

Fast Thermalization of Hadron Resonance Gas via Hagedorn states

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Transport Group Meeting



HGS-HIRe *for FAIR*
Helmholtz Graduate School for Hadron and Ion Research

The logo for HGS-HIRe for FAIR is contained within a dark blue rectangular box. The text "HGS-HIRe" is in a white sans-serif font, followed by "for FAIR" in a yellow, handwritten-style script font. Below this, the full name "Helmholtz Graduate School for Hadron and Ion Research" is written in a smaller white sans-serif font.

① Chemical equilibration in standard UrQMD

② Theory

③ HS properties

④ Dynamical Simulations

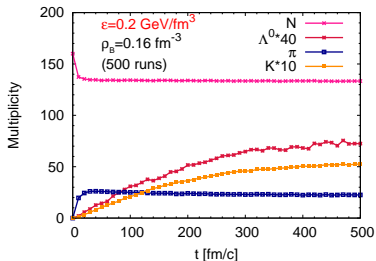
⑤ Summary and Outlook

UrQMD box simulation setup

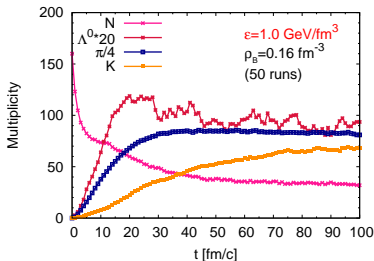
- cubic box with cyclic boundary conditions
- initial particles: 80 n + 80 p
- uniform distribution in configuration and momentum space
- string production disabled
- fixed $\rho_B = 0.16 \text{ fm}^{-3}$ and $\rho_S = 0 \text{ fm}^{-3}$
- energy density $\epsilon = 0.2 \text{ GeV}/\text{fm}^3$ (500 runs)
- energy density $\epsilon = 1.0 \text{ GeV}/\text{fm}^3$ (50 runs)

Chem. Equil. in UrQMD (box) too long

cf. M. Belkacem et al., PRC 58 (1998) 1727
see also E. Bratkovskaya et al., NPA 675 (2000) 661



$$t_\pi \approx 20 \text{ fm/c}$$
$$t_N \approx 15 \text{ fm/c}$$
$$t_\Lambda > 300 \text{ fm/c}$$
$$t_K > 400 \text{ fm/c}$$



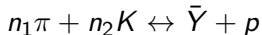
$$t_\pi \approx 20 \text{ fm/c}$$
$$t_N \approx 15 \text{ fm/c}$$
$$t_\Lambda > 40 \text{ fm/c}$$
$$t_K > 90 \text{ fm/c}$$

Application of Hagedorn States (HS) I:

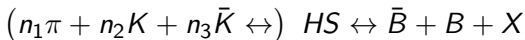
J. Noronha-Hostler, C. Greiner, I. A. Shovkovy., PRL 100

(2008) 252301

- SPS energies: strong increase of antiprotons/antihyperons through 'clustering' of mesons



- chemical equilibration time of $t_{\text{eq}} \approx 1 - 3 \text{ fm}/c$
- RHIC energies: $t_{\text{eq}} \sim 10 \text{ fm}/c$ for antibaryons
- quick chemical equilibration mechanism through HS

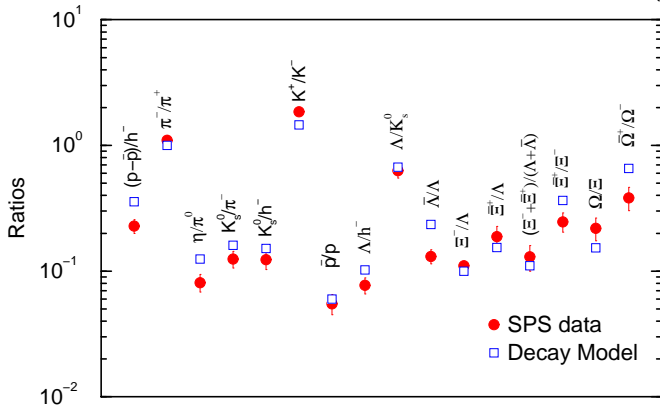


- dynamical evolution through set of coupled rate equations
- HS and pions in equilibrium $\rightarrow t_{\text{eq}} \approx 5 \text{ fm}/c$ for $B\bar{B}$ -pairs

Application of Hagedorn States (HS) II:

S. Pal, P. Danielewicz, Phys.Lett. B627 (2005) 55

- statistical model for decay and formation of HS
- Hagedorn Temperature of $T_H \simeq 170$ MeV
- subsequent decay of one single heavy resonance (HS)



Intention: Hagedorn States in UrQMD

- UrQMD = Ultrarelativistic Quantum Molecular Dynamics (S. A. Bass et al., Prog.Part.Nucl.Phys. 41 (1998) 225)
- microscopic transport model for p+p, p+N and A+A for Bevalac and SIS up to AGS, SPS and RHIC energies
- **detailed balance**
 - is enforced: meson-baryon, meson-meson, resonance-nucleon, resonance-resonance
 - is violated by string and some hadron decays ($\omega \rightarrow 3\pi$)
- for $\sqrt{s} \geq 2.5 - 10 \text{ GeV}$: **HS production replaces strings**

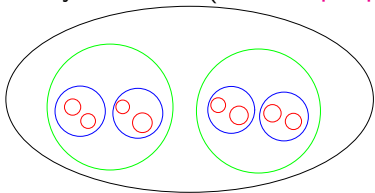
Observables:

- particle multiplicities
- chemical equilibration times
- estimates for $\frac{\eta}{s}$ (shear viscosity over entropy density)
- ...

Origin of Hagedorn states

1965: Rolf Hagedorn postulates "Statistical Bootstrap Model"
(R. Hagedorn, Nuovo Cim.Suppl. 3 (1965) 147-186)

- highly excited lumps of matter are not essentially different from observed hadronic resonances at lower excitation
- fireballs and their constituents are the same
- nesting fireballs into each other leads to self-consistency condition (**bootstrap-equation**)



- solution: "Hagedorn Spectrum", exponentially rising

Spectrum τ and Decay Width Γ of HS

$$\tau_{\vec{C}}(m) = \frac{R^3}{3\pi m} \sum_{\vec{C}_1, \vec{C}_2} \int_{m_1^0}^m dm_1 \int_{m_2^0}^{m-m_1} dm_2 \tau_{\vec{C}_1}(m_1) m_1$$

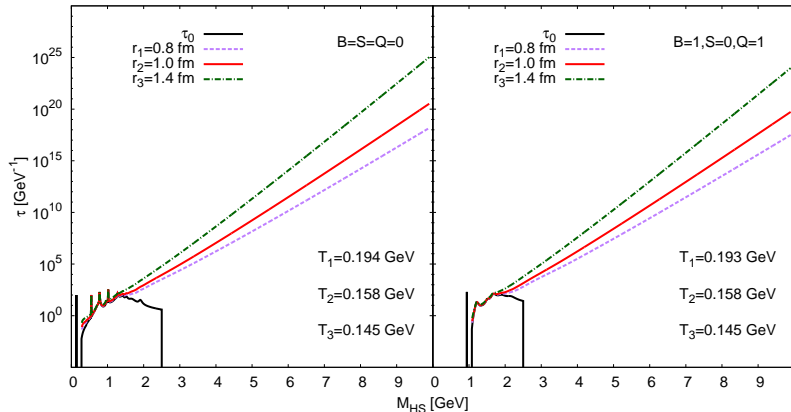
$$\times \tau_{\vec{C}_2}(m_2) m_2 p_{cm}(m, m_1, m_2) \delta_{\vec{C}, \vec{C}_1 + \vec{C}_2}^{(3)}$$

$$\Gamma_{\vec{C}}(m) = \frac{\sigma}{2\pi^2 \tau_{\vec{C}}(m)} \sum_{\vec{C}_1, \vec{C}_2} \int_{m_1^0}^m dm_1 \int_{m_2^0}^{m-m_1} dm_2 \tau_{\vec{C}_1}(m_1) \tau_{\vec{C}_2}(m_2)$$

$$\times p_{cm}(m, m_1, m_2)^2 \delta_{\vec{C}, \vec{C}_1 + \vec{C}_2}^{(3)}$$

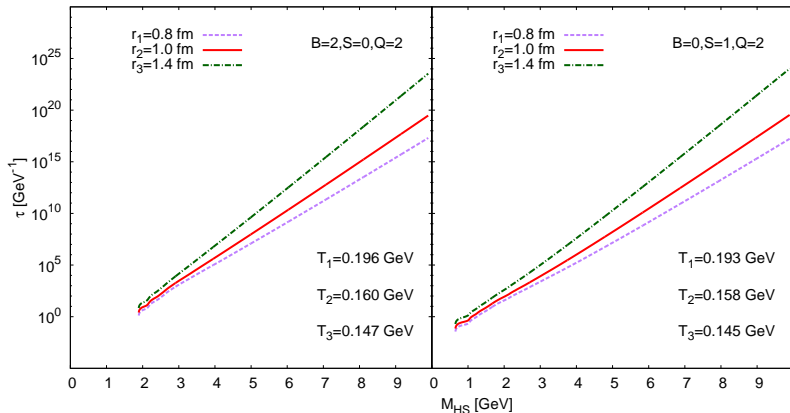
- τ : spectra at masses m and charges $\vec{C} = (B, S, Q)$
- R : HS (spherical) radius and σ : HS creation cross section
- p_{cm} momenta of decay products in rest frame of decaying HS

Mes. (l) and bar. (r) Hagedorn Spectra



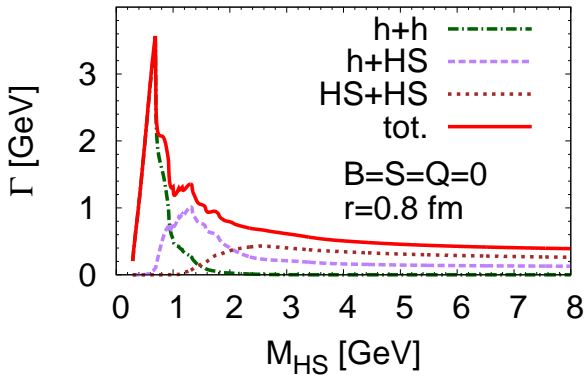
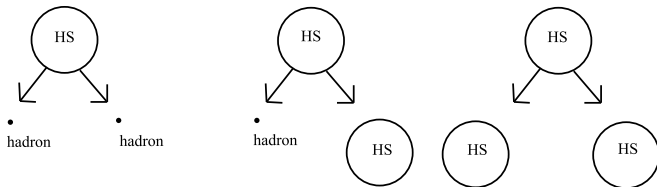
fit function: $f(m) = cm^a \exp\left(\frac{m}{T}\right)$

Exotic Hagedorn Spectra

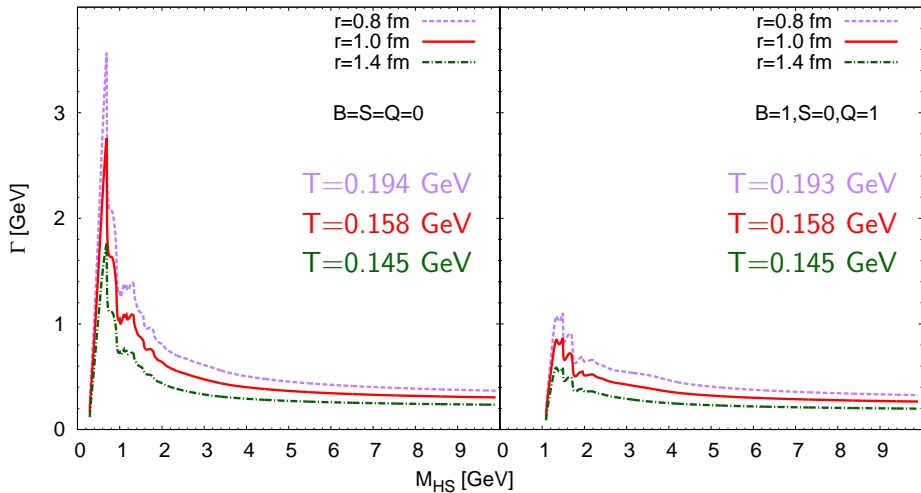


fit function: $f(m) = cm^a \exp\left(\frac{m}{T}\right)$

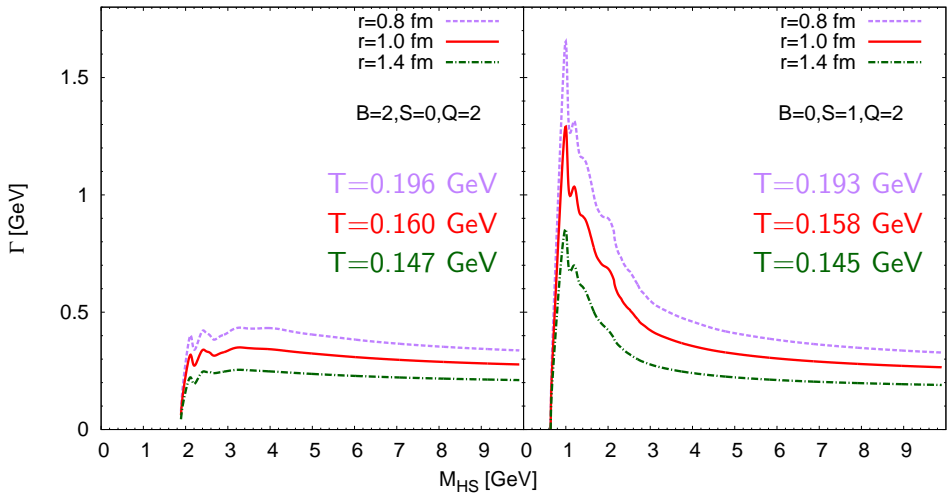
Hagedorn state decay modes



Decay Width for mes. (l) and bar. (r) HS



Decay Width for exotic HSs



Concept of Hagedorn State Gas

- HS appear most abundantly near Hagedorn temperature T_H
- HS - a **microscopic** tool for hadronization

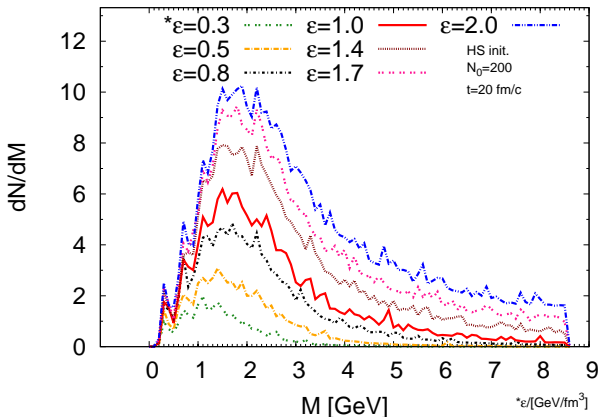
Scenario:

- QGP drop expands, cools and decays/dissolves into QGP droplets/HS
- assembly (gas) of HS is created and begins to evolve
- HS propagate, rescatter and **decay** into two **hadrons**, two (lighter) HS or one (lighter) and one **hadron**
- hadrons and HS collide elastically and **inelastically** and create (repopulate) new HS
- for all $h + h, HS + HS, h + HS \leftrightarrow HS$ inelastic collisions **detailed balance** holds
- dynamical, microscopical interplay between hadrons and/or HS drives hadrons and HS into **thermal** equilibrium

Simulation setup

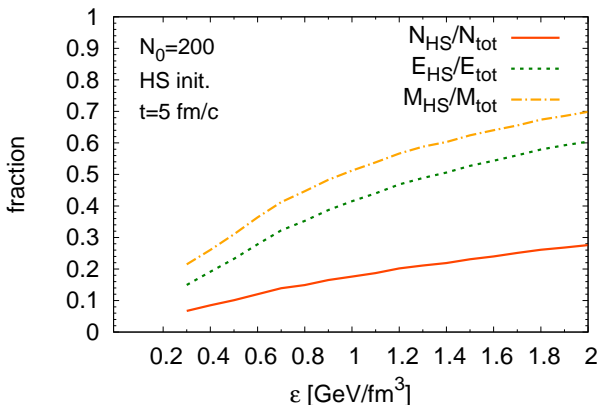
- cubic UrQMD box, volume $V = 1000 \text{ fm}^3$ and reflecting walls
- energy density ($E_{tot.}/V$) range $\epsilon = 0.2 - 2.0 \text{ GeV}/\text{fm}^3$
- number of initial HS $N_0 = 200$ with $\vec{C}_i = (0, 0, 0)$
- masses of initial HS range $m = 0.3 \text{ GeV} - 8.6 \text{ GeV}$, sampled uniformly
- uniform sampling of positions and momenta of the initial HS, ensures **non-equilibrated** system
- total momentum \vec{p} ($= 0$), total energy E and total charges \vec{C} conserved exactly
- overall charge $\vec{C} = (0, 0, 0)$, whereas during simulation particles (hadrons and **HS**) with $\vec{C}_j \neq (0, 0, 0)$ appear too

Hagedorn state mass distribution



convolution of Boltzmann distribution $f \sim \exp(E/T)$ with Hagedorn spectrum $\tau \sim \exp(m/T_H)$

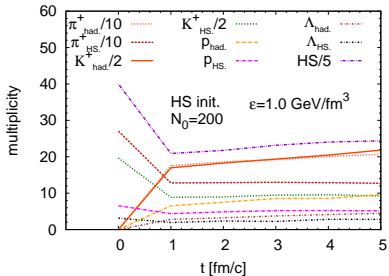
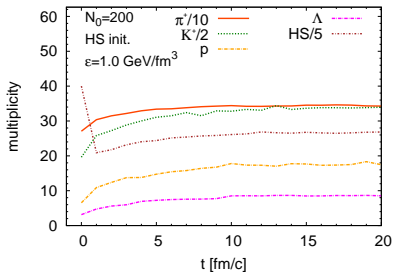
Impact of HS on the system



for $t \geq 5$ fm/c and $\epsilon = 2.0$ GeV/fm³

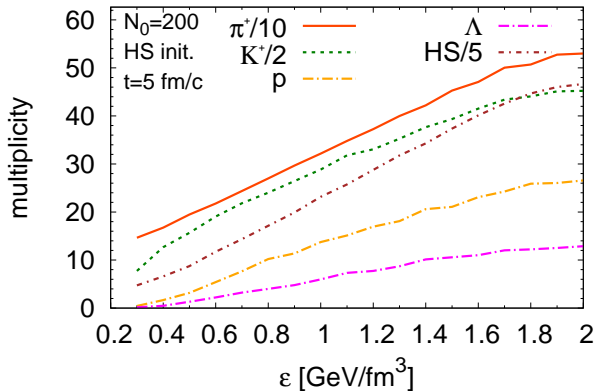
- every fourth particle is a HS
- $\sim 60\%$ of total energy and $\sim 70\%$ of total mass stored in HS

Multiplicity time evolution



- chem. equilibration of total multiplicities (left) within first $t < 3$ fm/c for all species
- initial HS decays (right) provide therm. equilibration almost immediately

Multiplicity energy density dependence



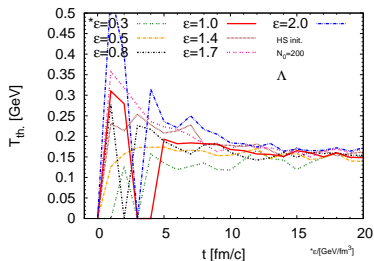
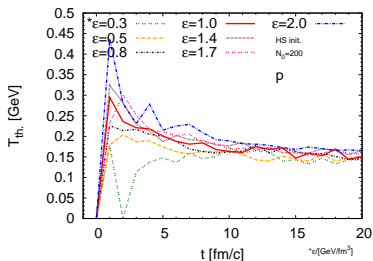
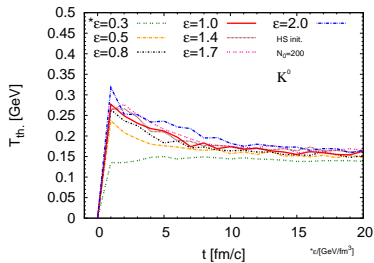
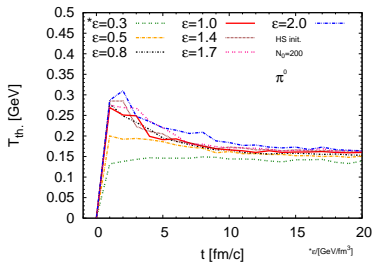
- yields determined by particle's masses, since $\vec{C} = (0, 0, 0)$ holds
- HS multiplicity has steepest slope in accordance to SBM

Comparison to experiment

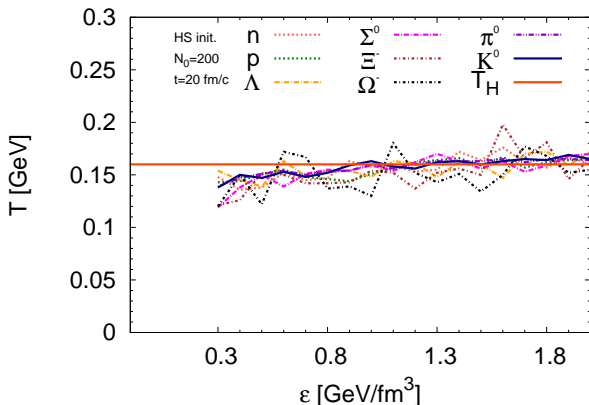
	p-p	Pb-Pb	0.3	0.8	1.0	2.0
K^-/π^-	0.123(14)	0.149(16)	0.192	0.197	0.193	0.185
\bar{p}/π^-	0.053(6)	0.045(5)	0.015	0.049	0.052	0.060
Λ/π^-	0.032(4)	0.036(5)	0.007	0.022	0.024	0.029
Λ/\bar{p}	0.608(88)	0.78(12)	0.475	0.456	0.469	0.499
$\Xi^-/\pi^- * 10^3$	3.000(1)	5.000(6)	1.565	6.492	5.769	7.106
$\Omega^-/\pi^- * 10^3$	-	0.87(17)	0.137	0.815	0.823	0.994

- p-p data at $\sqrt{s_{NN}} = 0.9$ TeV (K. Aamodt et al. (ALICE Collaboration), Eur. Phys. J. C 71, 1594 (2011)).
- Pb-Pb data at $\sqrt{s_{NN}} = 2.76$ TeV (B. B. Abelev et al. (ALICE Collaboration), Phys. Rev. Lett. 111, 222301 (2013))
- error denote experimental error in the last digits
- simulated ratios for $t = 20$ fm/c for energy densities $\epsilon = 0.3, 0.8, 1.0, 2.0$ GeV/fm³

Temperature evolution of hadrons



Temperature energy density dependence



- temperature dependence independent of particle species
- (Boltzmann) temperature tend to limiting value
- accordance to SBM: $\lim_{\epsilon \rightarrow \infty} T = T_H$.

Summary and Outlook

- chem. equilibration times in (standard) UrQMD (box) too long
- presentation of Hagedorn spectra and HS total decay widths
- presentation of microscopic box simulation results (HS mass distribution, HS fraction on total energy, mass etc.)
- hadronic yield and temperature time evolutions
- thermalization of all hadrons with $t \leq 3 \text{ fm}/c$
- comparison of multiplicity ratios with the experiment

- investigation of net-baryon fluctuations
- impact of HS on η/s in UrQMD
- extension of HS dynamics on heavy ion collision simulations