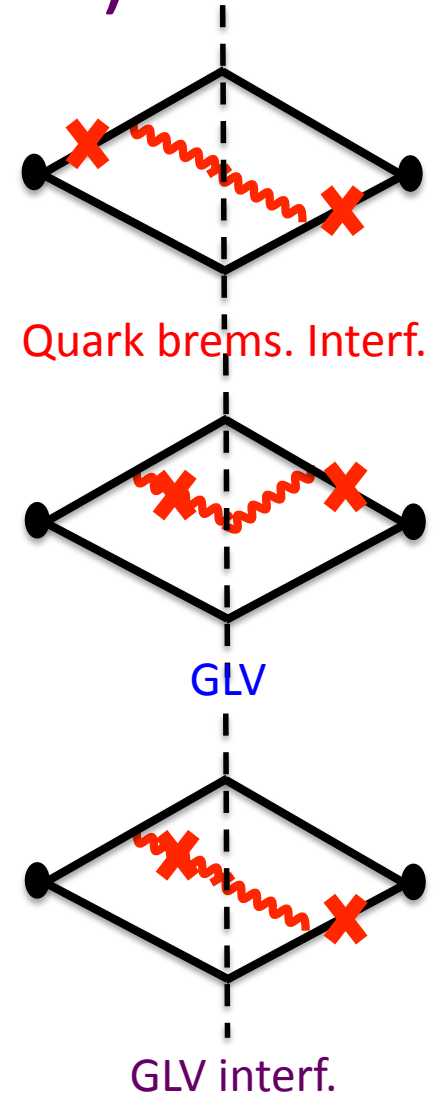
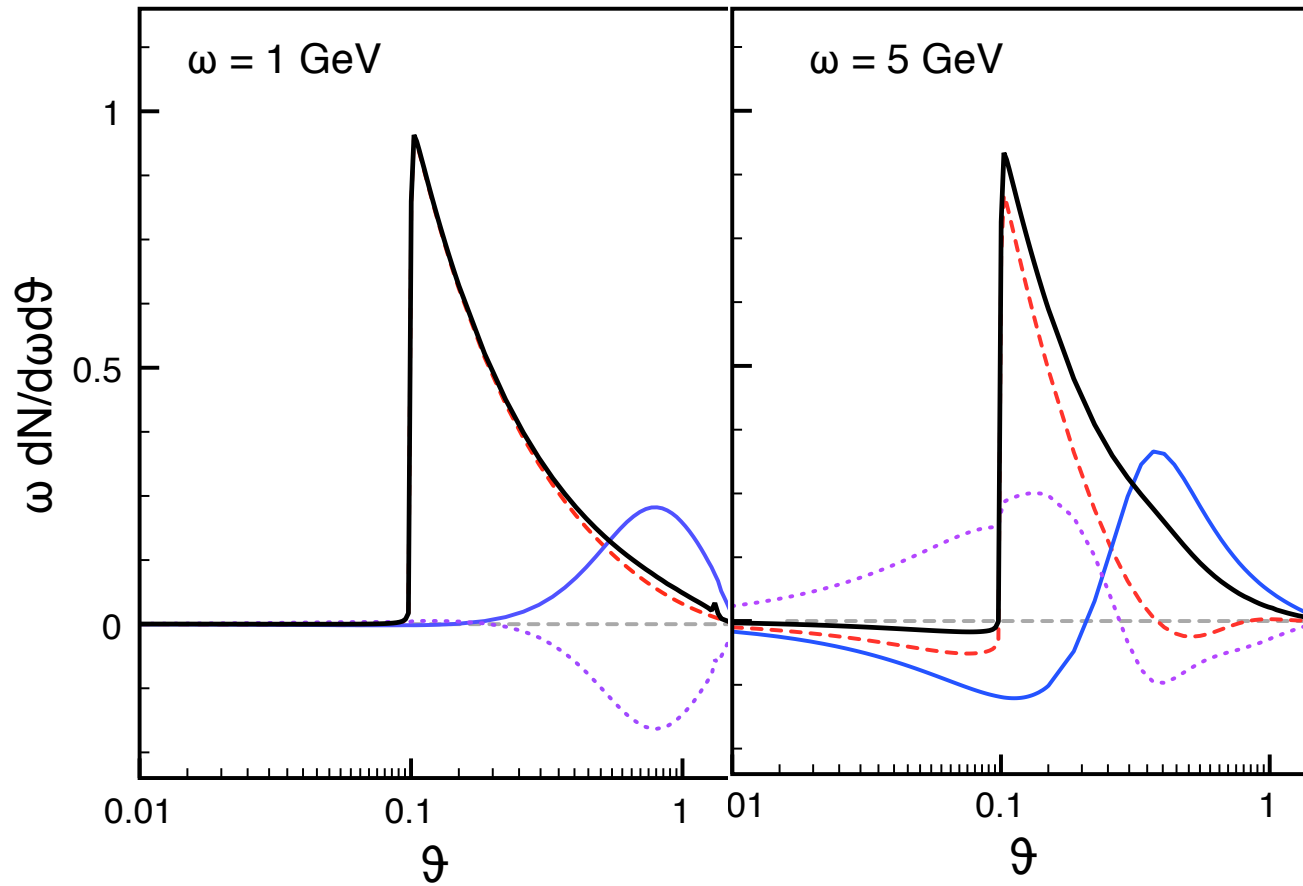
Toward medium modified jets?

- ✓ Coherence (neglected so far) plays an important role in medium-jet modification
- ✓ Geometrical separation between vacuum radiation and medium induced one. **Total decoherence in opaque media (Memory loss).**
- ✓ Logarithmic soft divergence: resummation of LL – QCD evolution eqs. in medium

Back up slides

Full spectrum (some numerics)

$L=20 \text{ GeV}^{-1} = 4 \text{ fm}$



Classical picture: Yang-Mills equations

$$[D_\mu, F^{\mu\nu}] = J^\nu \quad [D_\mu, J^\mu] = 0$$

- Soft gluons are described by a classical field

$$\mathcal{M}^{a,\mu}(k) = \lim_{k^2 \rightarrow 0} -k^2 A^{a,\mu}(k)$$

- The gluon production cross-section:

$$(2\pi)^3 2\omega \frac{dN}{d^3k} = \sum_{\lambda=\pm 1} |\mathcal{M}^a(k) \cdot \epsilon_\lambda|^2$$

- Linear response

$$A^\mu \equiv A_0^\mu + A_{\text{ind}}^\mu$$

Medium average

- Gaussian white noise

$$\langle \mathcal{A}_0^a(t, \mathbf{q}_\perp) \mathcal{A}_0^{*b}(t', \mathbf{q}'_\perp) \rangle = \hat{q} \delta^{ab} \delta(t - t') \delta^{(2)}(\mathbf{q}_\perp - \mathbf{q}'_\perp) V(\mathbf{q}_\perp)$$

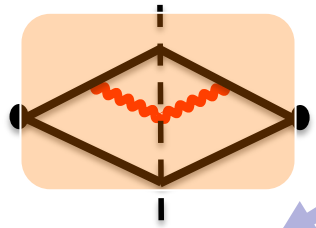
- 2-dimensional Coulomb potential ($\mu = m_D$)

$$V(\mathbf{q}_\perp) = \frac{1}{(\mathbf{q}_\perp^2 + \mu^2)^2}$$

The spectrum

Rearranging the terms according to the phases $\Omega_1, \Omega_2, \Omega_{12}$

$$(2\pi)^2 \omega \frac{dN}{d^3k} = 8\pi C_A C_F \alpha_s^2 \int \frac{d^2 \mathbf{q}_\perp}{(2\pi)^2} \int_0^L dt n(t) \mathcal{V}(\mathbf{q}_\perp)$$



GLV – GLV (interf)

$$\times \left[\begin{aligned} &(1 - \cos \Omega_1 t) \left(\frac{\mathbf{v}_\perp}{p \cdot v} - \frac{\bar{\mathbf{v}}_\perp}{\bar{p} \cdot v} \right) \cdot \left(\frac{\mathbf{v}_\perp}{p \cdot v} - \frac{\boldsymbol{\kappa}_\perp}{p \cdot k} \right) \\ &+ (1 - \cos \Omega_2 t) \left(\frac{\bar{\mathbf{v}}_\perp}{\bar{p} \cdot v} - \frac{\mathbf{v}_\perp}{p \cdot v} \right) \cdot \left(\frac{\bar{\mathbf{v}}_\perp}{\bar{p} \cdot v} - \frac{\bar{\boldsymbol{\kappa}}_\perp}{\bar{p} \cdot k} \right) \end{aligned} \right]$$

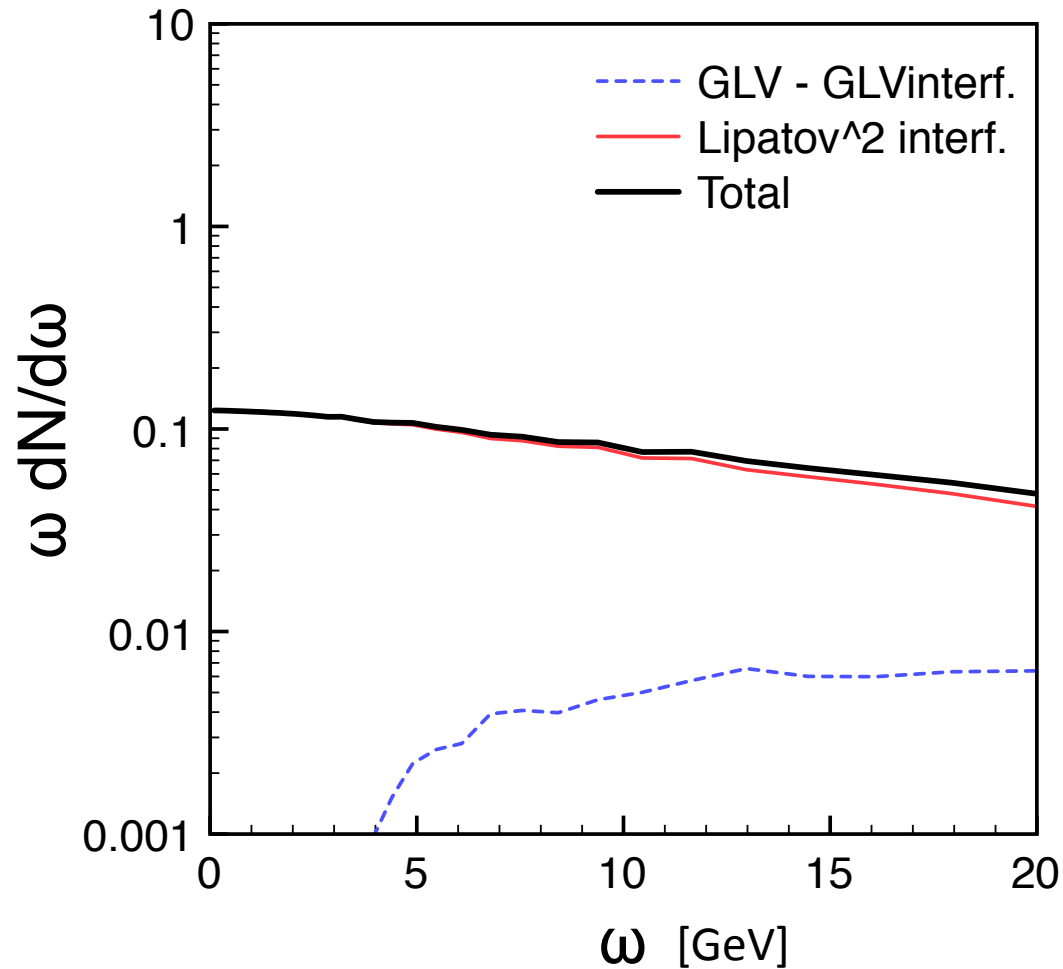
Interferences

$$+ (1 - \cos \Omega_{12} t) \left(\frac{\mathbf{v}_\perp}{p \cdot v} - \frac{\boldsymbol{\kappa}_\perp}{p \cdot k} \right) \cdot \left(\frac{\bar{\mathbf{v}}_\perp}{\bar{p} \cdot v} - \frac{\bar{\boldsymbol{\kappa}}_\perp}{\bar{p} \cdot k} \right) \Big]$$

$$L \cdot \bar{L}$$



Full spectrum (integrating the angle)



The spectrum is dropping exponentially

$$\omega \frac{dN}{d\omega} \sim e^{-\omega/\omega_{\max}}$$

$$\omega_{\max} \sim (\theta_{p\bar{p}}^2 L)^{-1}$$

GLV is cancelled by part of the gluon interferences