



Heavy quark and quarkonium evolutions in heavy ion collisions

Baoyi Chen

*Tianjin University
& Goethe Univeristy*

Main Collaborators: Pengfei Zhuang, Ralf Rapp, Yunpeng Liu, Xiaojian Du,
Wangmei Zha, Carsten Greiner



Topics

----- $\psi(2S)$

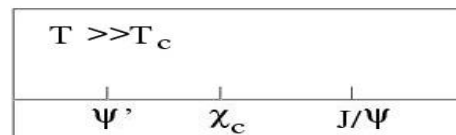
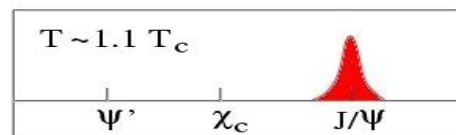
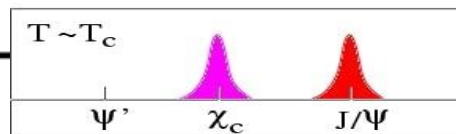
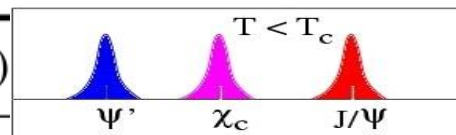
- 1) **Heavy quarkonium production mechanisms** in the Quark Gluon Plasma
primordial production, regeneration, photoproduction, transitions,...
- 2) **Charm diffusions** in the QGP
Langevin + Wigner function for single charm evolutions and recombination
large v_2 “puzzle” of J/ψ , v_2 between J/ψ and $\psi(2S)$
- 3) **Quantum effects inside $c\bar{c}$ dipole by color screening**
QGP screened heavy quark potential \rightarrow transitions between different bound states,
wave function evolutions (depend on T)
- 4) **Charmonium photoproduction from EB fields, even at $b < 2R_A$**
important at extremely low $p_T < 0.1$ GeV/c
 J/ψ , $\psi(2S)$
- 5) **pA collisions (still QGP existence ?)**
Phys.Lett. B 765, 323(2017)
- 6) **Ds/D0 enhancement: strange enhancement and charm conservation**

background

$$V = U$$

State	J/ ψ (1S)	χ_c (1P)	ψ' (2S)	Υ (1S)	χ_b (1P)	Υ (2S)
T_d/T_c	2.10	1.16	1.12	>4.0	1.76	1.60

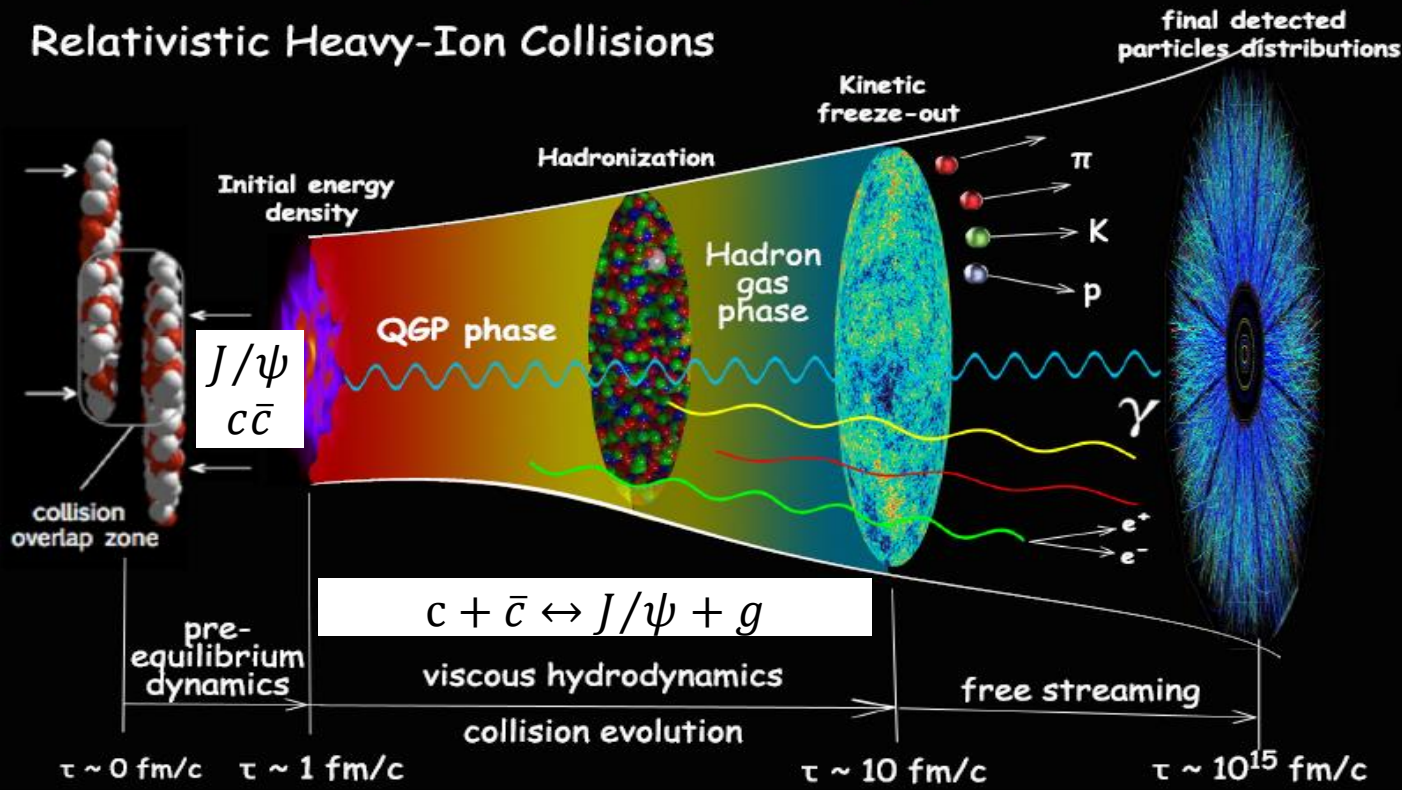
Satz, et al



Sequential dissociation

Little Bang @ C. Shen

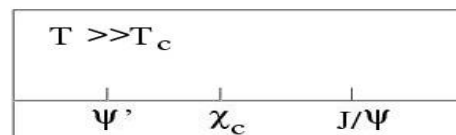
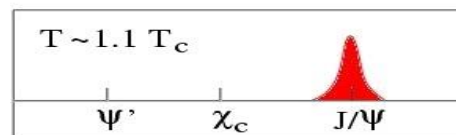
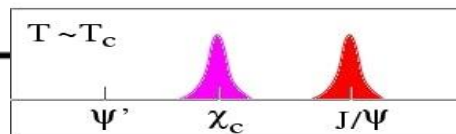
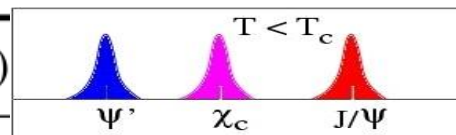
Relativistic Heavy-Ion Collisions



background

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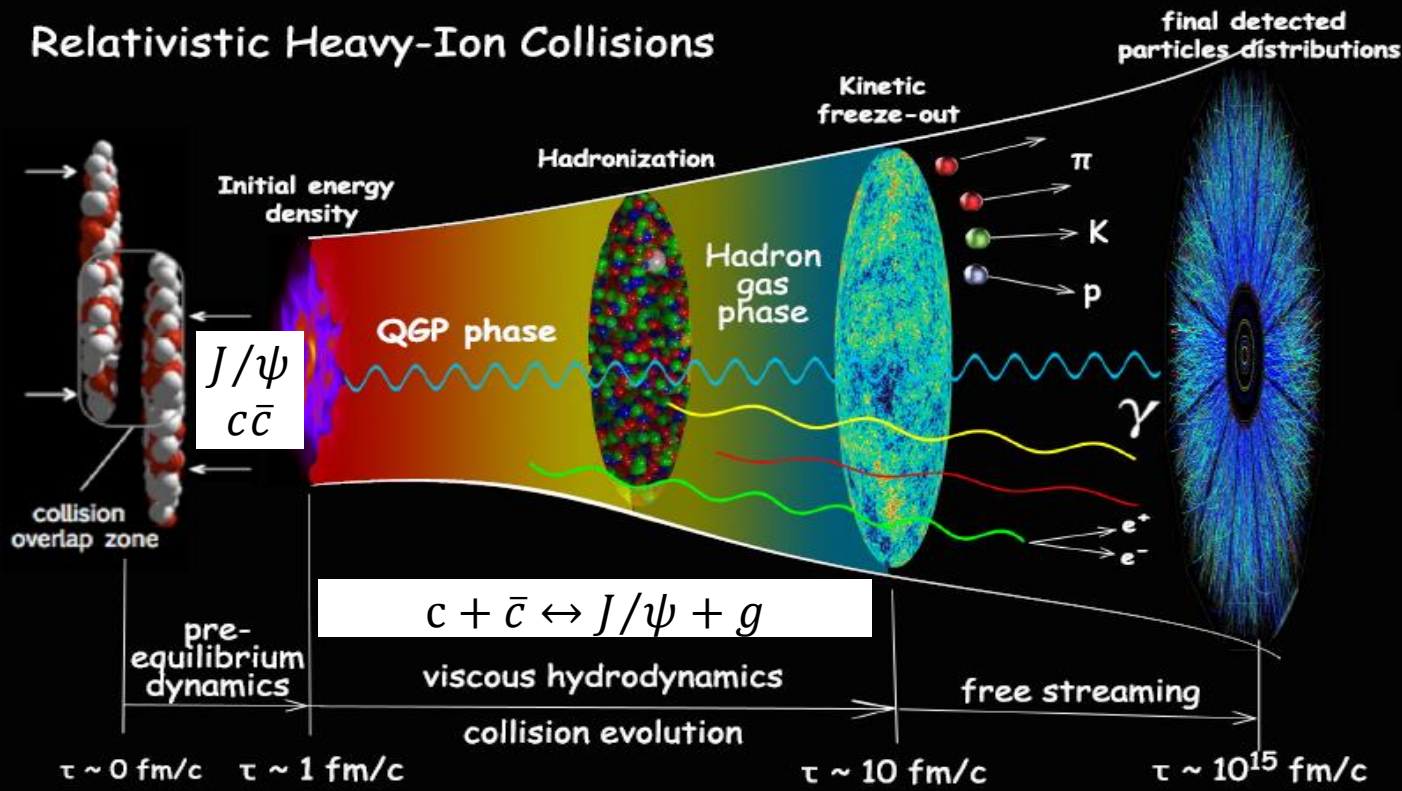
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Satz, et al

Little Bang @ C. Shen

Relativistic Heavy-Ion Collisions



Sequential dissociation

Heavy Ion:

- light hadron spectra;
- Jet energy loss;
- heavy quark thermalize;
- quarkonium dissociation
- thermal photons;
- B induced chiral effect

Heavy quarkonium as a probe of QGP

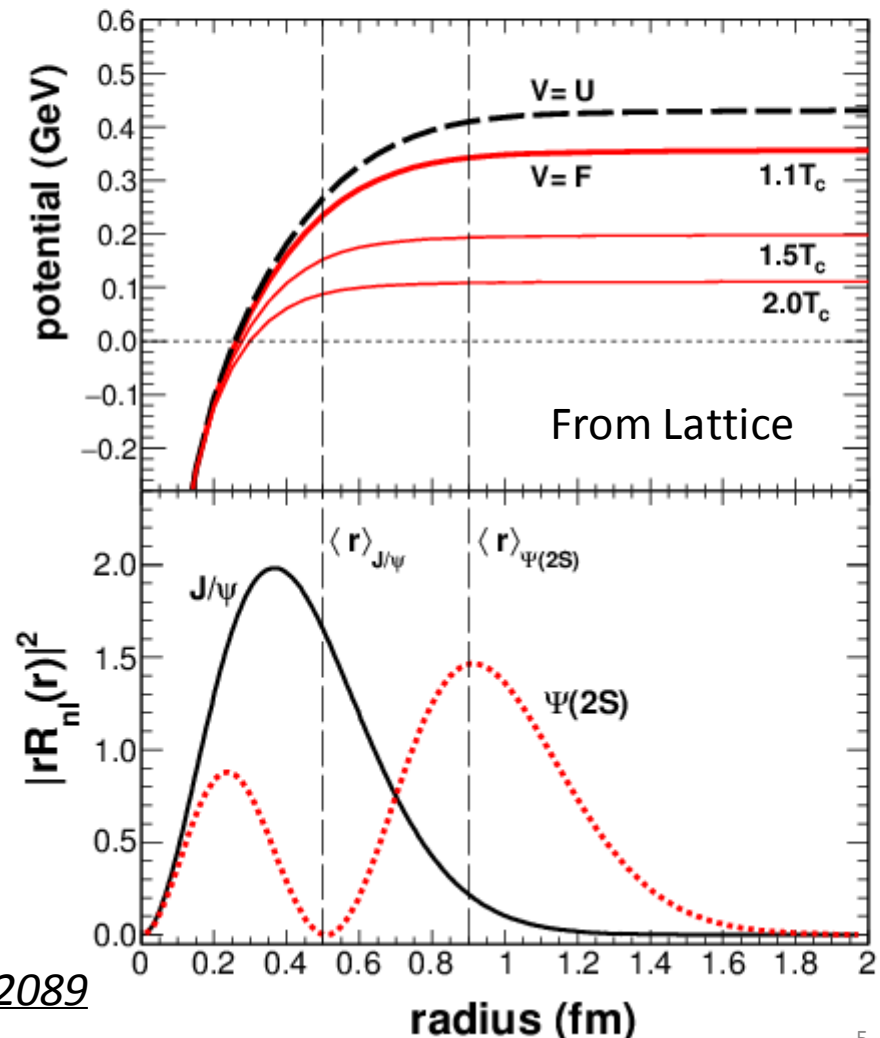
J/ψ as a probe of QGP:

J/ψ suffer color screening and inelastic collisions of partons in QGP

J/ψ production in AA collisions
(with cold and hot matter effects)

$$R_{AA}^{J/\psi} = \frac{N_{AA}^{J/\psi}}{N_{pp}^{J/\psi} N_{coll}}$$

J/ψ production in pp collisions
(without CNM and HM)



BC, Du, Rapp, arXiv:1612.02089

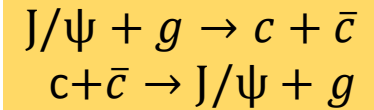


1. Charmonium production mechanisms in HIC

Heavy quarkonium as a probe of QGP

Transport model

$$\frac{\partial f_\psi}{\partial t} + \frac{\vec{p}_\psi}{E} \cdot \vec{\nabla}_x f_\psi = -\alpha_\psi f_\psi + \beta_\psi$$



$$\alpha_\psi(\vec{p}_t, \vec{x}_t, \tau, \vec{b}) = \frac{1}{2E_t} \int \frac{d^3\vec{k}}{(2\pi)^3 2E_g} \sigma_{g\psi}(\vec{p}, \vec{k}, T) 4F_{g\psi}(\vec{p}, \vec{k}) f_g(\vec{k}, T)$$

$$\beta_\psi(\vec{p}_t, \vec{x}_t, \tau, \vec{b}) = \frac{1}{2^4 (2\pi)^9 E_t} \int \frac{d^3\vec{k}}{E_g} \frac{d^3\vec{q}_c}{E_c} \frac{d^3\vec{q}_{\bar{c}}}{E_{\bar{c}}} W_{c\bar{c}}^{\psi g}(\vec{q}_c, \vec{q}_{\bar{c}}) f_c(\vec{q}_c, T) f_{\bar{c}}(\vec{q}_{\bar{c}}, T) \times (2\pi)^4 \delta^{(4)}(p + k - q_c - q_{\bar{c}})$$

Dynamical evolution

Quark number

	N(q \bar{q}) per central AA (b=0)		
	SPS	RHIC	LHC
charm	0.2	10	130
bottom	---	0.05	5

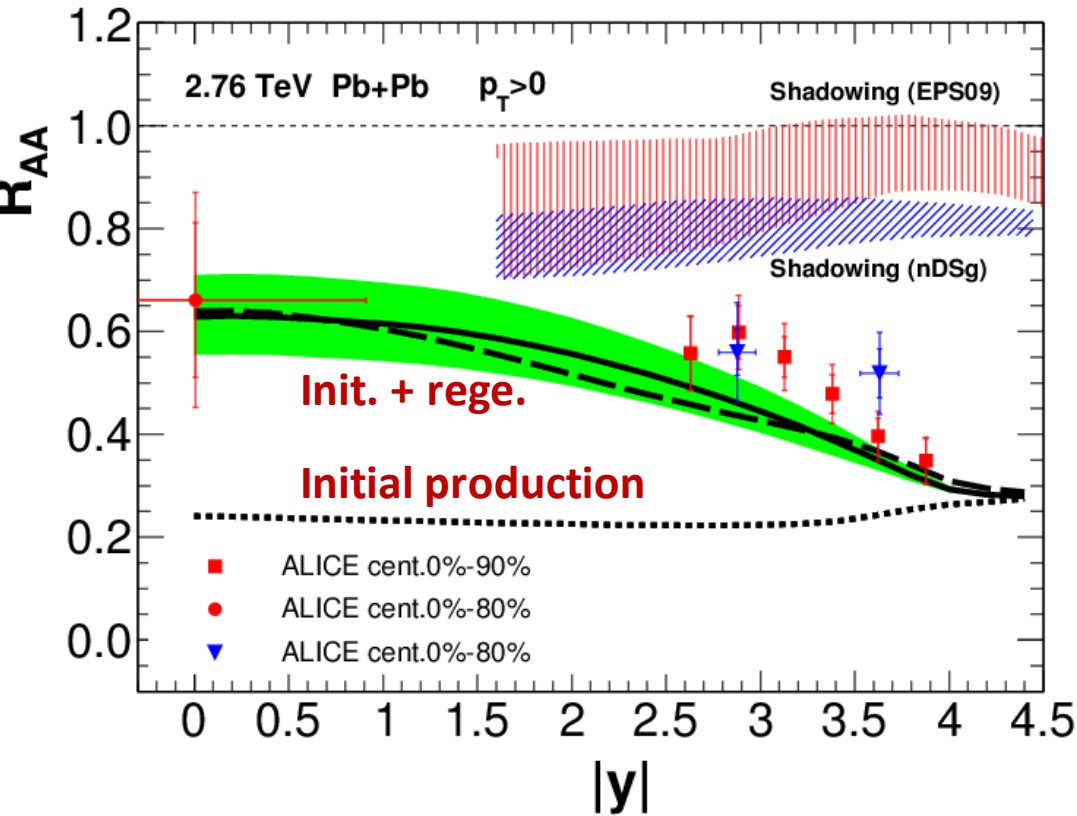
$$N^{c\bar{c} \rightarrow J/\psi} \sim (N^{c\bar{c}})^2$$

- ✓ Higher temperature, larger α_ψ , less initial production
- ✓ Larger $N_{c\bar{c}}$, larger β_ψ , more regeneration

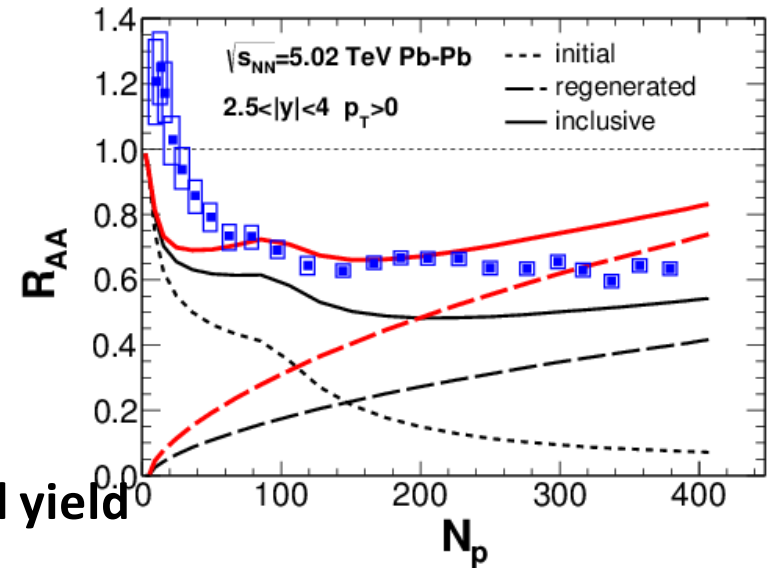
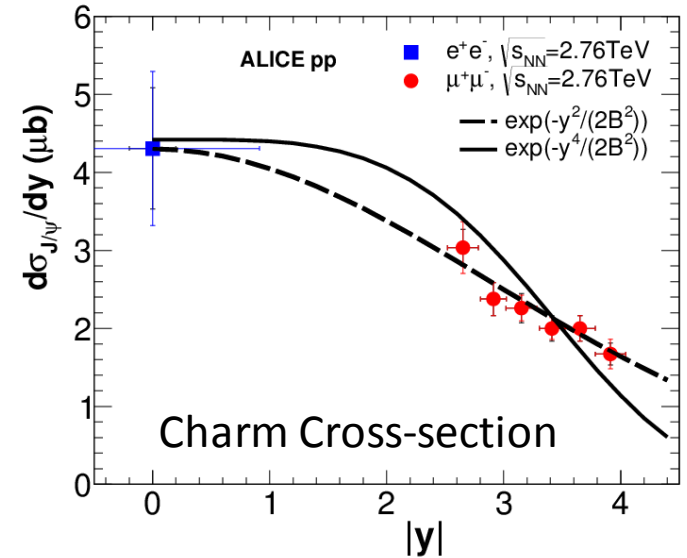
Initially produced ψ : from parton hard scatterings, carry large p_T

Regenerated: charm interact with QGP, loss energy, carry QGP collective flow

Charmonium in QGP



B. Chen, PRC 93, 054905(2016)



Summary:

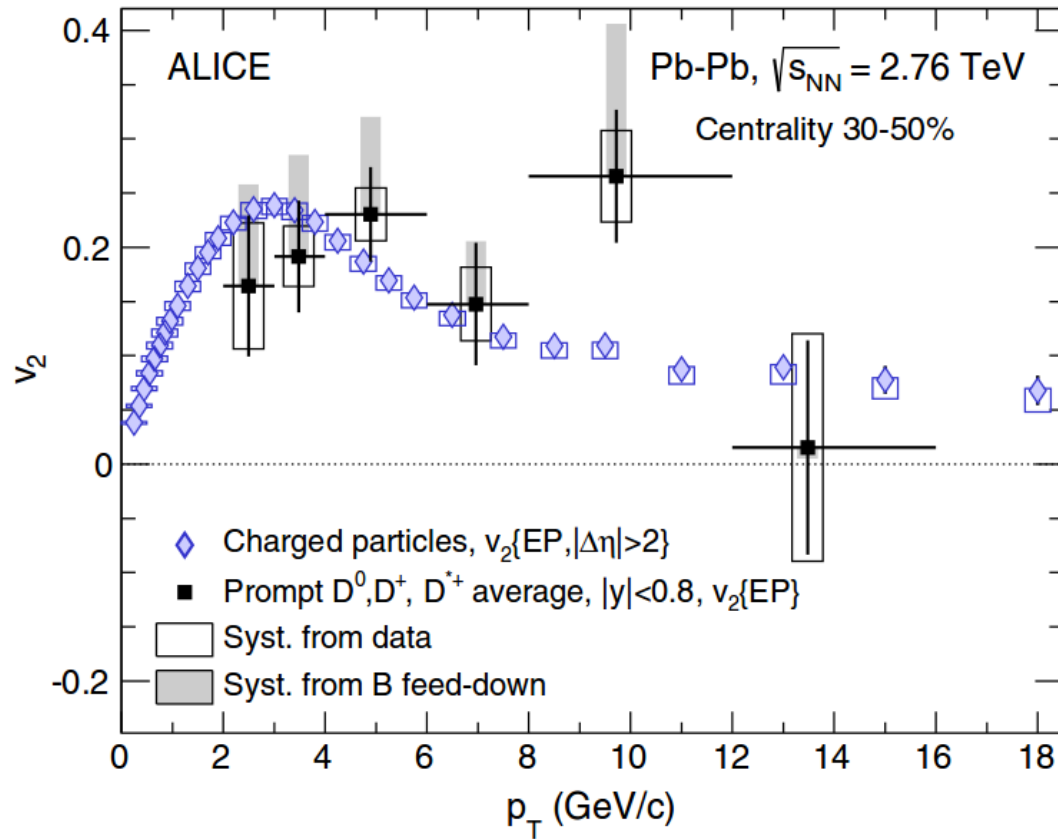
Regeneration dominates at low p_T , and total yield

Initial production dominates at high p_T

2. Charm diffusion in the expanding QGP

Charm diffusion

D mesons obtain the similar collective flows like light hadrons
→ indicate the momentum thermalization of charm quarks
at the QGP hadronization.



PRL, 111, 102301(2013)

However,
how and **when** charm quarks reach
thermalization ?

Depending on:
QGP temperature,
coupling strength,
Charm momentum, etc

How does charm diffusion **suppress** the Ψ regeneration process?

Charm diffusion

First, Let's assume an instant charm thermalization

1) Local momentum distribution

$$f_c(p) = \frac{N^{norm}}{e^{p^\mu u_\mu/T} + 1}$$

in local fluid cell
 u_μ : velocity of QGP cell

2) Charm distribution in coordinate space

$$\partial_\mu(\rho_c(r)u^\mu) = 0$$

Conservation of charm quark number;
Strong diffusion (controlled by u^μ)

Large mass of charm quark: Not chemical equilibrium

Full distribution in phase space $f_c(r, p) = \rho_c(r)f_c(p)$

3) Charm initial distribution from hard scatterings,

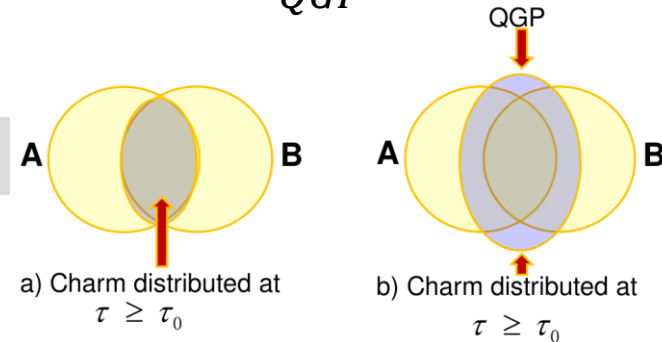
$$\rho_c(\tau_0, x_T, \eta) = \frac{T_A(x_T)T_B(x_T - b)\cosh\eta}{\tau_0} \frac{d\sigma_{pp}^{c\bar{c}}}{d\eta}$$

Usually with
 uncertainties
 ~ 50%

Charm diffusion and kinetic equilibrium

Remember that
$$N_{J/\psi} \sim \int dV \frac{N_c}{V_{QGP}} \frac{N_{\bar{c}}}{V_{QGP}} W_{combine} \sim \frac{(N_{c\bar{c}})^2}{V_{QGP}}$$

Charm expands outside with QGP

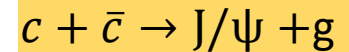


Beam-line View

- **coalescence model**

*J. Zhao, B. Chen,
arXiv:1705.04558*

$$\frac{dN_{J/\psi}}{d^2\vec{P}_T d\eta} = C \int \frac{P^\mu d\sigma_\mu(R)}{(2\pi)^3} \frac{d^4r d^4p}{(2\pi)^3} W(r, p) f_c(\vec{r}_1, \vec{p}_1, t) f_{\bar{c}}(\vec{r}_2, \vec{p}_2, t)$$



C=1/12 for vector meson (J/psi)

- Wigner function describes the recombination probability of one c and \bar{c} :

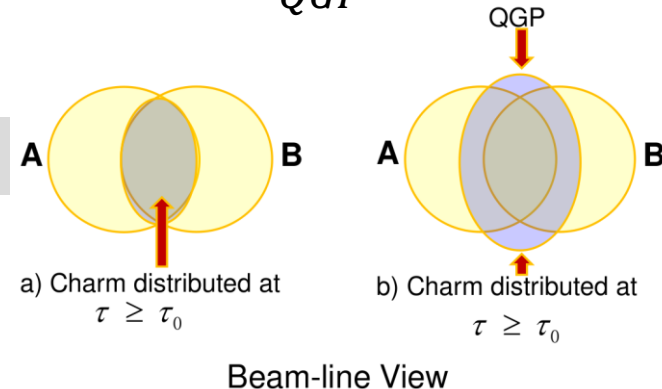
$$W(\vec{r}, \vec{p}) = \int d^3y e^{-i\vec{p} \cdot \vec{y}} \psi(\vec{r} + \frac{\vec{y}}{2}) \psi^*(\vec{r} - \frac{\vec{y}}{2})$$

$\psi(\vec{r})$: wavefunction of charmonium eigenstate. (from time-independent Schrodinger equation)

Charm diffusion and kinetic equilibrium

Remember that
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Charm expands outside with QGP



● **2.76 TeV** V.S. **5.02 TeV**

(Pb-Pb collisions):

larger initial T_0^{QGP} , larger QGP volume at hadronization

charm number enhanced by more than 50%

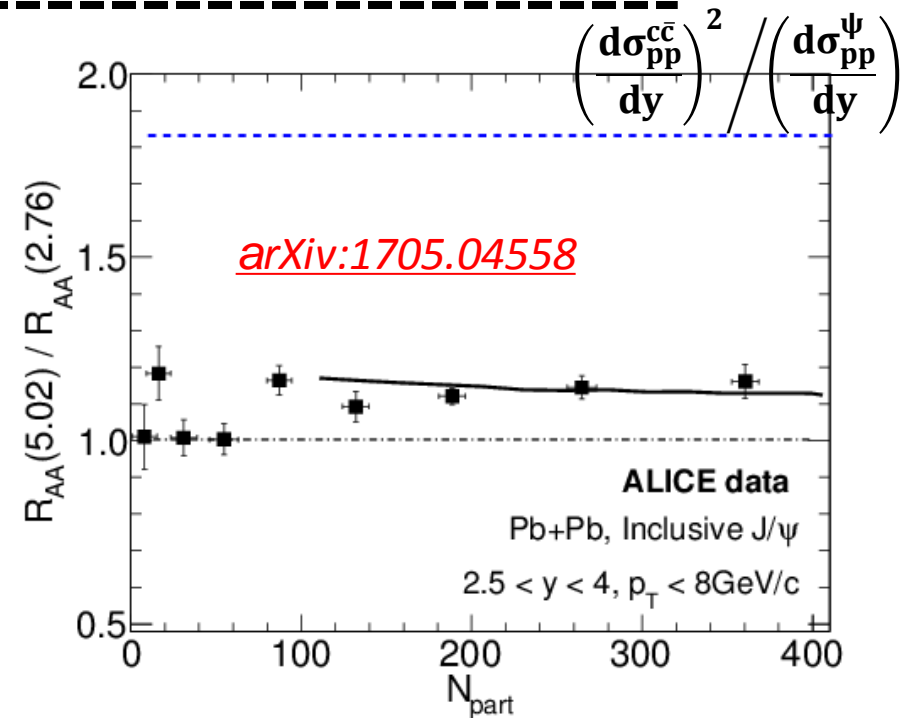
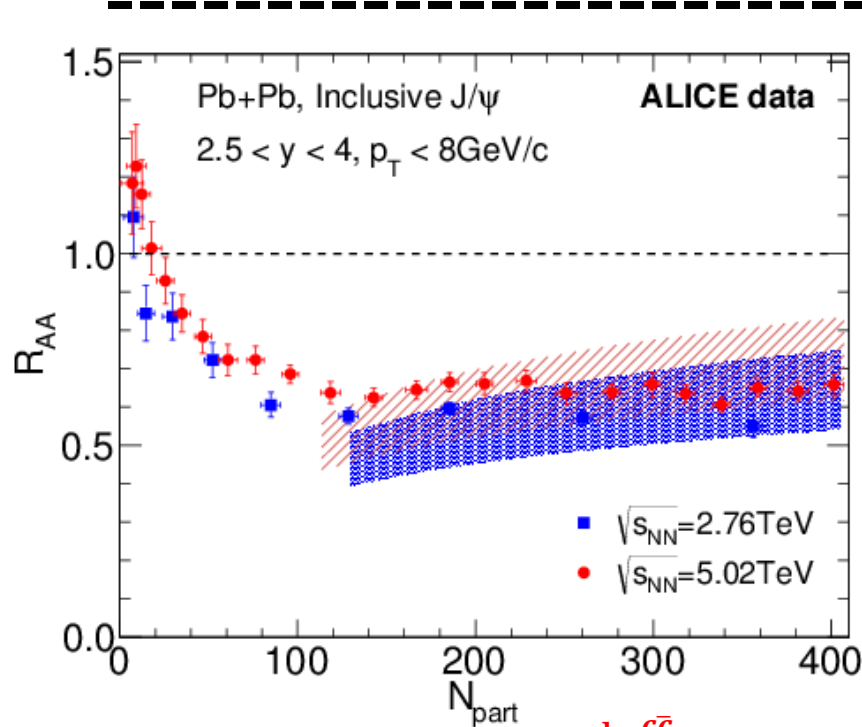
→ Accelerating expansion makes $V_{QGP}(T = T_c, 5.02)$ larger

→ $N_{J/\psi}(5.02)$ does not become $\sim 1.5^2$ times, (see exp. Data later)

Experimental data gives:

$$R_{AA} = \frac{N_{AA}^{c+\bar{c} \rightarrow J/\psi+g}}{N_{pp}^{J/\psi} N_{coll}}$$

J/ψ R_{AA} at 2.76 and 5.02 TeV



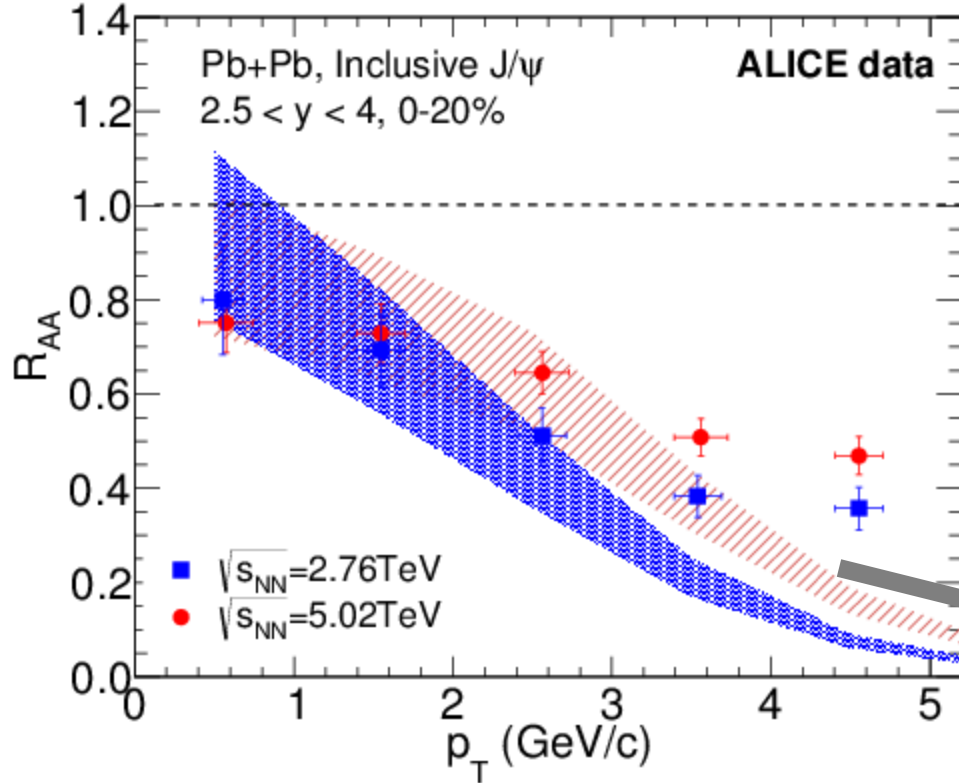
Cross section: $\left[\frac{d\sigma_{pp}^{c\bar{c}}}{dy} = 0.33\text{mb} \text{ (} 0.57\text{mb)} \text{ for } 2.76 \text{ (} 5.02) \text{ TeV} \right.$
 $\left. \text{Upper limit: } \frac{d\sigma_{pp}^{c\bar{c}}}{dy} \text{ enhanced by } 20\% \right.$

The ratio of charm quark number at 5.02 and 2.76 TeV is around 1.7 with large uncertainty,

- (1) with the same QGP, we expect R_{AA} ratio \approx charm ratio ≈ 1.7
- (2) with different QGP, R_{AA} ratio ≈ 1.1

→ Strong diffusion of charm suppress J/ψ regeneration.

J/ψ R_{AA} at 2.76 and 5.02 TeV



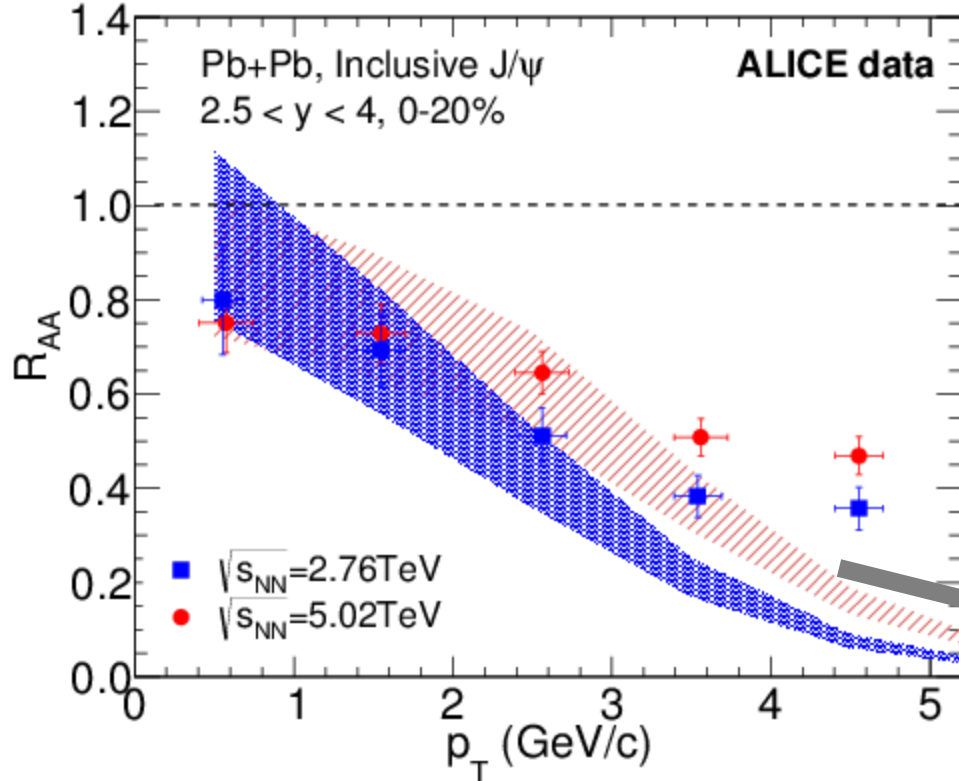
1). Charm collective flow also change the regenerated J/ψ p_T distribution

2). At 5.02 TeV, QGP expansion stronger, push charm quark to larger p_T bin

3). Underestimation at high p_T is due to the lack of initial production, which dominate the high p_T region.

[arXiv:1705.04558](https://arxiv.org/abs/1705.04558)

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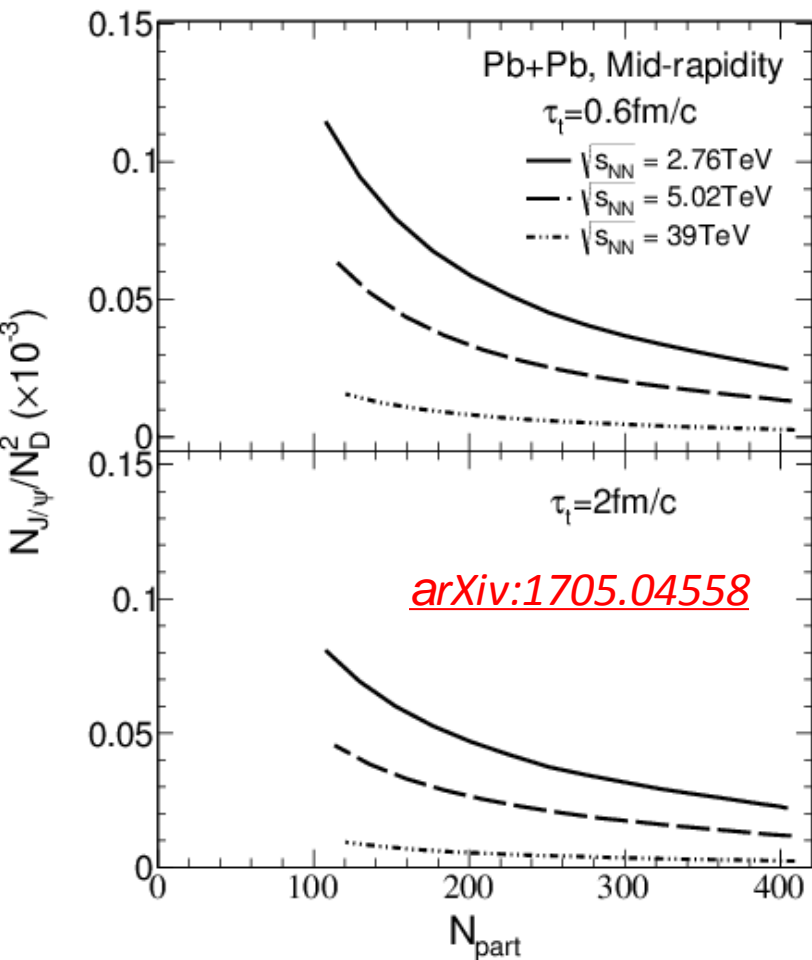
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[arXiv:1705.04558](https://arxiv.org/abs/1705.04558)

● Can we define an observable to measure the charm diffusion effect ?

independent of charm cross section, shadowing effect, etc

$$N_{J/\psi} / N_D^2$$

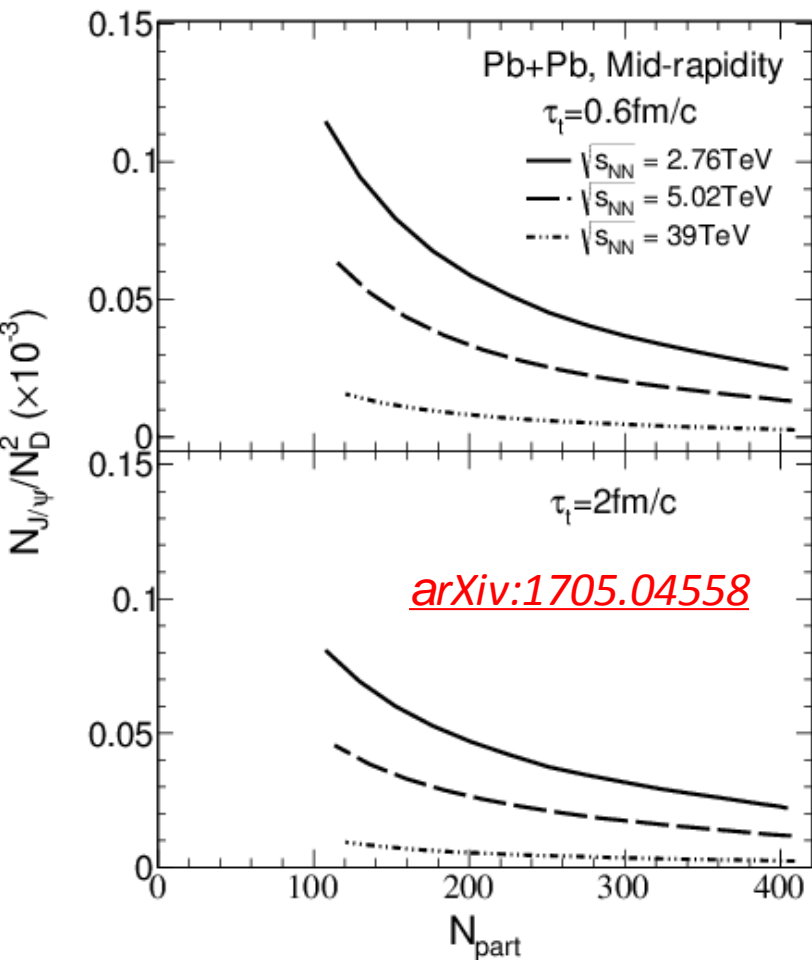


$$\frac{N_{J/\psi}}{(N_D)^2} \sim \int dV \overset{\text{Hot Medium Effect}}{\downarrow} f_c^{\text{norm}} f_{\bar{c}}^{\text{norm}} W_{\text{combine}}$$

This ratio in AA collisions:

- ① eliminate the shadowing effect.
- ② Does NOT depend on $\frac{d\sigma_{pp}^{c\bar{c}}}{d\eta}$
- ③ Contains hot medium effects on charm (collective flows of QGP change f_c^{norm})

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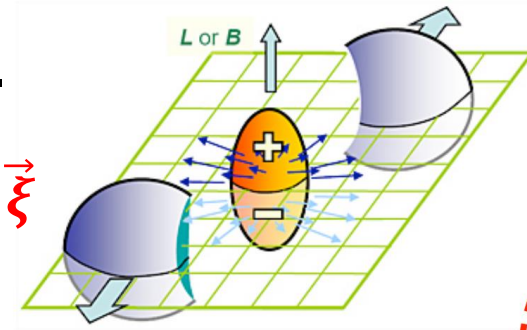
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● **Centrality dependence**

from semi-central to central collisions:
 larger T_0^{QGP} , stronger QGP expansion,
recombination probability of ONE c and \bar{c}
decreases.

- **$\sqrt{s_{NN}}$ Dependence:** higher $\sqrt{s_{NN}}$, QGP expansion also stronger.

$\psi(2S)$ v.s. J/ψ



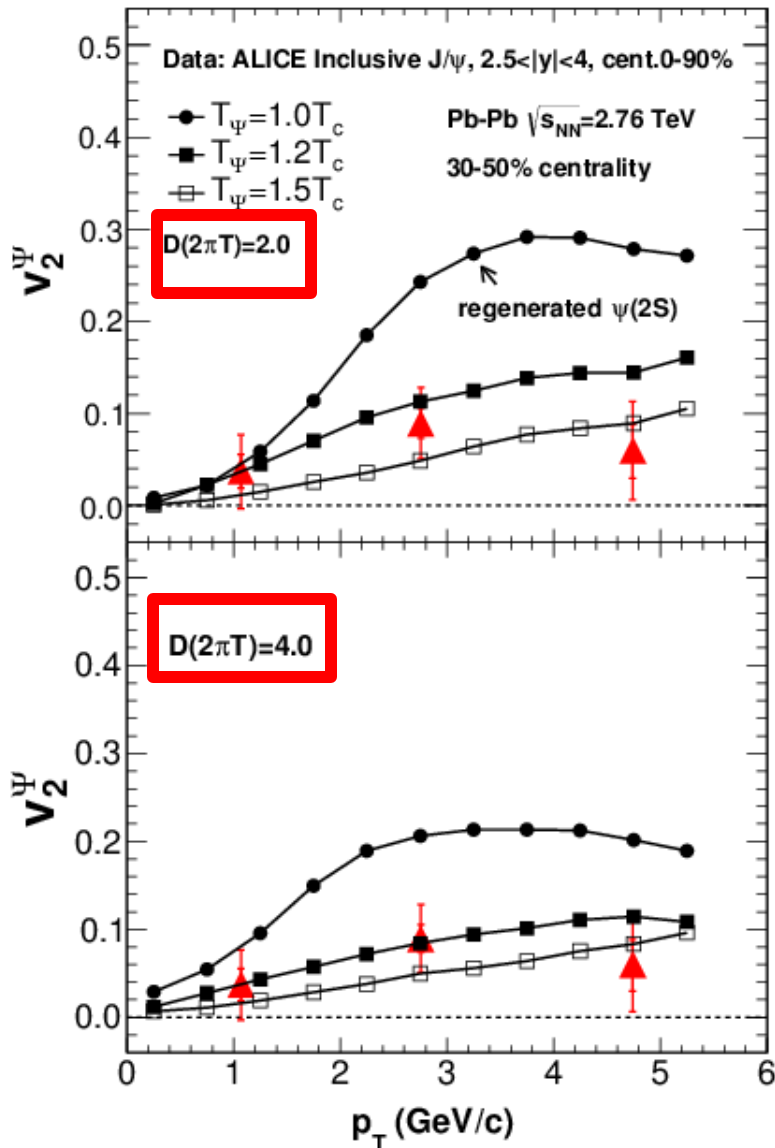
$$\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi}$$

$$\eta_D = \frac{T}{DE_c} \quad D: \text{spatial diffusion coeff.}$$

$\psi(2S)$ will be regenerated in the later stage of QGP expansion,

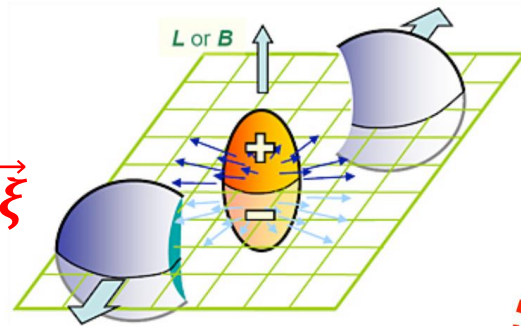
→ $\psi(2S)$ Carry relatively larger collective flows

independent of c coupling strength



B. Chen, PRC 95 (2017) 034908

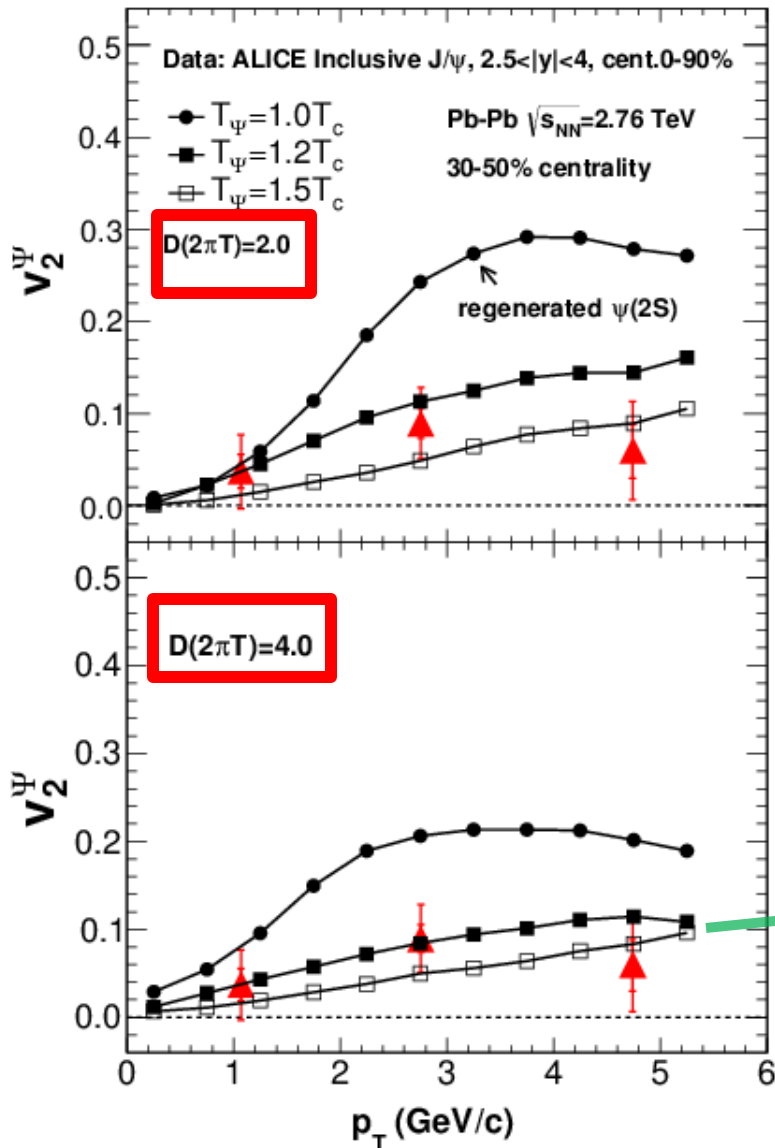
$\psi(2S)$ v.s. J/ψ



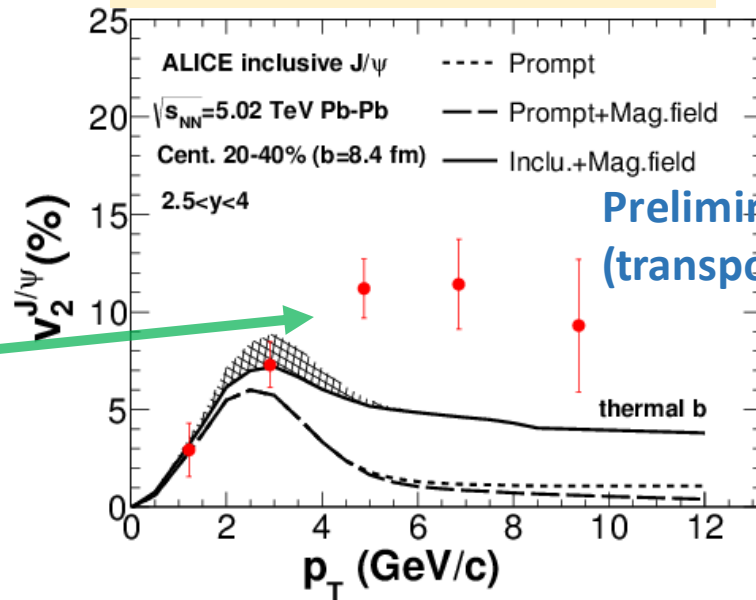
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“non-thermal charm + coalescence” can explain J/ψ v_2 at 5.02 TeV?



Shape of v_2 is important!



Preliminary
(transport model)

B. Chen, PRC 95 (2017) 034908

$\psi(2S)$ production

3. Internal evolutions of $c\bar{c}$ dipole wave function

Time-dependent Schrodinger equation

$$\tau_{c\bar{c}} < 0.1 \text{ fm}$$

$$\tau_{\psi} < \tau_0 (\sim 0.6 \text{ fm})$$

Pre-equilibrium

QGP evolution (hydro)

time \rightarrow

$$V_{c\bar{c}}(r) = \text{Cornell}$$

pp data

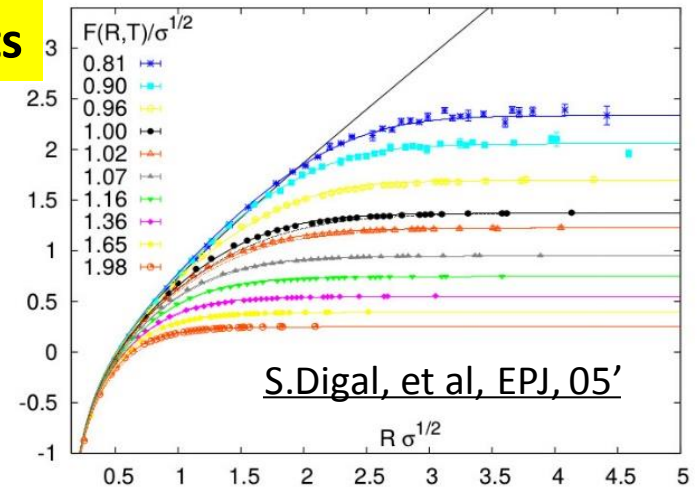
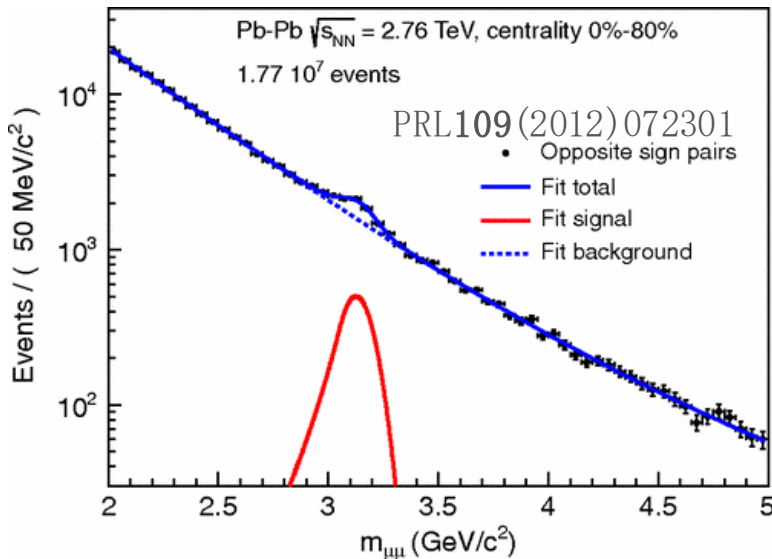
$$V_{c\bar{c}}(r, T) = \text{Lattice } (F, U)$$

Time-dependent Schrodinger equation

$\tau = 0$
(Pb-Pb)

τ_0
 $c\bar{c}$ dipole

J/ ψ and $\psi(2S)$ measurements in experiments



$$|c\bar{c}\rangle = c_{1S}(t)|J/\psi\rangle + c_{2S}(t)|\psi(2S)\rangle + \dots$$

Exp. measure the eigenstates of Cornell potential (in vacuum);
by dilepton decay.

$c\bar{c}$ dipole potential in QGP is COLOR SCREENED. transitions

Time-dependent Schrodinger equation

$\tau_{c\bar{c}} < 0.1 \text{ fm}$ $\tau_{\psi} < \tau_0 (\sim 0.6 \text{ fm})$

Pre-equilibrium

QGP evolution (hydro)

time →

$V_{c\bar{c}}(r) = \text{Cornell}$

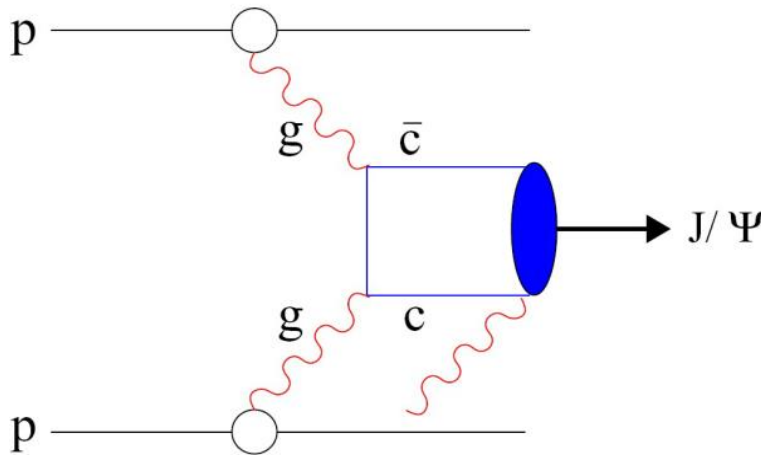
pp data

$V_{c\bar{c}}(r, T) = \text{Lattice } (F, U)$

Time-dependent Schrodinger equation

$\tau = 0$
(Pb-Pb)

τ_0
 $c\bar{c}$ dipole



$$r_{c-\bar{c}} \sim 1/(2m_c) \sim 0.07 \text{ fm}$$

Radii of J/ψ and ψ(2S) : 0.5 fm and 0.9 fm

It takes some time to evolve into a charmonium,
Shorter for ground state, longer for 2S

Color screening change $c\bar{c}$ dipole wave function evolutions,
Change fractions of 1S and 2S in the dipole.

Time-dependent Schrodinger equation

$$\tau_{c\bar{c}} < 0.1 \text{ fm}$$

$$\tau_{\psi} < \tau_0 (\sim 0.6 \text{ fm})$$

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pp data

$$V_{c\bar{c}}(r, T) = \text{Lattice } (F, U)$$

Time-dependent Schrodinger equation

$\tau = 0$
(Pb-Pb)

τ_0
 $c\bar{c}$ dipole

$$i\hbar \frac{\partial}{\partial t} \psi(r, t) = \left[-\frac{\hbar^2}{2m_{\mu}} \nabla^2 + V(r, t) \right] \psi(r, t)$$

[R. Katz, P. B. Gossiaux, 16'](#)
[B.Z. Kopeliovich, et al, PRC, 15'](#)
[Taesoo Song, et al, PRC, 15'](#)

r: relative distance between c and \bar{c}
 $m_{\mu} = m_c/2$: scaling mass

Wavefunction of eigenstates:

$$\Psi_{klm}(\vec{r}) = R_{kl}(r) Y_{lm}(\theta, \varphi)$$

● Numerical form:

$$\begin{pmatrix} \mathbf{T}_{0,0}^{n+1} & \mathbf{T}_{0,1}^{n+1} & 0 & 0 & \dots \\ \mathbf{T}_{1,0}^{n+1} & \mathbf{T}_{1,1}^{n+1} & \mathbf{T}_{1,2}^{n+1} & 0 & \dots \\ 0 & \mathbf{T}_{2,1}^{n+1} & \mathbf{T}_{2,2}^{n+1} & \mathbf{T}_{2,3}^{n+1} & \dots \\ \dots & \dots & \dots & \dots & \dots \\ \dots & \dots & \dots & \dots & \dots \end{pmatrix} \begin{pmatrix} \psi_0^{n+1} \\ \psi_1^{n+1} \\ \psi_2^{n+1} \\ \psi_3^{n+1} \\ \dots \end{pmatrix} = \begin{pmatrix} \Gamma_0^n \\ \Gamma_1^n \\ \Gamma_2^n \\ \Gamma_3^n \\ \dots \end{pmatrix}$$

Matrix elements: $\mathbf{T}_{j,j}^{n+1} = 2 + 2a + bV_j^{n+1}$

$$\mathbf{T}_{j,j+1}^{n+1} = \mathbf{T}_{j+1,j}^{n+1} = -a$$

$$a = i \Delta t / (2m_{\mu} (\Delta r)^2)$$

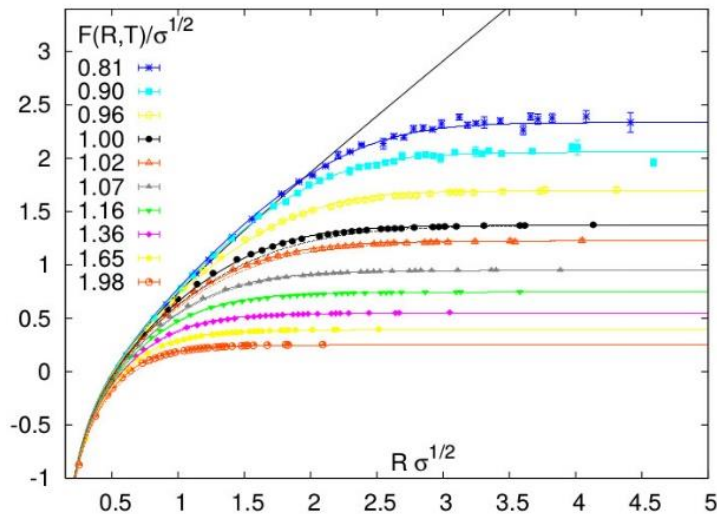
$$b = i \Delta t$$

Heavy quark potential at finite temperature

- mS eigenstate components in one dipole:

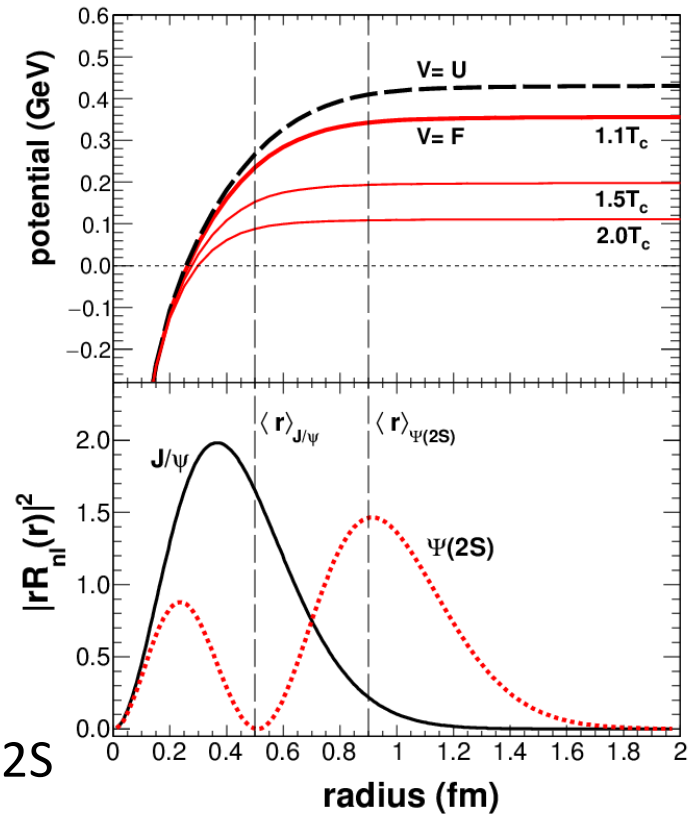
$$c_{mS}(t) = \langle R_{mS}(r) | \frac{\psi(r, t)}{r} \rangle = \int R_{mS}(r) \psi(r, t) \cdot r dr$$

- Heavy quark potential :



S.Digal, et al, EPJ, 05'

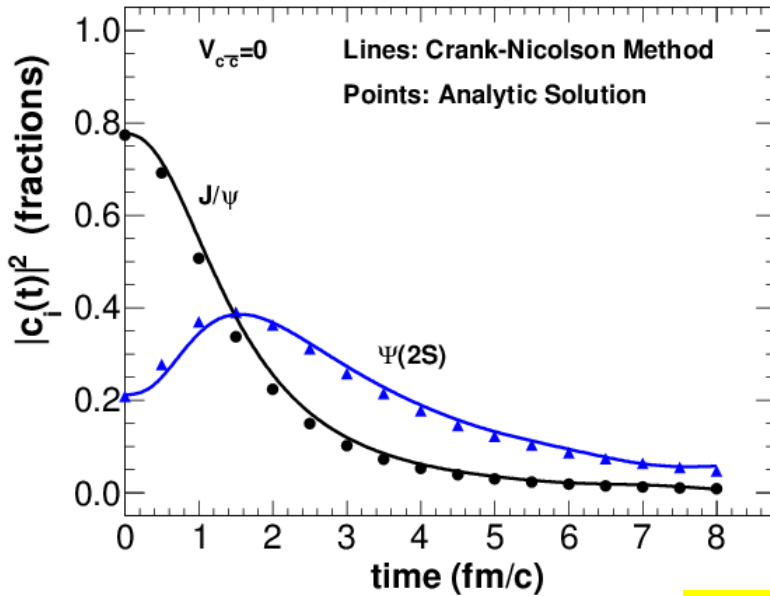
BC, Du, Rapp, arXiv:1612.02089



- At $\sim 2T_c$, Strong color screenin for 1S and 2S
- At $\sim 1T_c$, potential recover at $\langle r(1S) \rangle$

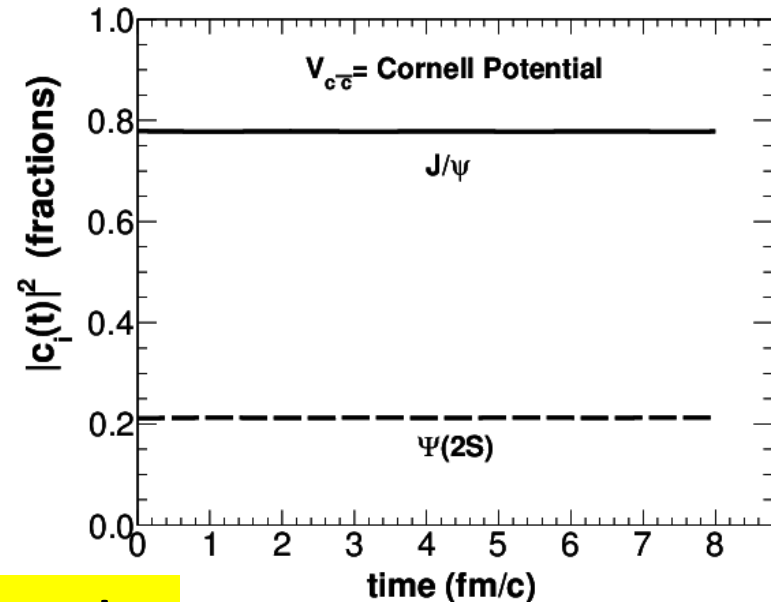
Initialization of $c\bar{c}$ wavefunction

◆ Evolutions of one $c\bar{c}$ with different potential



Testing codes

$$V_{c\bar{c}}(r) = 0$$



$$V_{c\bar{c}}(r) = \text{Cornell Potential}$$

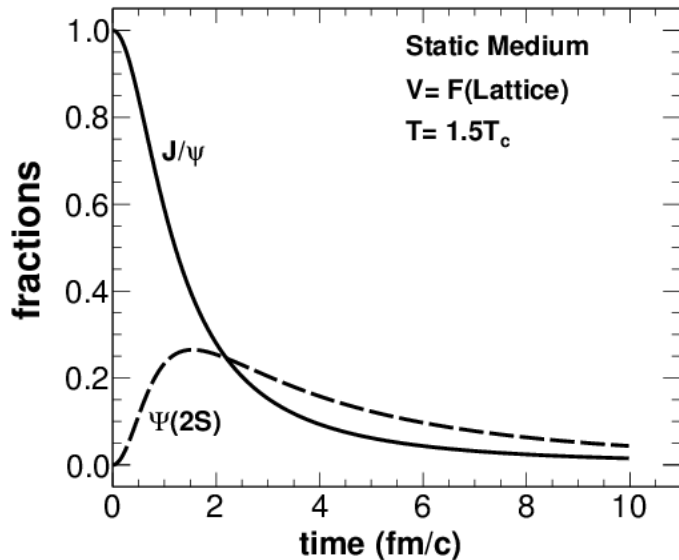
With weak potential, the $c\bar{c}$ dipole becomes a loosely bound dipole, its wavefunction expands outside.



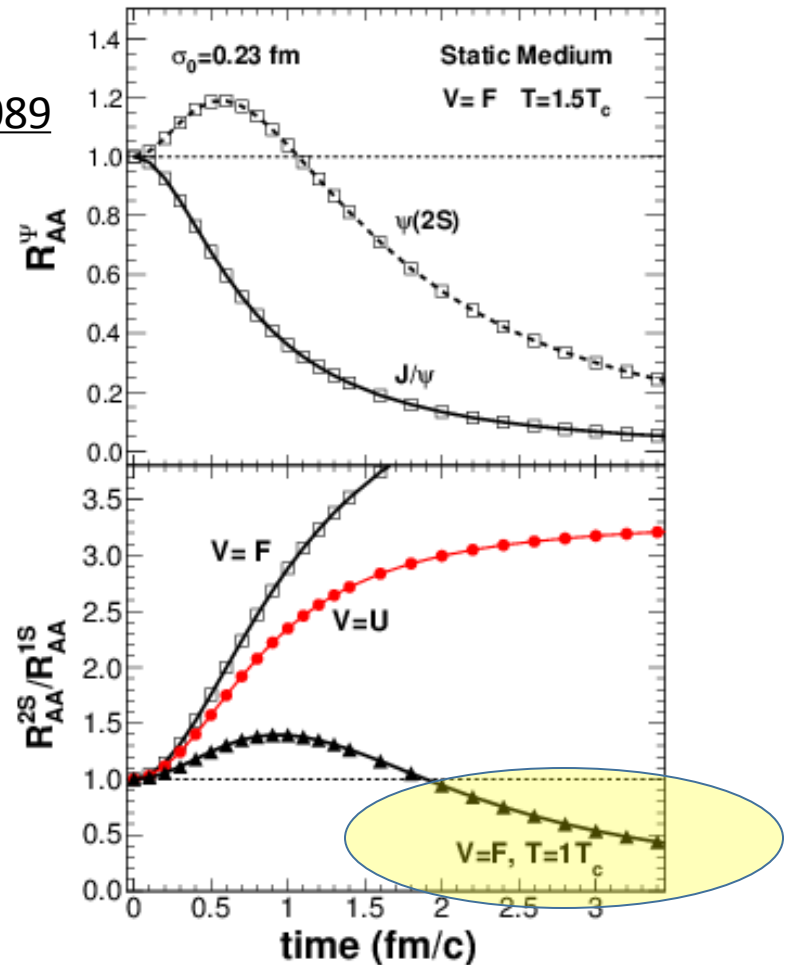
the overlap between $\psi_{c\bar{c}}(r, t)$ and $\Psi(2S)$ increase at first, then decrease

Heavy quark dipole in **Static Medium**

With real part of heavy quark potential (color screening)



[arXiv:1612.02089](https://arxiv.org/abs/1612.02089)



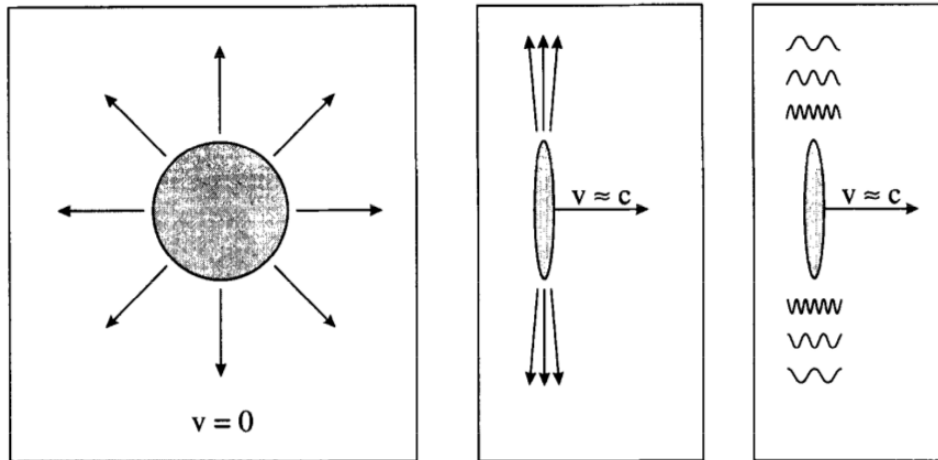
- At high T , Large density of partons, $c\bar{c}$ wavefunction expand outside, correspond transitions of $1S \rightarrow 2S$
- At low T , recovering of potential at mean radius of $1S$: $1S$ well constrained, mainly transitions of $2S \rightarrow 1S$

Additional parton inelastic scatterings may change the game.

4. Photoproduction from electromagnetic fields at $b < 2R_A$

Equivalent Photon Approximation

Prog.Part.Nucl.Phys. 39,503-564, 1997



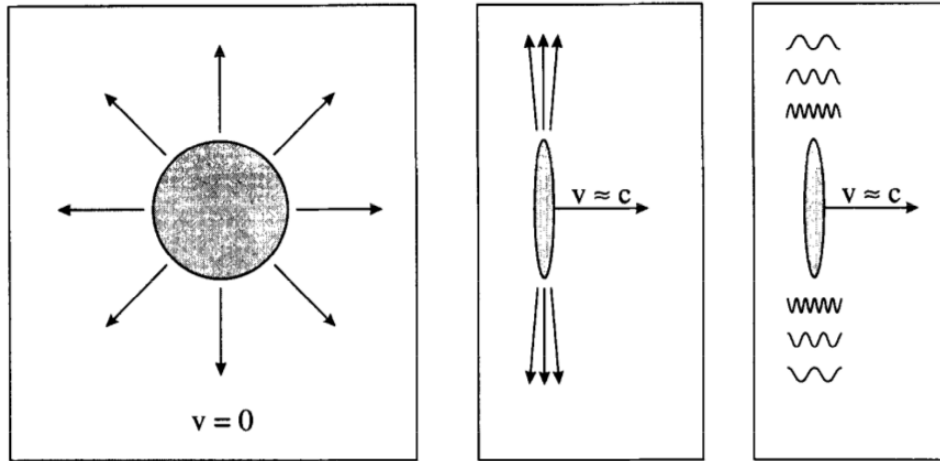
charges moves at nearly speed of light → produce E-B fields

Strong Lorentz-contracted **Electromagnetic field** (transverse)
approximated as longitudinally moving photons

Equivalent-Photon-Approximation
Fermi, 1924'

Equivalent Photon Approximation

Prog.Part.Nucl.Phys. 39,503-564, 1997

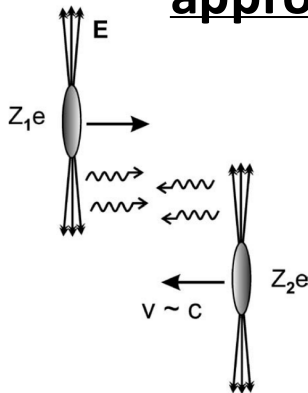


$$eB \sim m_\pi^2 \sim 10^{18} G$$

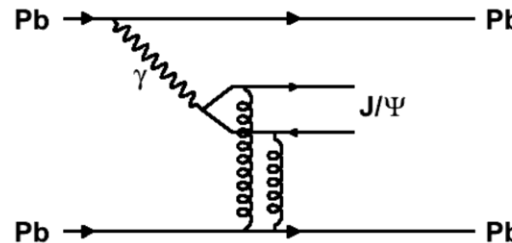
Ultra-peripheral collisions

charges moves at nearly speed of light → produce E-B fields

Strong Lorentz-contracted **Electromagnetic field** (transverse) approximated as **longitudinally moving photons**



Equivalent-Photon-Approximation
Fermi, 1924'



$$\gamma + A \rightarrow J/\psi + A$$

$$\gamma\gamma \rightarrow c\bar{c}(l\bar{l})$$

$$|\gamma\rangle = C_{\text{pure}}|\gamma_{\text{pure}}\rangle + C_{\rho^0}|\rho^0\rangle + C_\omega|\omega\rangle + C_\phi|\phi\rangle + C_{J/\psi}|J/\psi\rangle + \dots + C_{q\bar{q}}|q\bar{q}\rangle_{30}$$

p_T and b dependence

- Compare the p_T and b dependence of **coherent photoproduction and hadroproduction**

Charmonium hadro-production (**initial distributions**) in Pb-Pb collisions, can be extracted from the **scaling with pp collisions**.

Normalized distribution

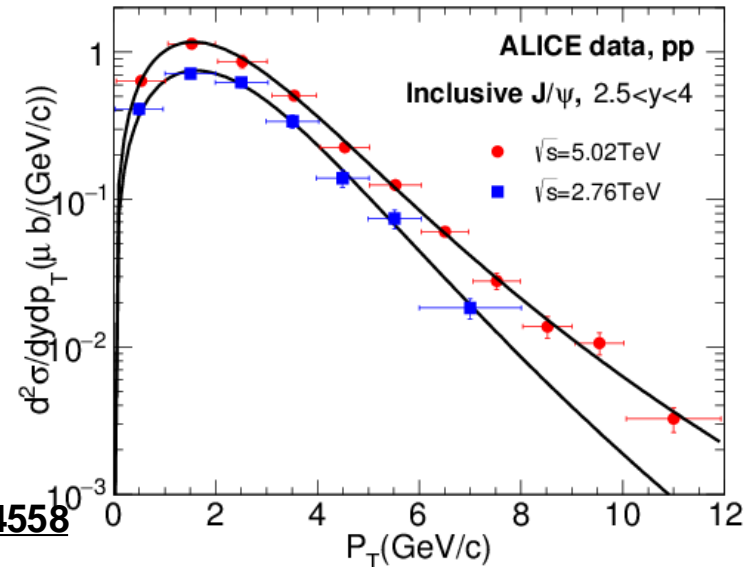
$$\frac{d\sigma_{pp}^{J/\psi}}{2\pi p_T dp_T} = \frac{2(n-1)}{2\pi(n-2) \langle p_T^2 \rangle_{pp}^{J/\psi}} \left[1 + \frac{p_T^2}{(n-2) \langle p_T^2 \rangle_{pp}^{J/\psi}} \right]^{-n}$$

Works well for RHIC and LHC

- **2.76 TeV forward rapidity $2.5 < y < 4$, inclusive J/ψ**
- $$\langle p_T^2 \rangle_{pp}^{J/\psi} = 7.8 \text{ (GeV/c)}^2$$
- $$n = 4$$

At $p_T \rightarrow 0$, $\frac{d\sigma_{pp}^{J/\psi}}{dp_T} \propto p_T$

Hadronic cross section drops to zero at $p_T \rightarrow 0$



J. Zhao, B. Chen, arXiv: 1705.04558
Physics Letters B 2017

p_T and b dependence

Fractions of hadronic cross sections in different p_T region

p_T range (GeV/c)	$\sigma_{p_{T1}-p_{T2}} / \sigma_{total}$
0 – 0.01	1.9×10^{-5}
0 – 0.05	4.8×10^{-4}
0 – 0.1	0.19%
0 – 0.5	4.5%
0 – 1	15%

Rapidity differential cross section at 2.76 TeV $2.5 < y < 4$

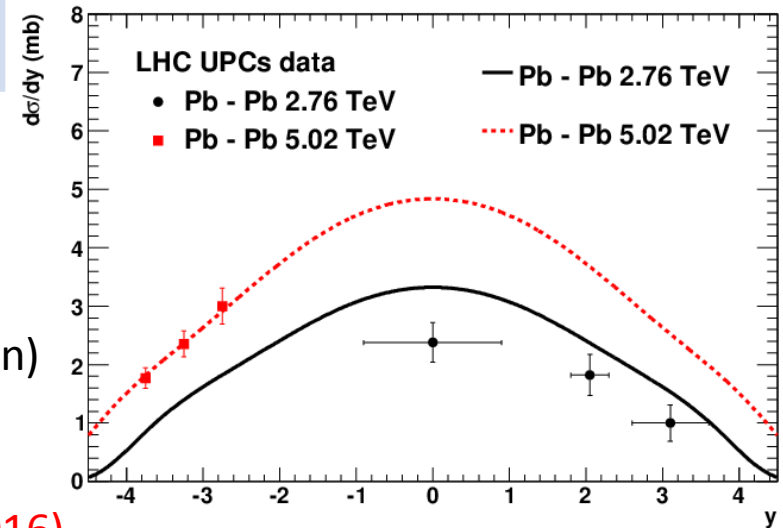
$$\frac{d\sigma_{pp}^{J/\psi}}{dy} = 2.3 \mu b$$

$$\frac{d^2\sigma_{pp}^{J/\psi}}{2\pi p_T dp_T dy} = \frac{d\sigma_{pp}^{J/\psi}}{2\pi p_T dp_T} \cdot \frac{d\sigma_{pp}^{J/\psi}}{dy}$$

Coherent photoproduction:
Photons interact with entire nucleus,

$$p_T \sim 1/R_A \sim 0.03 \text{ GeV/c}$$

Ultra-peripheral collisions
(photoproduction)



Exp. $\langle p_T \rangle = 0.055 \text{ GeV/c}$ PRL 116,, 222301 (2016)

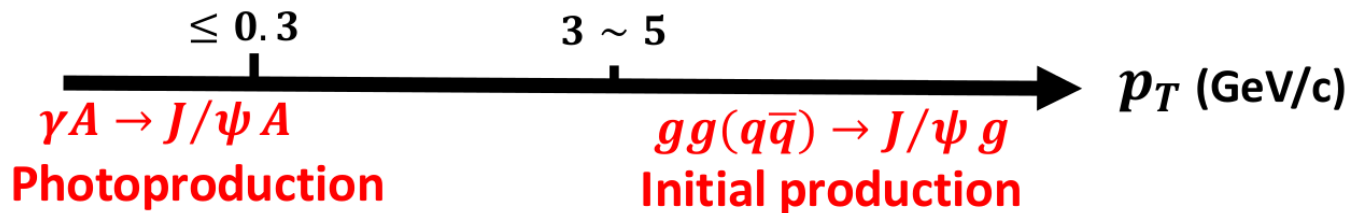
pT and b dependence

Hadronic initial yield
$$N_{AA}^{J/\psi} = \sigma_{pp}^{J/\psi} \int d^2x_T T_A(x_T) T_B(x_T - b)$$

$$= 30 \text{ fm}^{-2} (b = 10.2)$$

b=10.2 fm	Hadroproduction 2.5 < y < 4	photoproduction
0 < p _T < 0.04 GeV/c	0.47 × 10 ⁻⁵	5.54 × 10 ⁻⁵
0 < p _T < 0.1	2.4 × 10 ⁻⁵	15.7 × 10 ⁻⁵
0 < p _T < 0.5	50 × 10 ⁻⁵	~16 × 10 ⁻⁵
0 < p _T < 1	179 × 10 ⁻⁵	
0 < p _T < 3	772 × 10 ⁻⁵	

$c + \bar{c} \rightarrow J/\psi + g$
regeneration

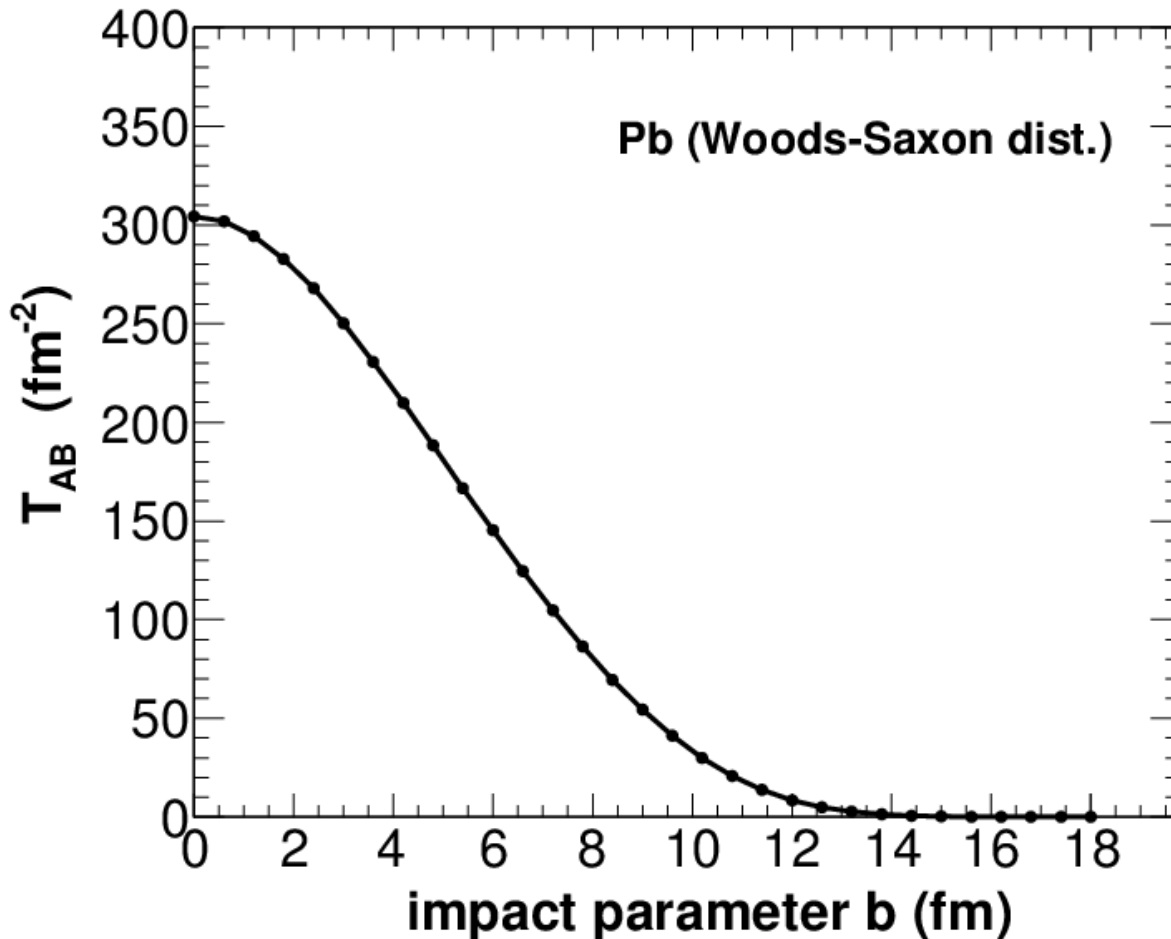


pT and b dependence

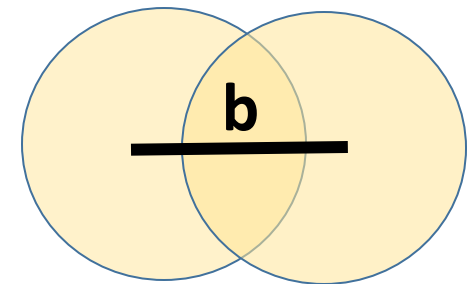
Hadronic initial yield

$$N_{AA}^{J/\psi} = \sigma_{pp}^{J/\psi} \int d^2x_T T_A(x_T) T_B(x_T - b)$$

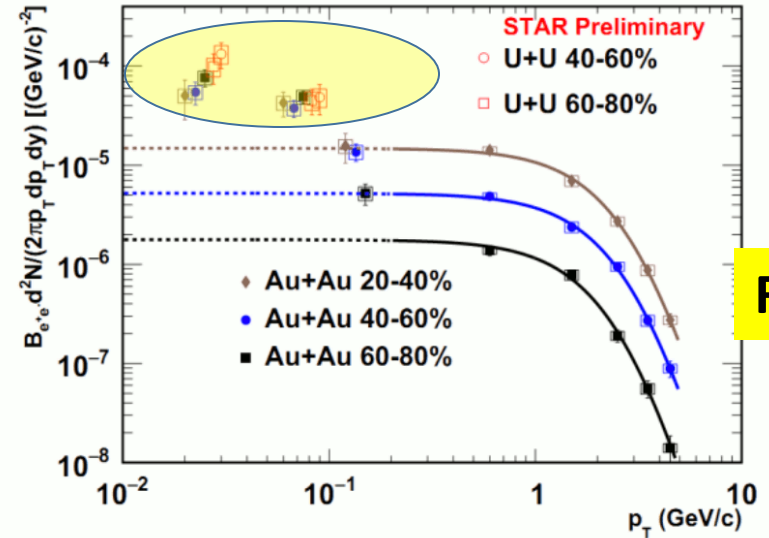
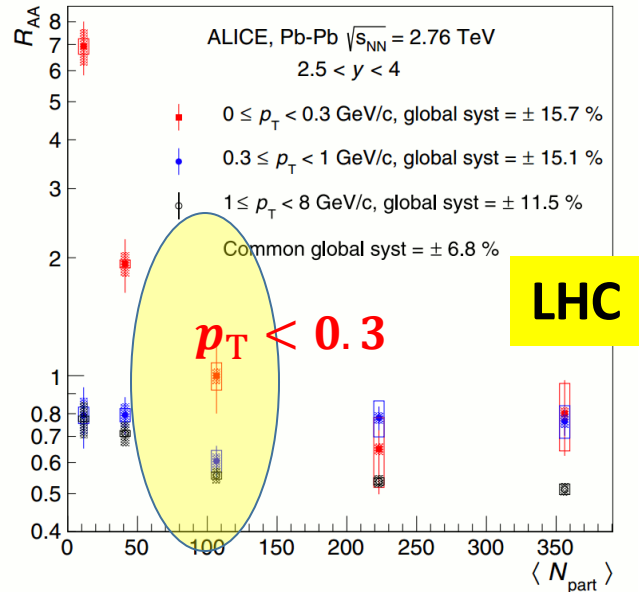
$$= 30 \text{ fm}^{-2} (b = 10.2)$$



Overlap area between two colliding nuclei,
~ the hadronic yields.



Photoproduction contribution



- Significant enhancement of J/ψ yield in low $p_T < 0.1$ GeV/c, and peripheral and semi-central collisions

- At $N_p=100$, $T_0^{QGP} = 2T_c$

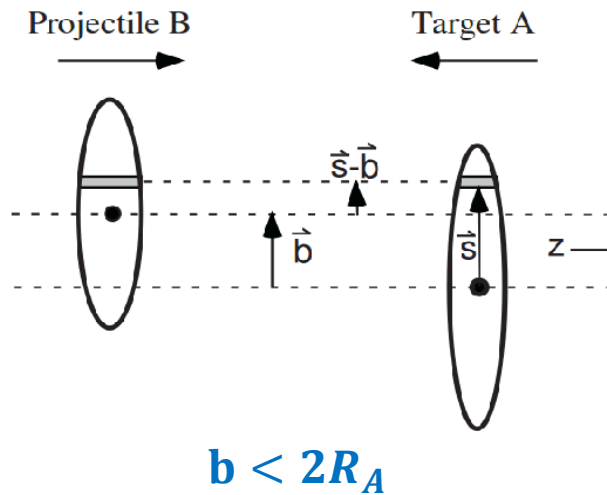
Similar with maximum T at RHIC Au-Au

QGP effect important !
Photoproduction important !

TABLE I: Information of QGP based on (2+1)D ideal hydrodynamics

Hydro in LHC $\sqrt{s_{NN}}=2.76$ TeV Pb-Pb, $2.5 < y < 4$			
b(fm)	N_p	T_0^{QGP}/T_c	τ_f^{QGP} (fm/c)
0	406	2.6	7.3
9	124	2.1	4.2
9.6	103	2.06	3.9
10.2	83	1.95	3.5
10.8	64	1.84	3.1

J/ψ from hadro-production and EB field



**Heavy quarks (and quarkonium)
+ light partons (QGP)**

Produced in the *overlap area*.

$$gg(q\bar{q}) \rightarrow J/\psi + g$$

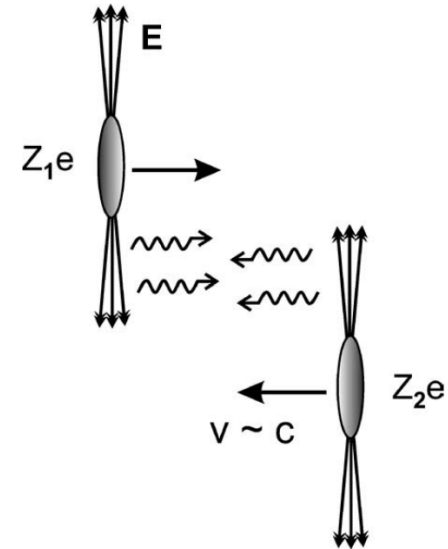
$$\rightarrow c + \bar{c}$$

Transport model (heavy quarkonium)

$$\frac{\partial f_\psi}{\partial t} + \frac{\vec{p}_\psi}{E} \cdot \vec{\nabla}_x f_\psi = -\alpha_\psi f_\psi + \beta_\psi$$

Hydrodynamics (light partons)

$$\partial_\mu T^{\mu\nu} = 0$$



Produced in the entire nucleus surface

$$\gamma A \rightarrow J/\psi A$$

$$N_\psi^{\gamma A} \propto \int dw \frac{dN_\gamma}{dw} \sigma_{\gamma A \rightarrow J/\psi A} \Gamma_{QGP}^{decay}$$

$$R_{AA} = \frac{N^{\gamma A} + N^{hadro}}{N^{hadro}}$$

J/ψ from electromagnetic field

Mainly three ingredients:

$$N_{\psi}^{\gamma A} \propto \int d\omega \frac{dN_{\gamma}}{d\omega} \sigma_{\gamma A \rightarrow J/\psi A} \Gamma_{QGP}^{decay}$$

Already Given before

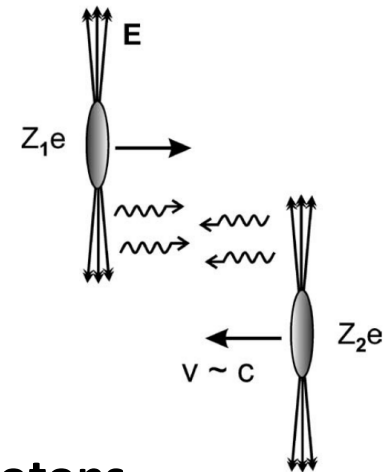
● Photon density $\frac{dN_{\gamma}}{d\omega}$ emitted by one nucleus

Poynting vector $\vec{S}(\vec{r}, t) = \vec{E}(\vec{r}, t) \times \vec{B}(\vec{r}, t) \xrightarrow{v \rightarrow c} |\vec{E}(\vec{r}, t)|^2 \vec{v}$

$$\int_{-\infty}^{\infty} dt \int d\vec{x}_{\perp} \cdot \vec{S}(\vec{r}, t) \stackrel{!}{=} \int_0^{\infty} d\omega \int d\vec{x}_{\perp} \omega n(\omega, \vec{x}_{\perp})$$

Energy flux of the fields

Energy flux of equivalent photons



$$\frac{dN_{\gamma}}{d\omega} = n(\omega) = \frac{1}{\pi\omega} \int d\vec{x}_T |\vec{E}_T(\vec{r}, \omega)|^2$$

$$= \frac{(Ze)^2}{\pi\omega} \int_0^{\infty} \frac{d^2\vec{k}_T}{(2\pi)^2} \left[\frac{F\left(\left(\frac{\omega}{v\gamma}\right)^2 + k_T^2\right)}{\left(\frac{\omega}{v\gamma}\right)^2 + k_T^2} \right]^2 \frac{k_T^2}{v^2}$$

Nuclear charge form factor is the **Fourier transform** of Woods-Saxon distribution

J/ψ from electromagnetic field

- Photon-nucleus cross section $\sigma_{\gamma A \rightarrow J/\psi A}$

Widely studied in UPC

Start from photon-proton $\sigma_{\gamma p}$

$$\sigma(\gamma A \rightarrow J/\psi A) = \frac{d\sigma(\gamma A \rightarrow J/\psi A)}{dt} \Big|_{t=0} \int_{-t_{min}}^{\infty} |F(t)|^2 dt$$

S.R.Klein, J. Nystrand, PRC, 1999

Physics Reports, G.Baur, et al, 2002

With the optical theorem, above cross section can be written as $J/\psi - A$ total cross section. With Geometry scale,

$$\sigma_{tot}(J/\psi A) = \int d^2 \vec{x}_T (1 - e^{-\sigma_{tot}(J/\psi p) T_A(\vec{x}_T)})$$

Using optical theorem again, and finally

$$\frac{d\sigma_{\gamma p \rightarrow J/\psi p}}{dt} \Big|_{t=0} = B_{J/\psi} X_{J/\psi} W_{\gamma p}^{\epsilon_{J/\psi}}$$

**Measured by HERA data.
(main input of photo-production)**

**Center of mass energy of
photon and proton**

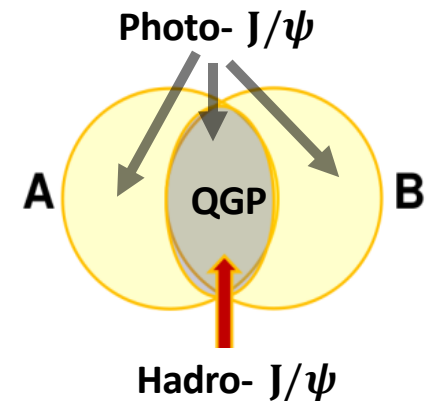
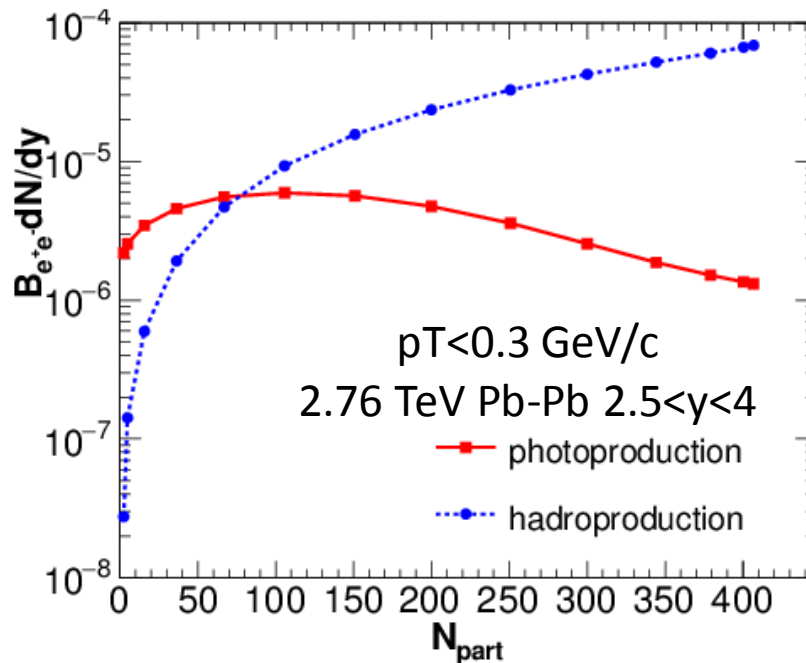
J/ψ from EB field + QGP

Our formula for J/ψ photo-production with QGP effect

$$\frac{dN_{J/\psi}}{dy}(y) = w \cdot \frac{1}{\pi R_A^2} \int_0^{R_A} r dr \int_0^{2\pi} d\phi \frac{d^3 r N_\gamma(w, b + r \cos(\phi))}{dw r dr d\phi} \sigma_{\gamma A \rightarrow J/\psi A}(w) \times e^{-\int_{\tau_0}^{\tau_f} d\tau \alpha_{QGP}(r, \phi, b, \tau)}$$

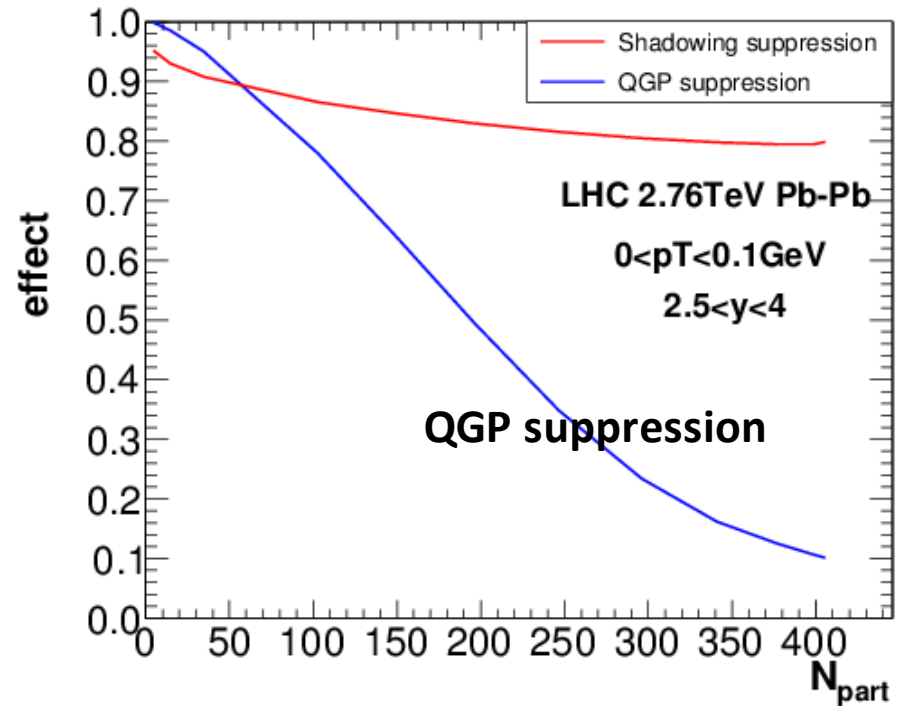
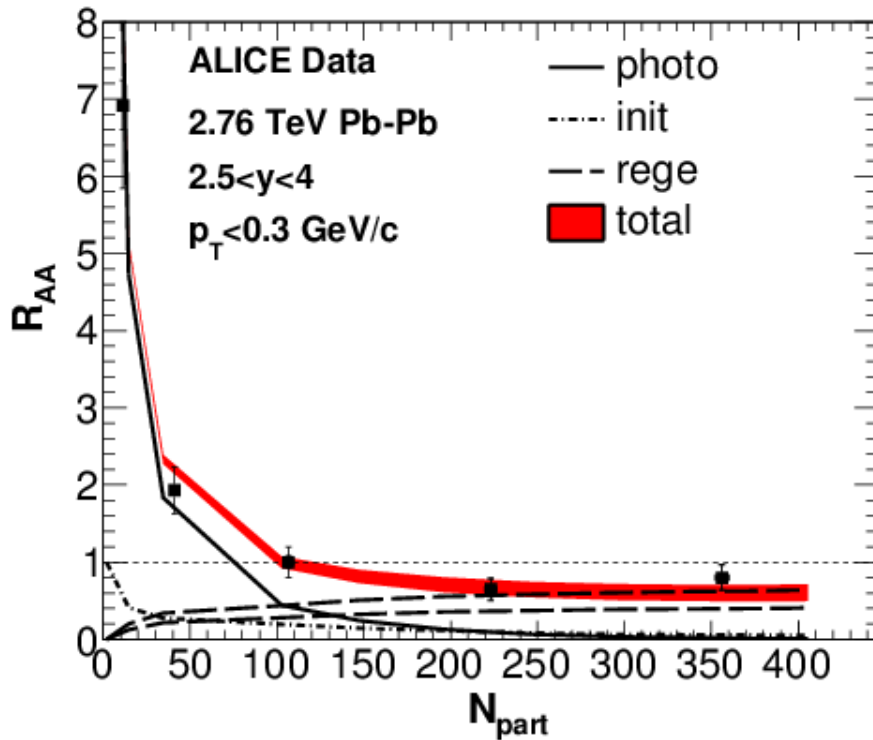
+ ($y \rightarrow -y$ term.)

Hadroproduction **V.S.**
Photoproduction
(without QGP Effect)



- hadroproduction show **strong dependence** on **impact parameter** (overlap between nucleus A and B).

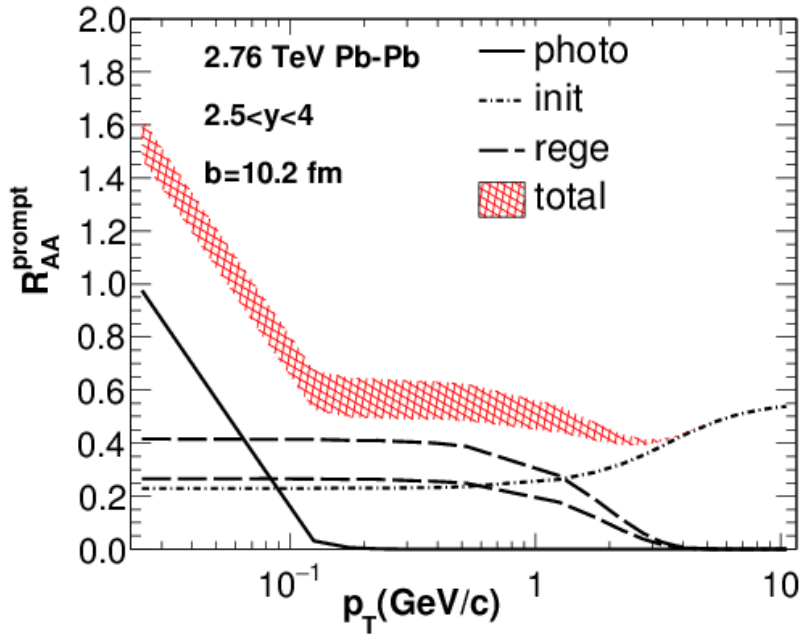
Total J/ψ from EB field + QGP



[W. Shi, W. Zha, B. Chen, arXiv:1710.00332](#)

- Also significant enhancement at $N_p \approx 100$, where $T_0^{QGP} = 2T_c$, similar with **RHIC 200 GeV Au-Au (most central)**
- When $N_{part} \rightarrow 0$ ($b > 2R_A$), **hadroproduction $\rightarrow 0$, photoproduction \rightarrow nonzero, $R_{AA} \rightarrow$ infinity**

Total J/ψ from EB field + QGP



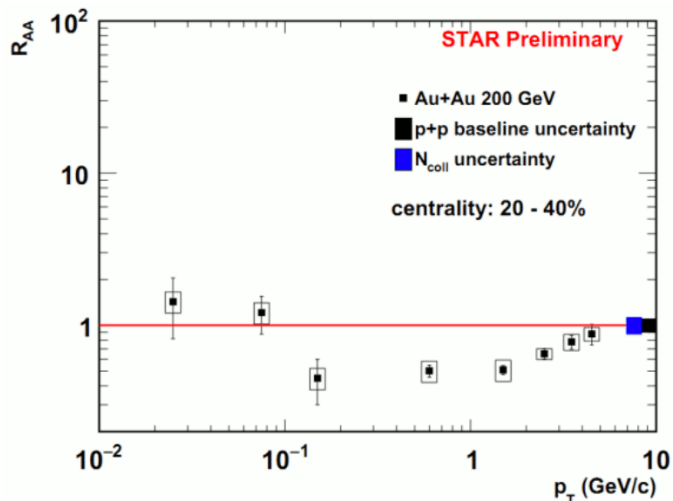
LHC

- $p_T < 0.05$, $\gamma A \rightarrow J/\psi$ A important
- $0.1 < p_T < 2-4$, $c + \bar{c} \rightarrow J/\psi + g$
- $p_T > 4$ primordial production

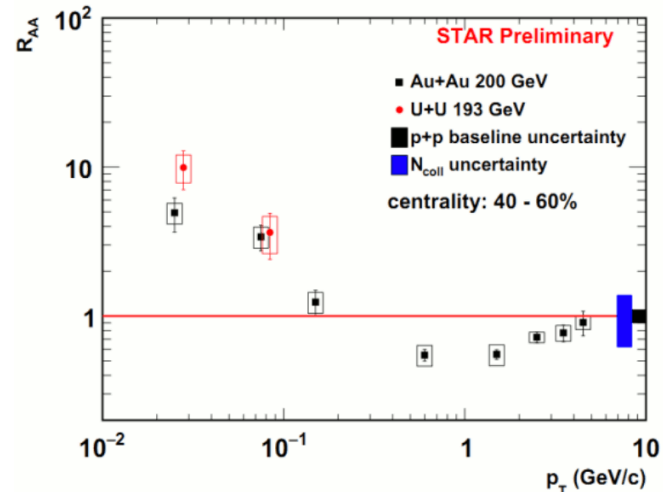
R_{AA} decreases, then increases with p_T

photoproduction \rightarrow rege. \rightarrow init.

[W. Shi, W. Zha, B. Chen, arXiv:1710.00332](https://arxiv.org/abs/1710.00332)



RHIC



Photoproduced 2S/1S

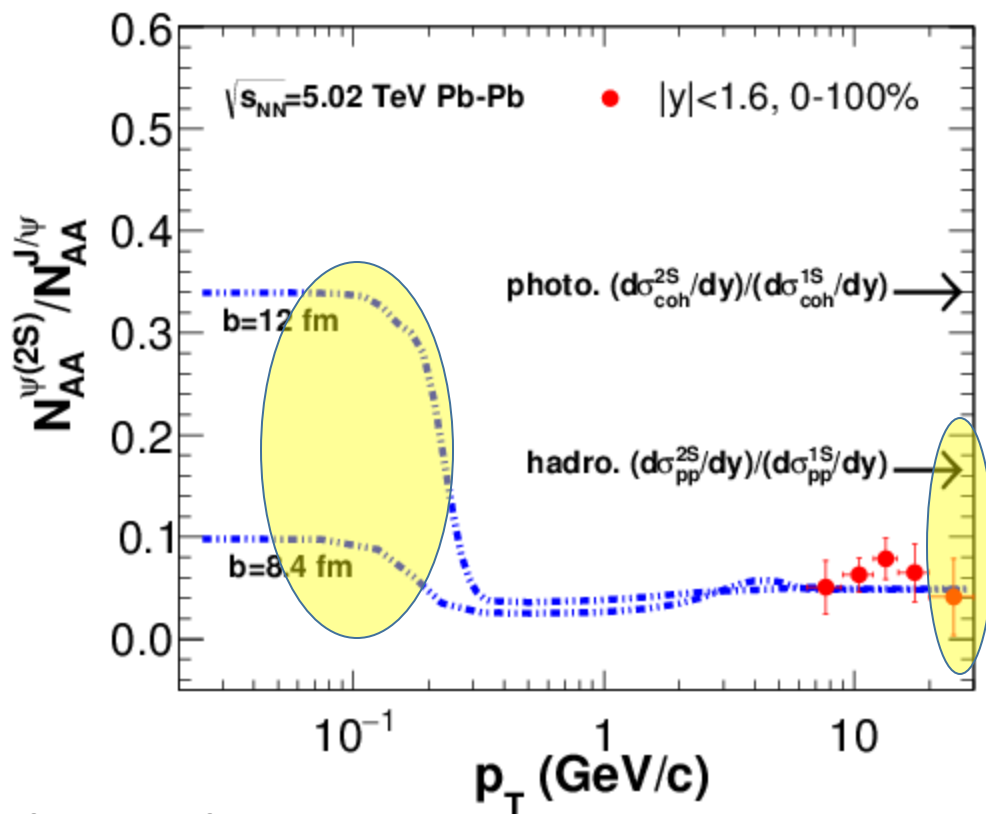
- Photoproduction is usually studied in Ultra-peripheral Collisions, absent of hadronic collisions and QGP

Can photoproduction and QGP be BOTH important ?

Photoproduced 2S/1S

- Photoproduction is usually studied in Ultra-peripheral Collisions, absent of hadronic collisions and QGP

Can photoproduction and QGP be BOTH important ?



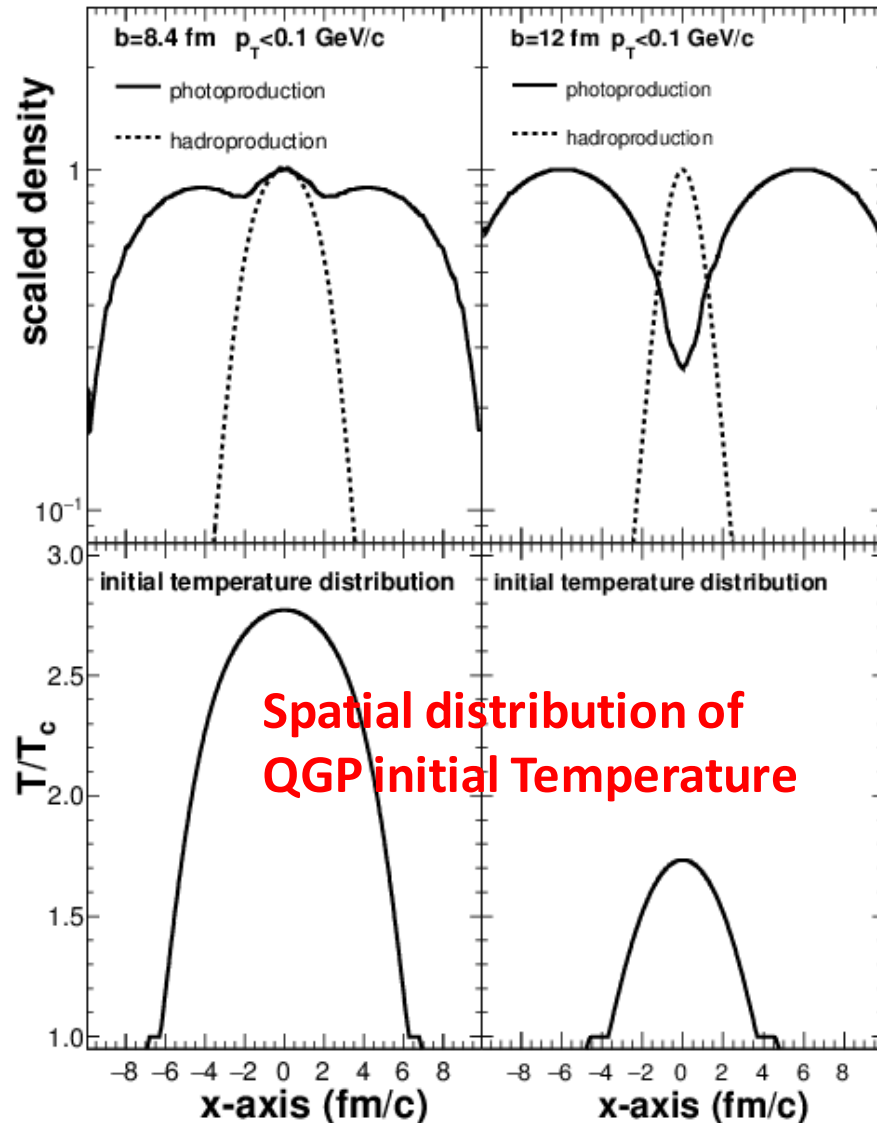
**Enhancement:
additional photoproduction on
both 1S and 2S**

Suppression: QGP effect.

Independent of initial nuclear effects

B.Chen, et al, in preparation

Photoproduced 2S/1S

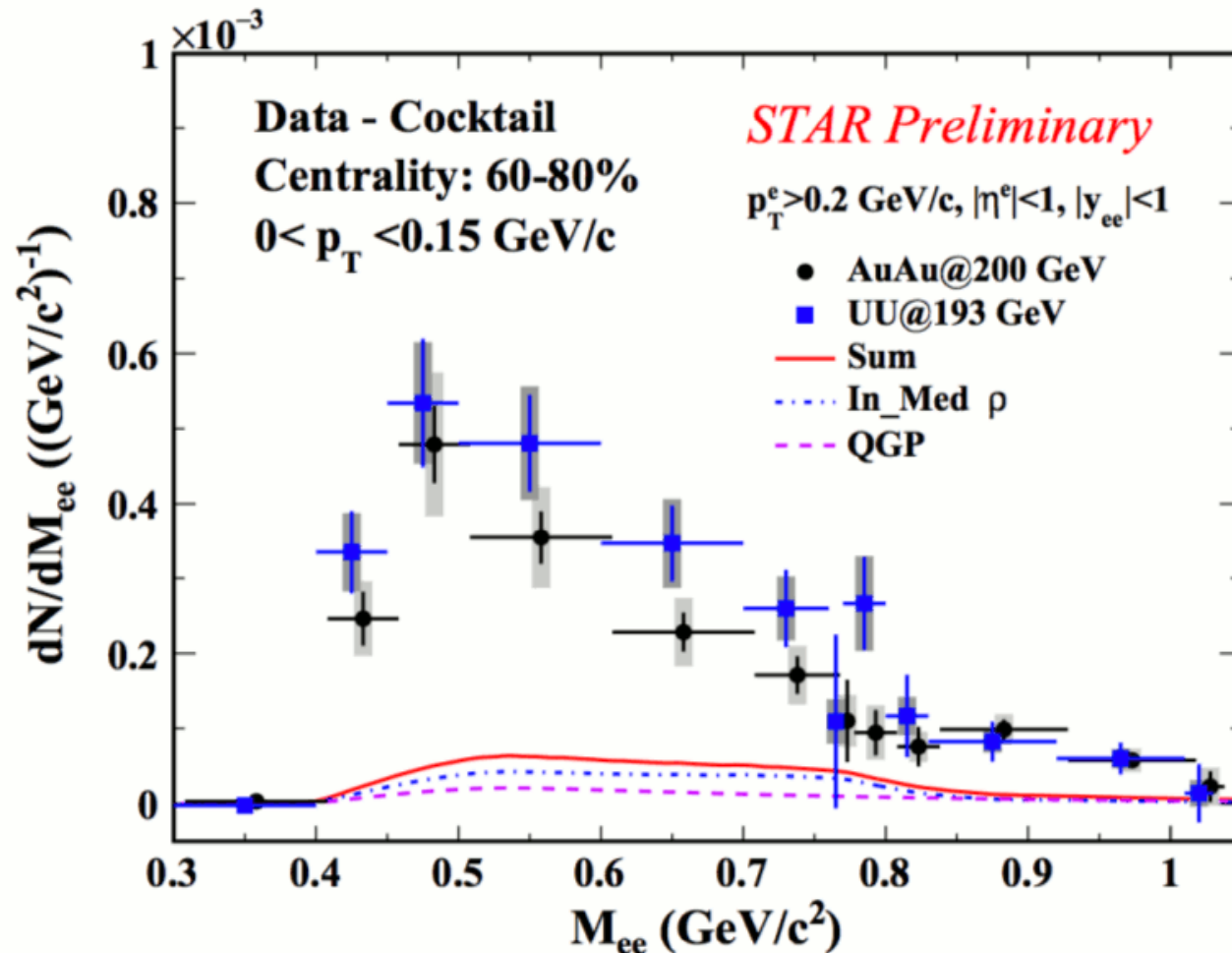


Spatial distribution of hadroproduction and coherent photoproduction

- **Hadroproduction:**
in the overlap area of two nuclei,
where QGP are also produced.
- **Photoproduction:**
over the entire nucleare surface
photons interact with entire nucleus

- 2S/1S shape needs 3 factors:**
- 1) QGP existence,
 - 2) abundant photoproduction,
 - 3) different spatial distributions

Photoproduction at RHIC



At RHIC, photoproduction from $\gamma + A \rightarrow \rho + A$, $\gamma\gamma \rightarrow e^+e^-$?

Summary

- ◆ We study the charmonium production in the heavy ion collisions with QGP. **When most of final charmonia are from c and \bar{c} combination, charmonia behavior is closely connected with charm diffusions in the expanding QGP.**
- ◆ $\psi(2S)$ production is an interesting topic, **and internal evolutions (transitions between 1S and 2S) should be crucial for 2S/1S observables**
- ◆ In the extremely low p_T regions, even at $b < 2R_A$, **photoproduction from strong electromagnetic fields can be larger than the hadroproduction in certain centralities.**
- ◆ We also propose the strong enhancement at $p_T < 0.1$ GeV/c and suppression at high p_T of 2S/1S, **to be an probe for both photoproduction and QGP effects**

Future interests:

electromagnetic fields induced particle production, EB-QGP, particle correlations, etc