

Hanbury-Brown Twiss

Results from UrQMD

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for Advanced Studies



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HIC
for **FAIR**
Helmholtz International Center

H-QM | Helmholtz Research School
Quark Matter Studies

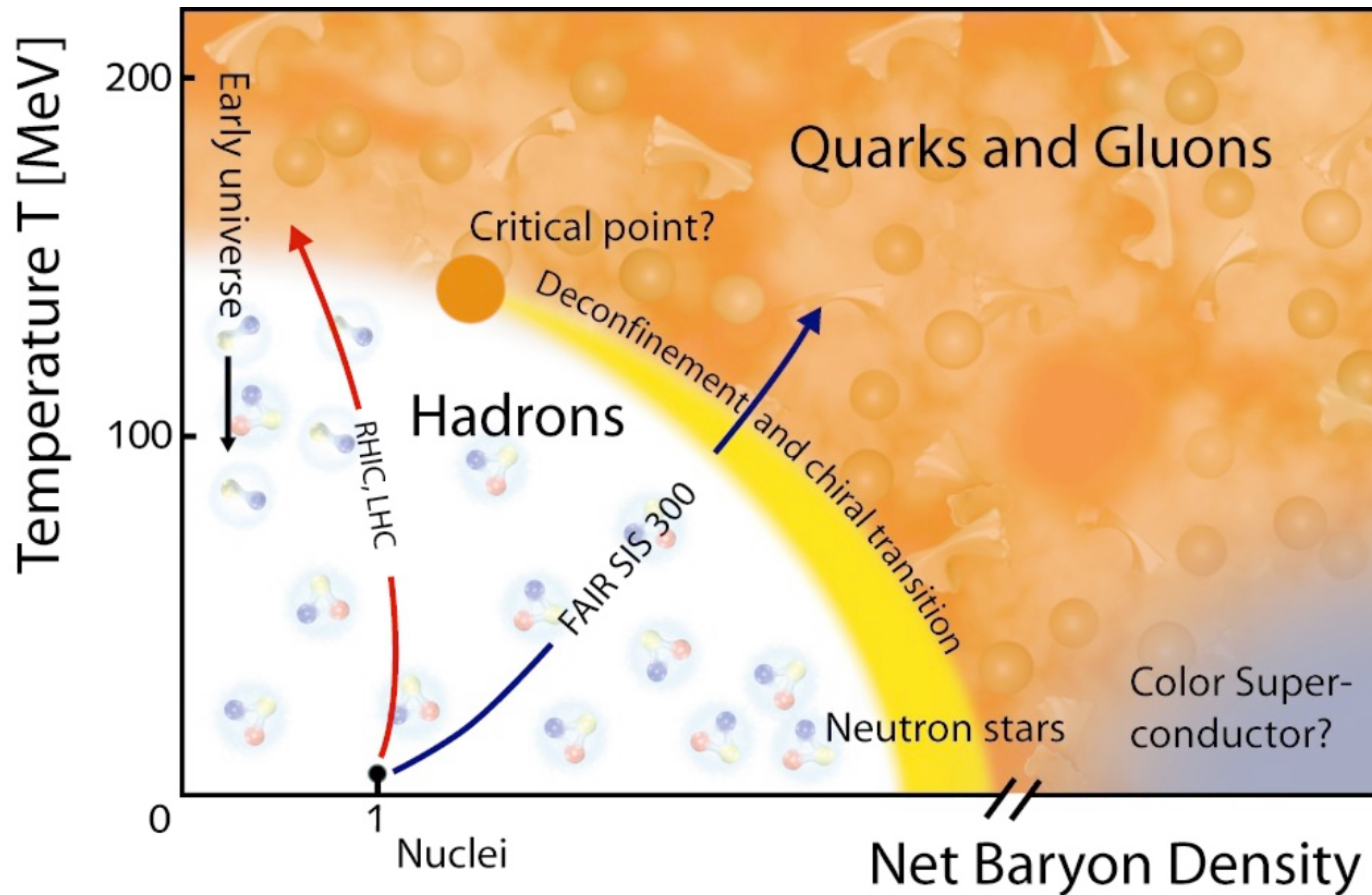


Outline

- General introduction to HBT
- Results & Techniques
 - Hadron formation time
 - Particle emission duration
 - Multiplicity scaling
 - Measuring a twisted emission geometry



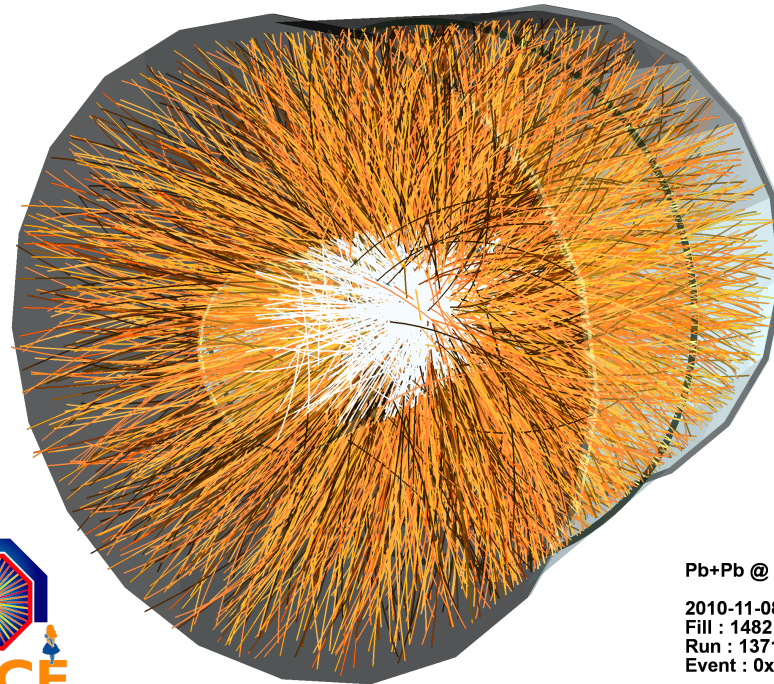
The strong interaction



Our probes

Momentum space and multiplicity observables:

- Flow (v_1, v_2, \dots, v_n)
- R_{AA}
- Rapidity spectra
- p_{\perp} spectra
- Particle ratios
- \vdots



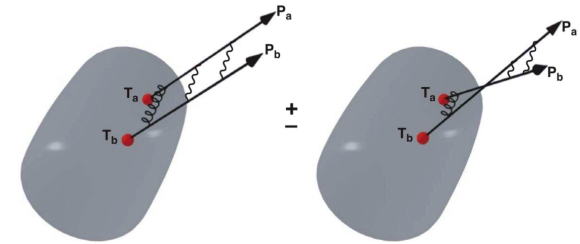
Pb+Pb @ sqrt(s) = 2.76 ATeV
2010-11-08 11:30:46
Fill : 1482
Run : 137124
Event : 0x00000000D3BBE693

- **Shape & Time \leftrightarrow HBT interferometry**

Hanbury-Brown Twiss technique

HBT connects momentum space to position space

$$C(q) = \frac{\int d^4x_1 d^4x_2 S(p_1, x_1) S(p_2, x_2) |\psi_{12}|^2}{\int d^4x_1 d^4x_2 S(p_1, x_1) S(p_2, x_2)}$$



$$\psi_{12} = \frac{1}{\sqrt{2}} \left[e^{ip_1(x'_1 - x_1)} e^{ip_2(x'_2 - x_2)} + e^{ip_2(x'_2 - x_1)} e^{ip_1(x'_1 - x_2)} \right]$$

$$C(q) = 1 + \langle \cos(x_\mu q^\mu) \rangle$$

$$q^\mu = p_1^\mu - p_2^\mu$$

$$x^\mu = x_1^\mu - x_2^\mu$$

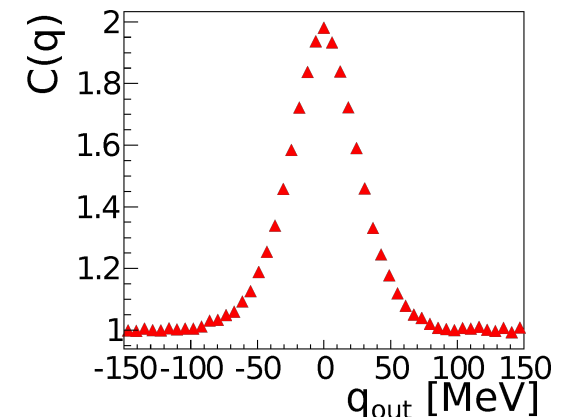
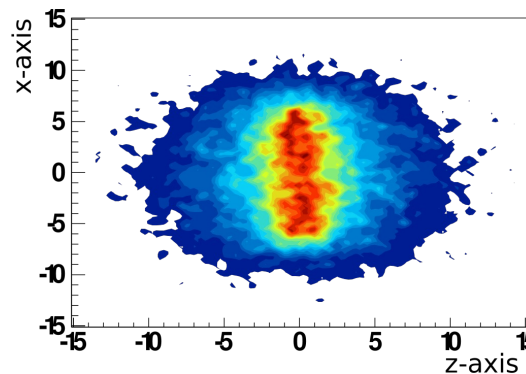
Gaussian shape

$$S(p, x) = S(p) e^{-\frac{x_\mu x_\nu}{2R_{\mu\nu}^2}}$$

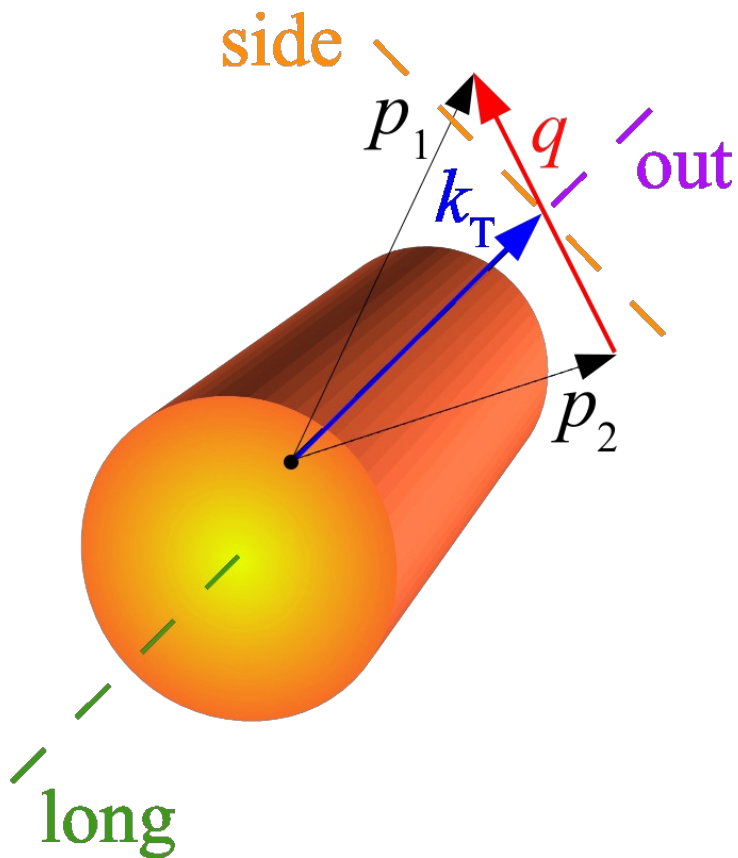
$$C(q) = 1 + \lambda e^{-q_\mu q_\nu R^{\mu\nu 2}}$$

Freeze-out distribution

Correlation function



The Out-Side-Long system



Out: In transverse momentum direction

Long: Along the beam axis

Side: Orthogonal to the other directions

K_T : Transverse pair momentum

q : Pair momentum difference

$$R_o^2 = \langle (x_o - \beta_o t)^2 \rangle$$

$$= \langle x_o^2 \rangle - 2 \langle \beta_T t x_o \rangle + \langle \beta_T^2 t^2 \rangle$$

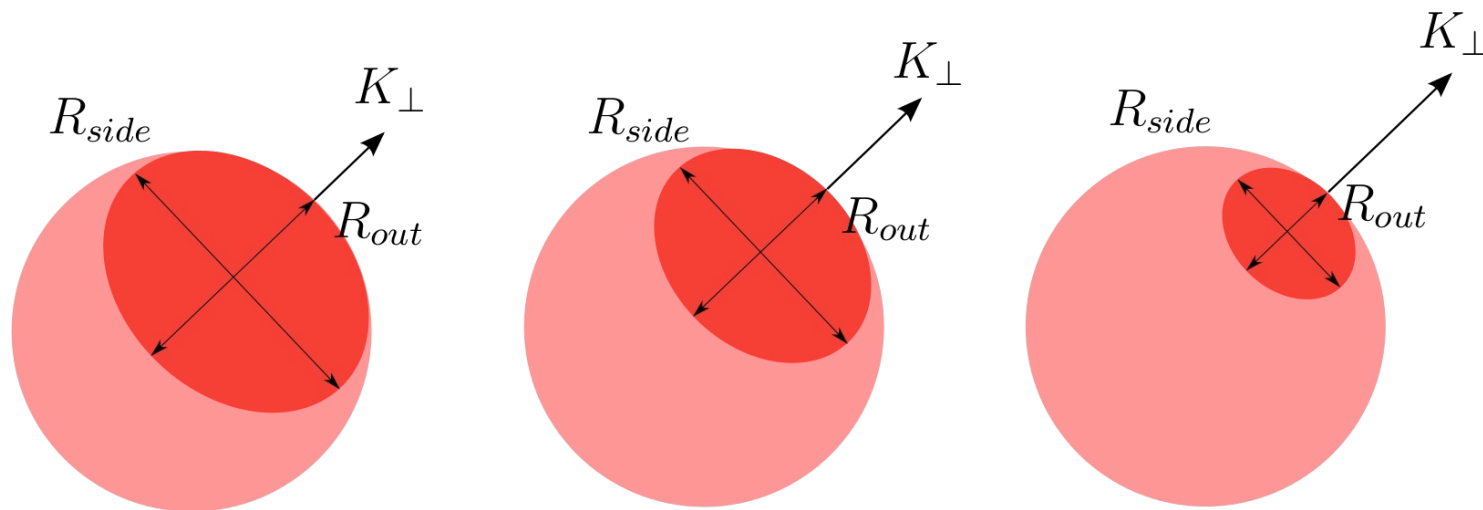
$$R_s^2 = \langle x_s^2 \rangle$$

$$R_l^2 = \langle x_l^2 \rangle$$

Region of homogeneity

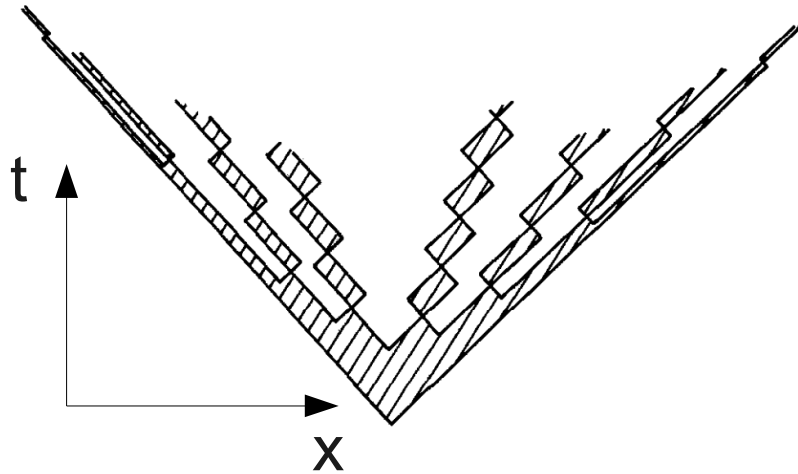
$$C(q) = 1 + \langle \cos(x_\mu q^\mu) \rangle$$

- Oscillations \rightarrow q and x need to be small for $C \neq 1$
- Radial flow
 - Close in momentum \rightarrow close in space
 - Big pair momentum \rightarrow small emission region



Hadron formation time

String fragmentation



Formation time

[C.-Y. Wong, Introduction to High-Energy HICs]

Assuming constant τ_f and the formation of two strings

$$\sqrt{s_{pp}} = 62.3 \text{ GeV}$$

$$\tau_f \approx 0.6 \text{ fm}/c$$

τ_f dependence of the longitudinal source size



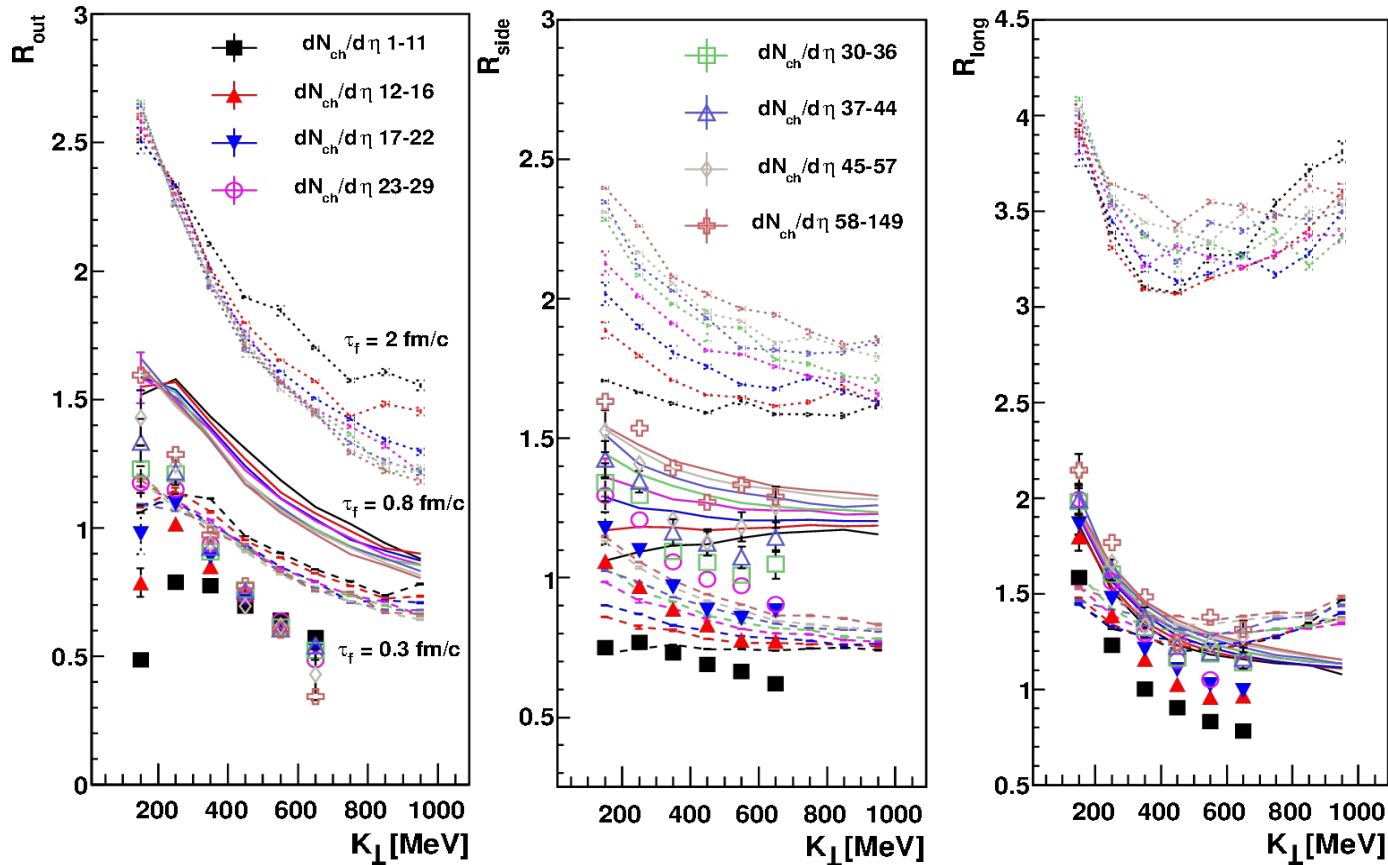
Small source

Big source

τ_f from p+p at LHC

[ALICE, PRD84 (2011) 112004]

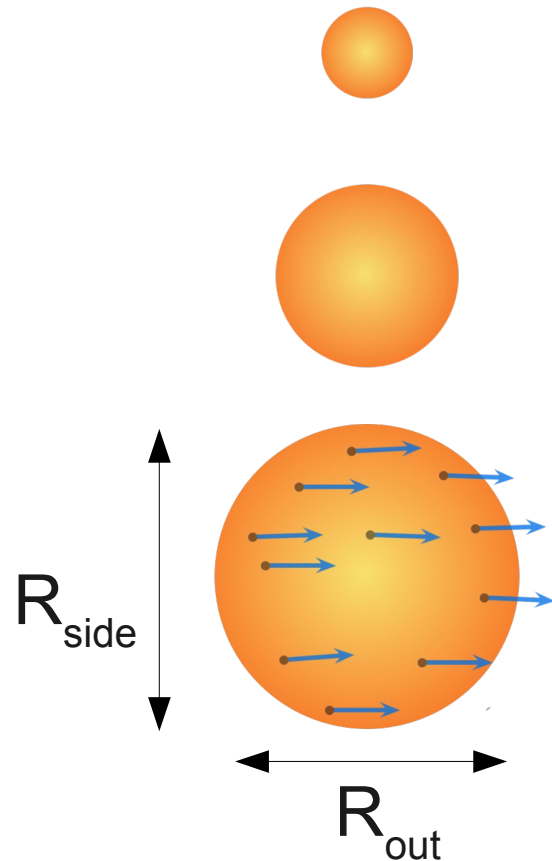
[G. G. et al., J.Phys. G39 (2012) 065101]



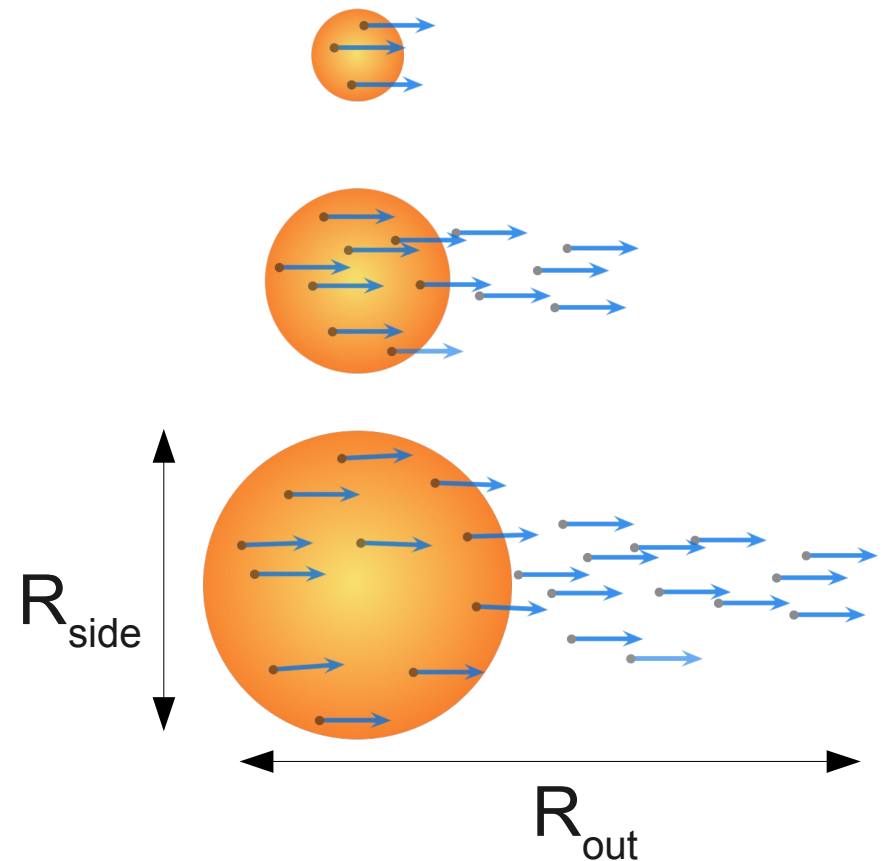
- Size of the radii scales with τ_f
- Comparison with data yields $\tau_f < 0.8$ fm/c

Source lifetime \neq Collision duration

Zero lifetime



Finite lifetime



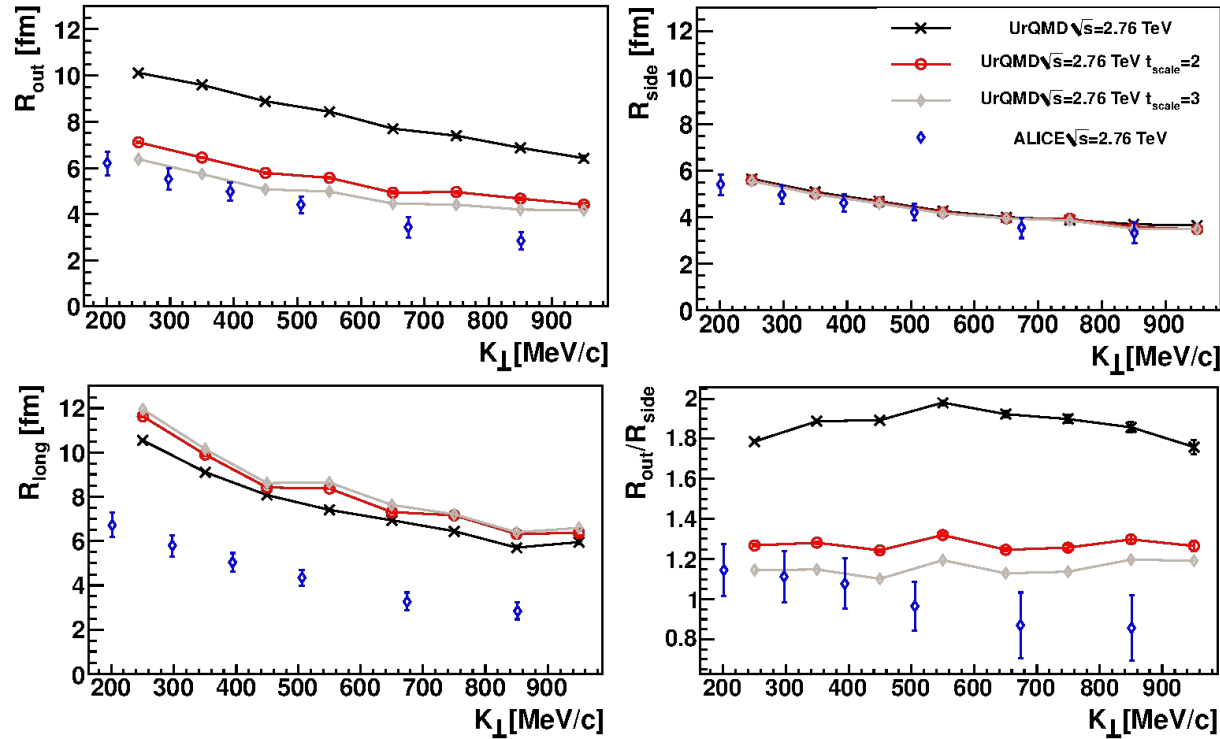
Collision duration

$$R_o^2 = \langle (x_o - \beta_o t)^2 \rangle = \langle x_o^2 \rangle - 2 \langle \beta_T t x_o \rangle + \langle \beta_T^2 t^2 \rangle \quad R_s^2 = \langle x_s^2 \rangle \quad R_l^2 = \langle x_l^2 \rangle$$

t from Pb + Pb at LHC

[ALICE, PLB696 (2011) 328]

[Q. Li, G. G., M. Bleicher, PRC85 (2012) 034908]



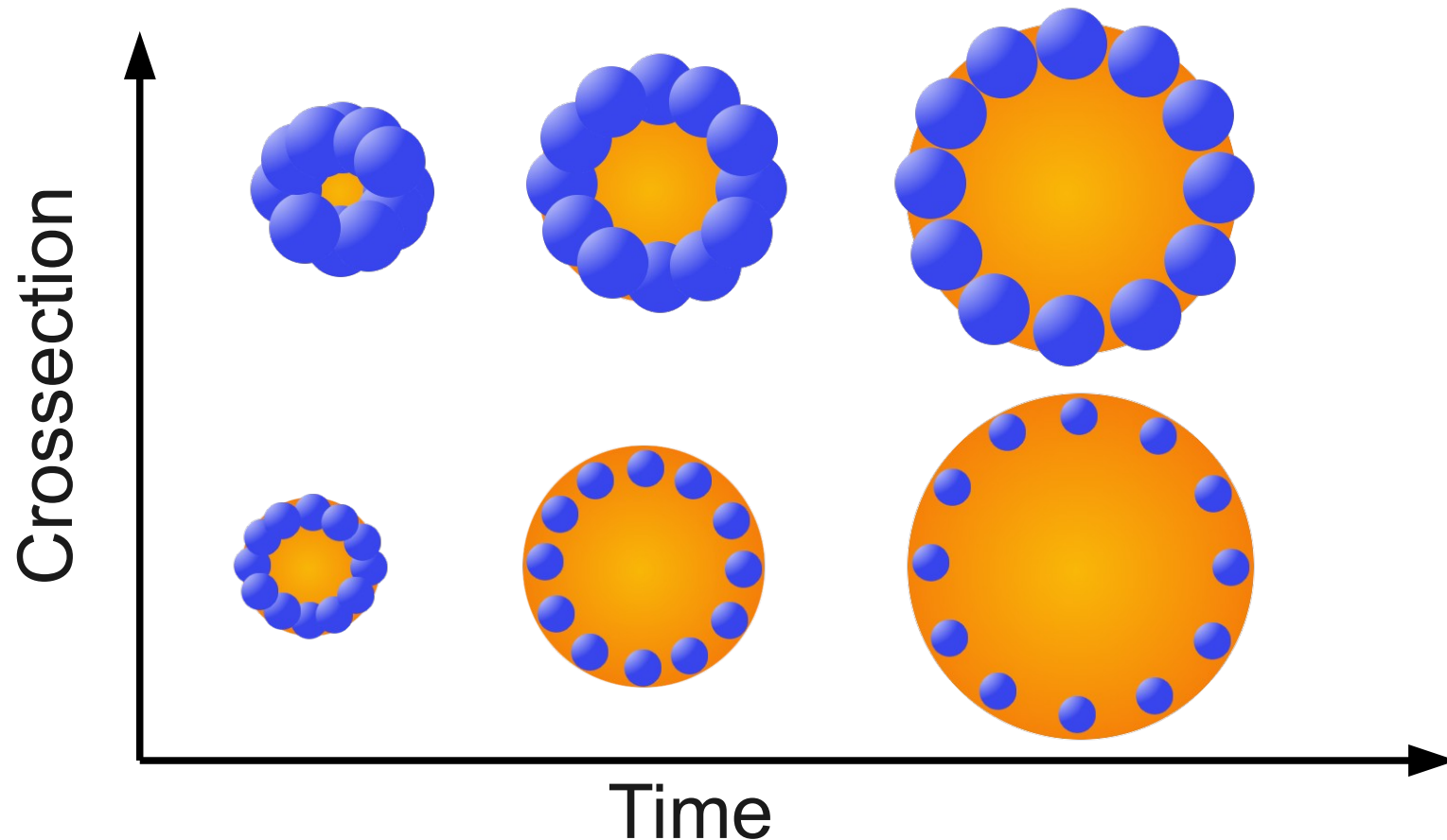
- R_{out} and R_{long} are overestimated by the calculations
- The lifetime is too long by a factor of ≈ 3
- We attribute this to the missing partonic interactions

$$t = t_i - \bar{t} \rightarrow t' = (t_i - \bar{t})/t_{scale} \quad R_O'^2 = \langle (x - \beta_T t')^2 \rangle = \langle x^2 \rangle - 2 \frac{\langle \beta_T t x \rangle}{t_{scale}} + \frac{\langle \beta_T^2 t^2 \rangle}{t_{scale}^2}$$

Decoupling

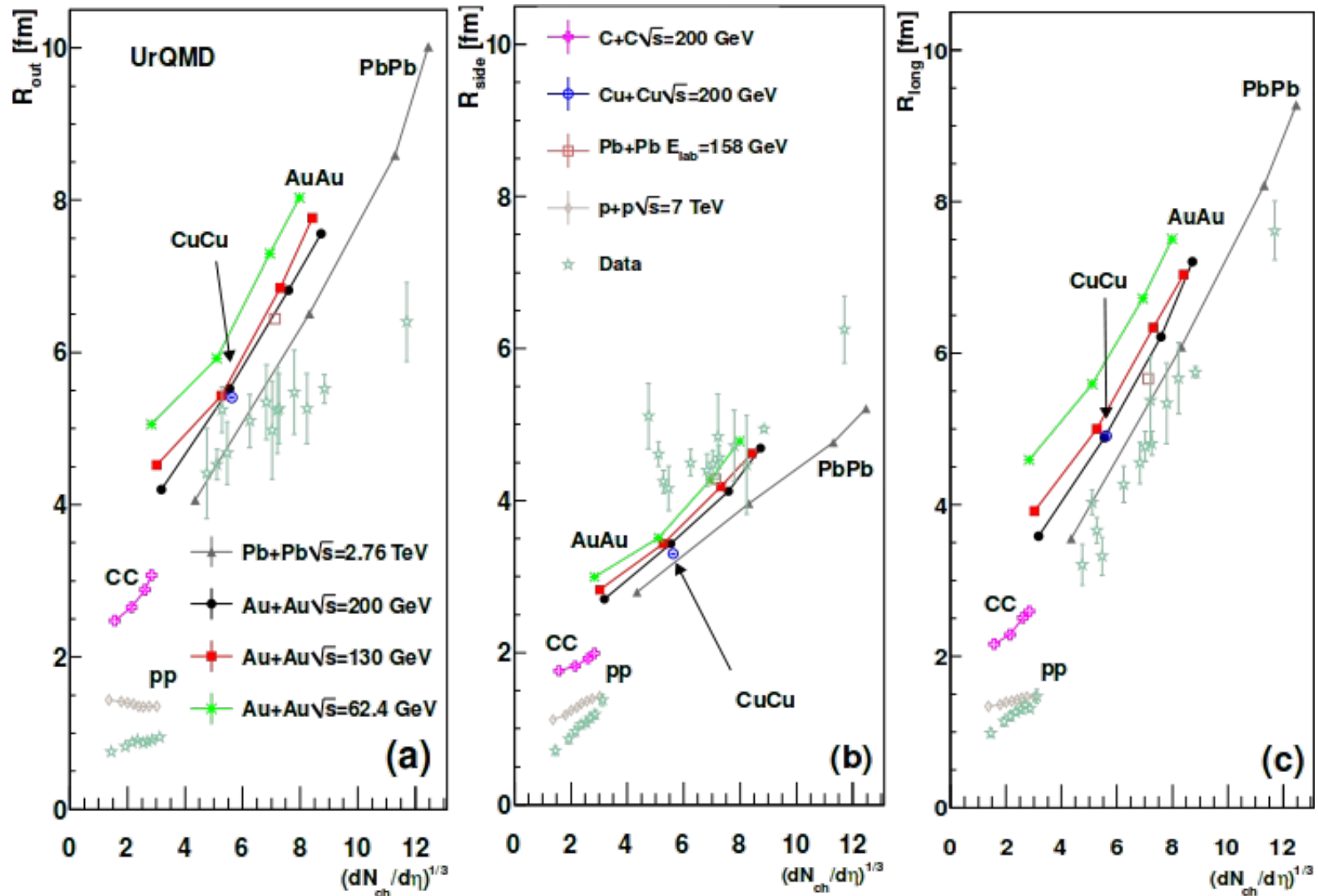
Same decoupling density \rightarrow HBT radii scale with $\left(\frac{dN_{ch}}{d\eta}\right)^{\frac{1}{3}}$

Different crosssection \rightarrow Different decoupling density



Scaling of the HBT radii

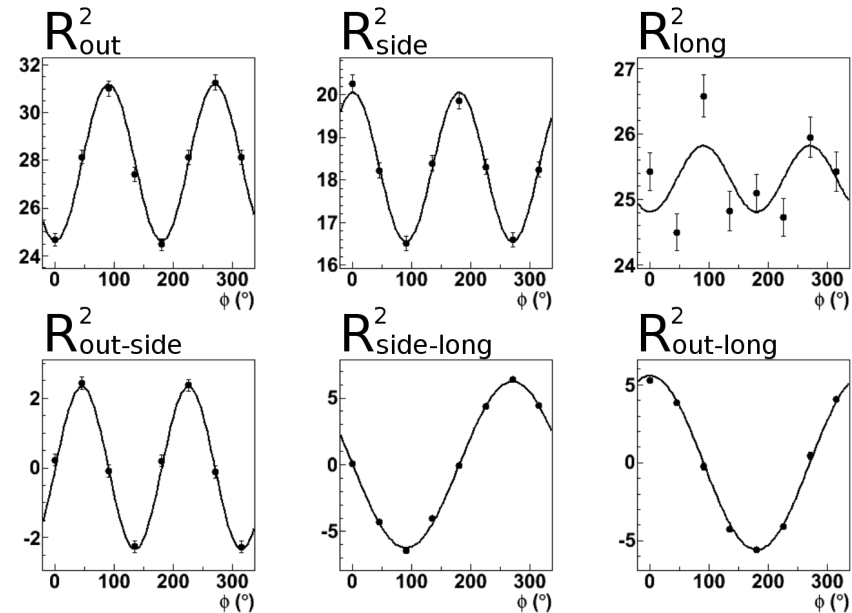
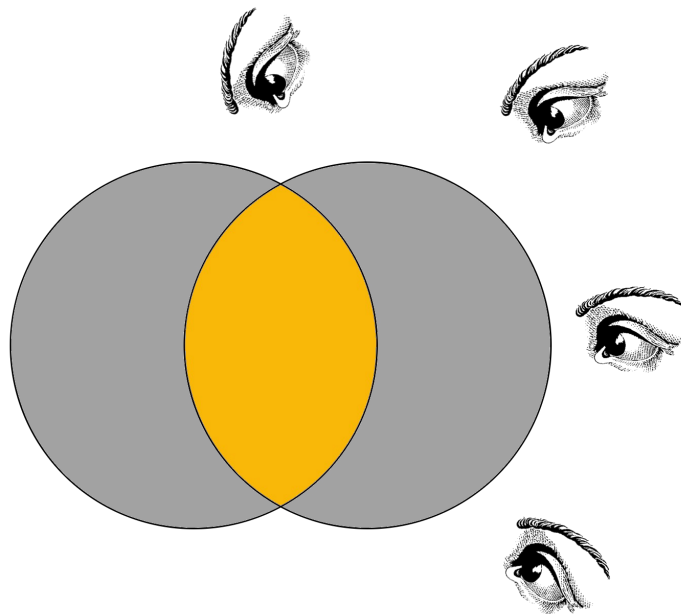
[G. G., M. Bleicher, Q. Li, PRC85 (2012) 044901]



Radii dependent on: Chemical composition and density

Azimuthally sensitive HBT

Source looks different from different directions

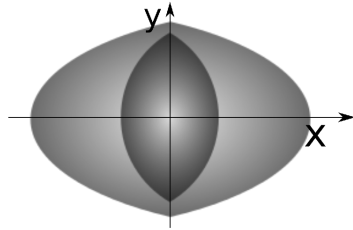
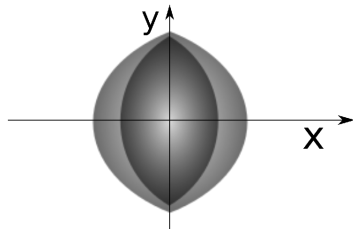
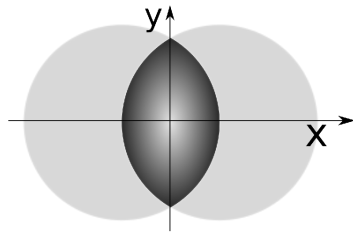


Fourier coefficients of the radii yield information about the source



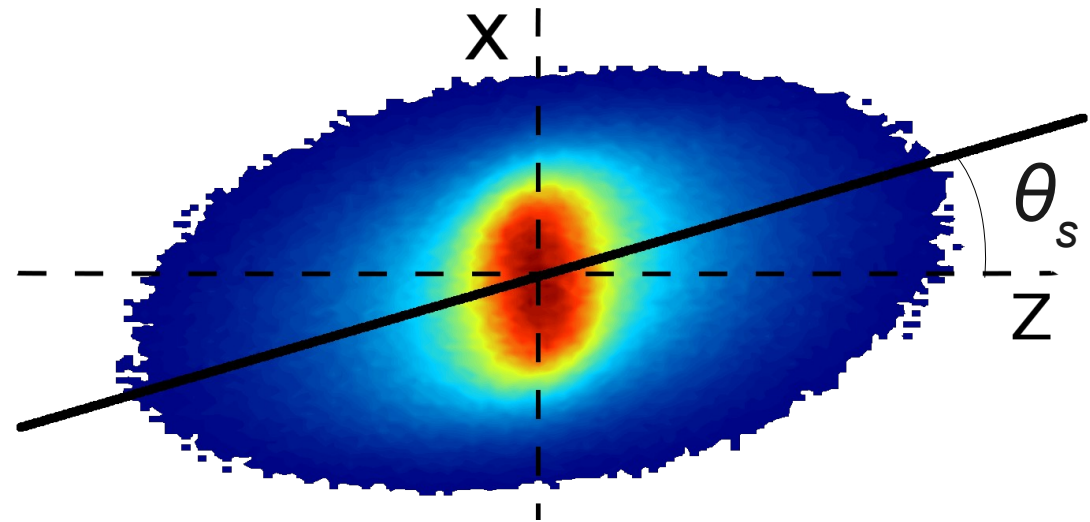
Non-central collisions

Eccentricity



$$\epsilon = 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

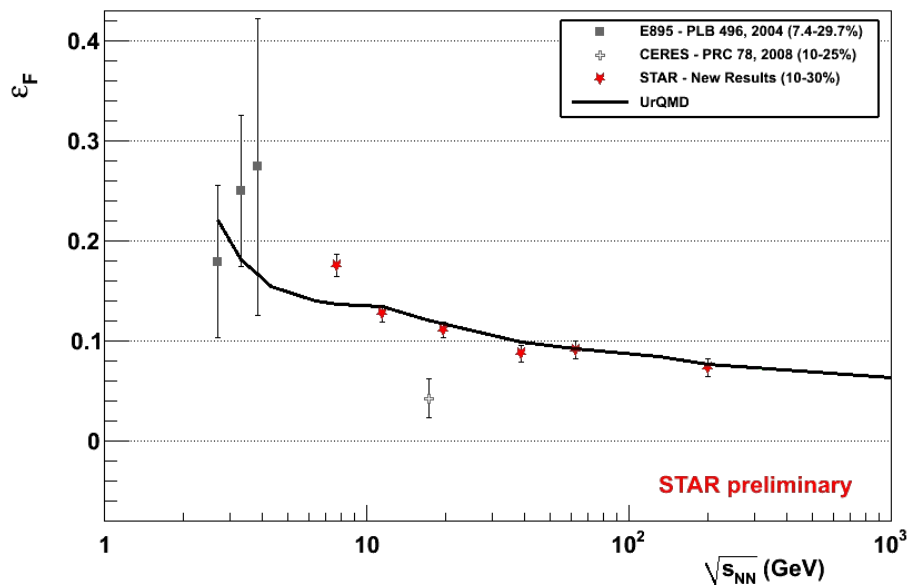
Tilt



$$\theta_s = \frac{1}{2} \tan^{-1} \left(\frac{-4R_{sl,1}^2}{R_{l,0}^2 - R_{s,0}^2 + 2R_{s,2}^2} \right)$$

Energy dependence

Eccentricity

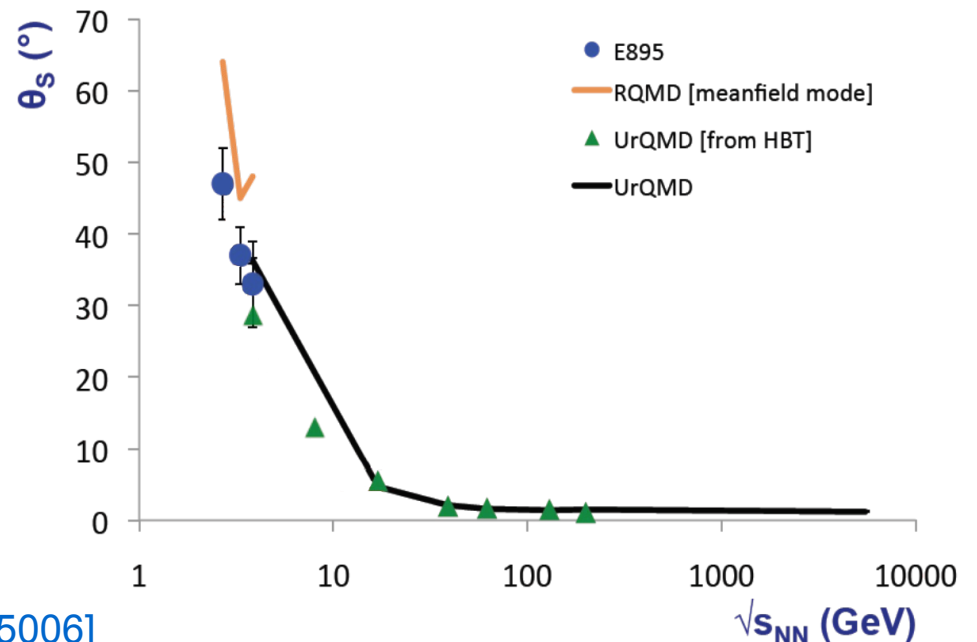


[M. Lisa, G.G., et al., New J.Phys. 13 (2011) 065006]

[A. Schmah for STAR, Central Eur.J.Phys. 10 (2012) 1238]

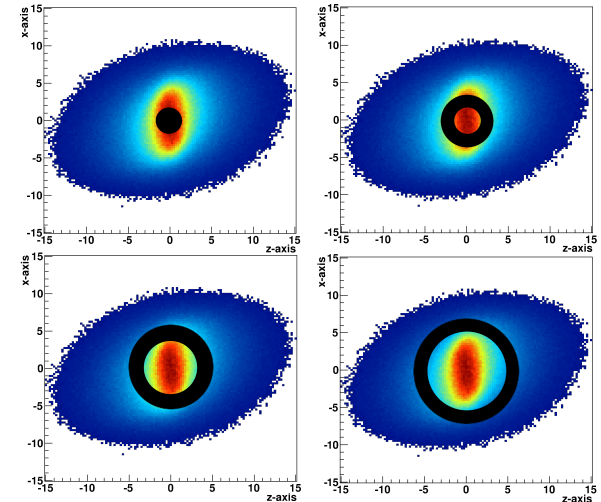
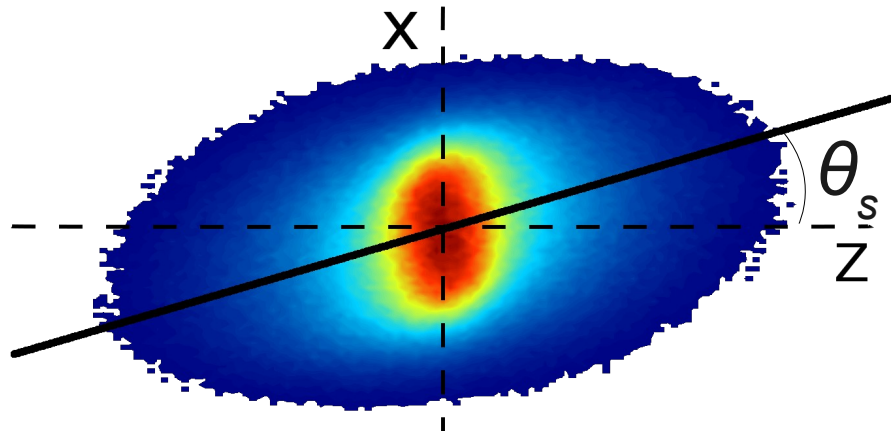
- ε_F and θ_s decrease with increasing energy
- Longer collision duration \rightarrow rounder source \rightarrow smaller ε_F
- Higher energy \rightarrow elongation in beam direction \rightarrow smaller θ_s

Tilt

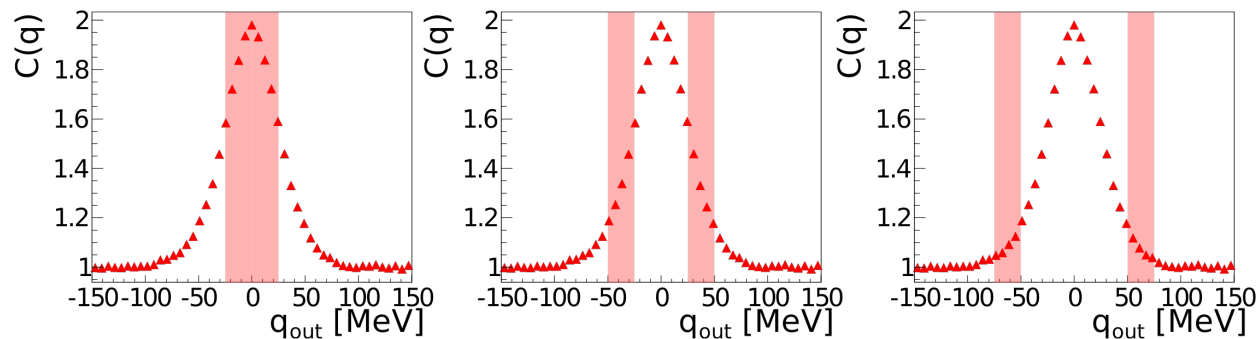


Tilt substructure – Twist

$E_{\text{lab}} = 8 \text{ AGeV}$, $b = 3.4 - 6.8 \text{ fm}$, $p_T < 0.4 \text{ GeV}$



$$f(x, y, z) \propto \exp \left(-\frac{(x \cos \theta_s - z \sin \theta_s)^2}{2\sigma_{x'}^2} - \frac{y^2}{2\sigma_y^2} - \frac{(x \sin \theta_s + z \cos \theta_s)^2}{2\sigma_{z'}^2} \right)$$



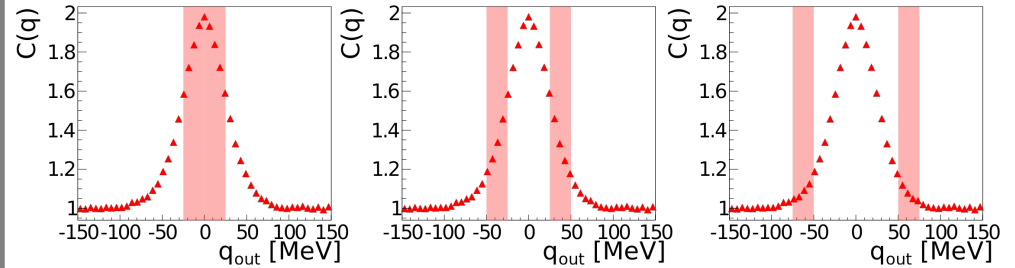
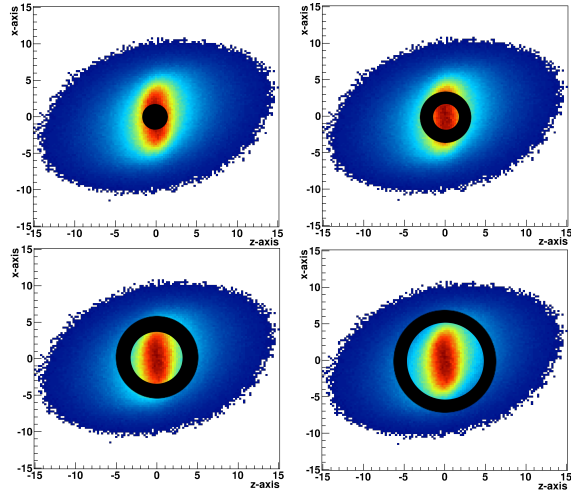


Twist – Two techniques

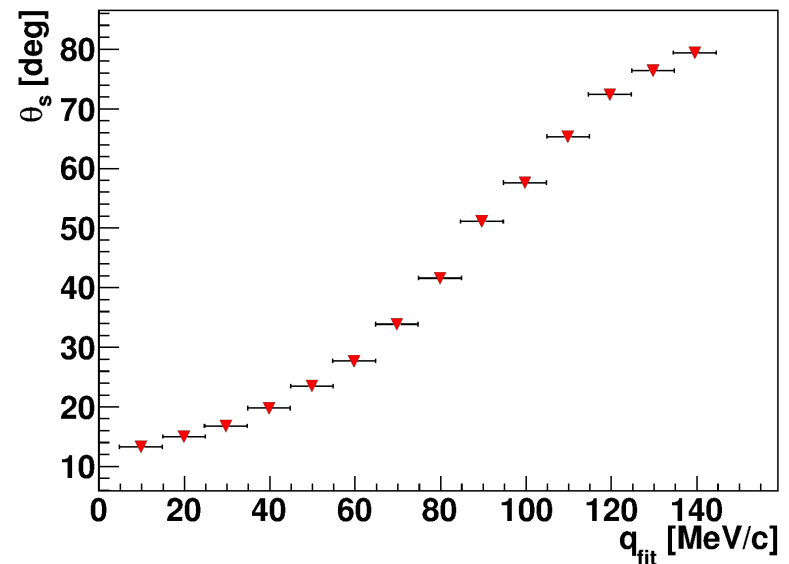
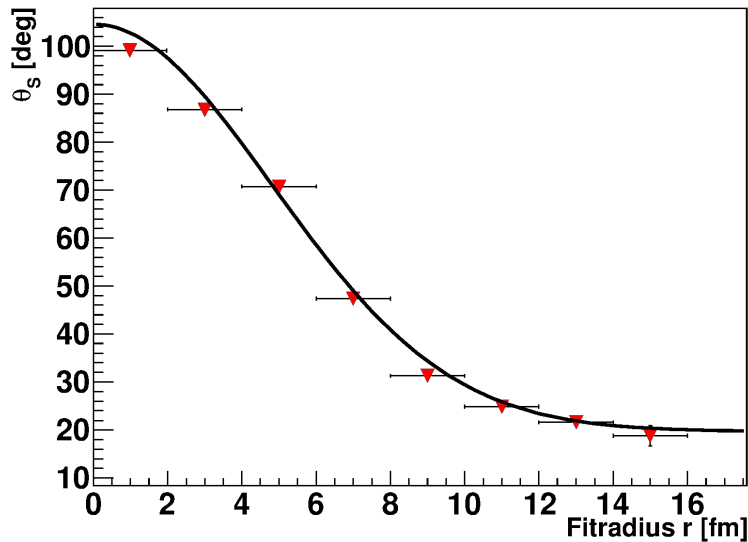
Freeze-out fit

HBT fit

Method



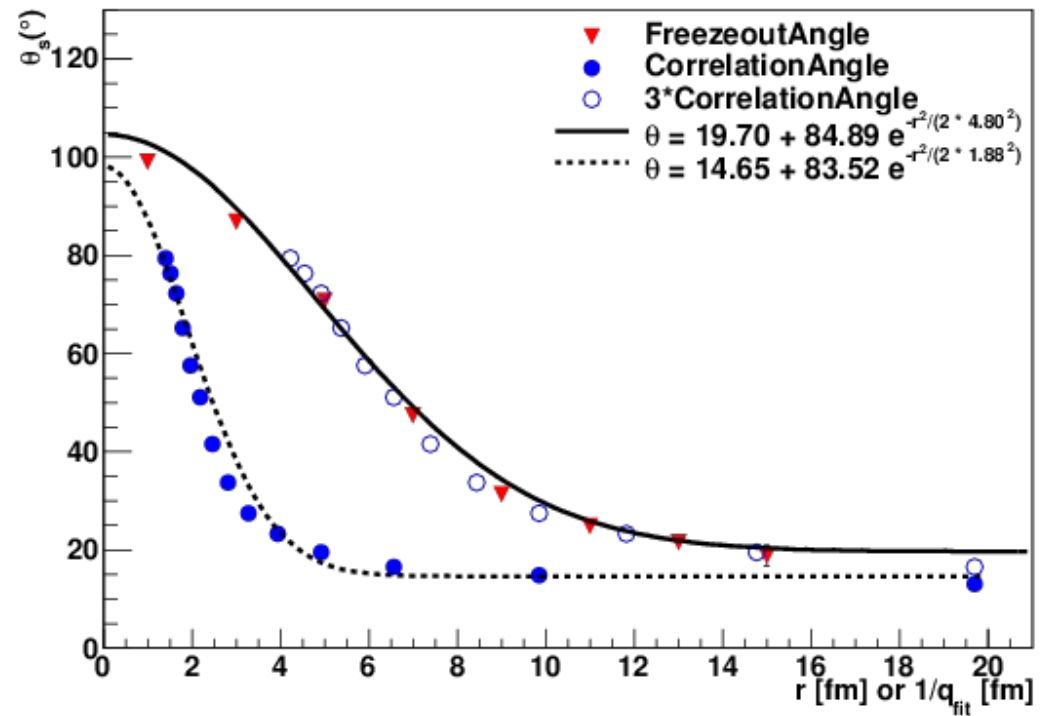
Result



Twist – The results

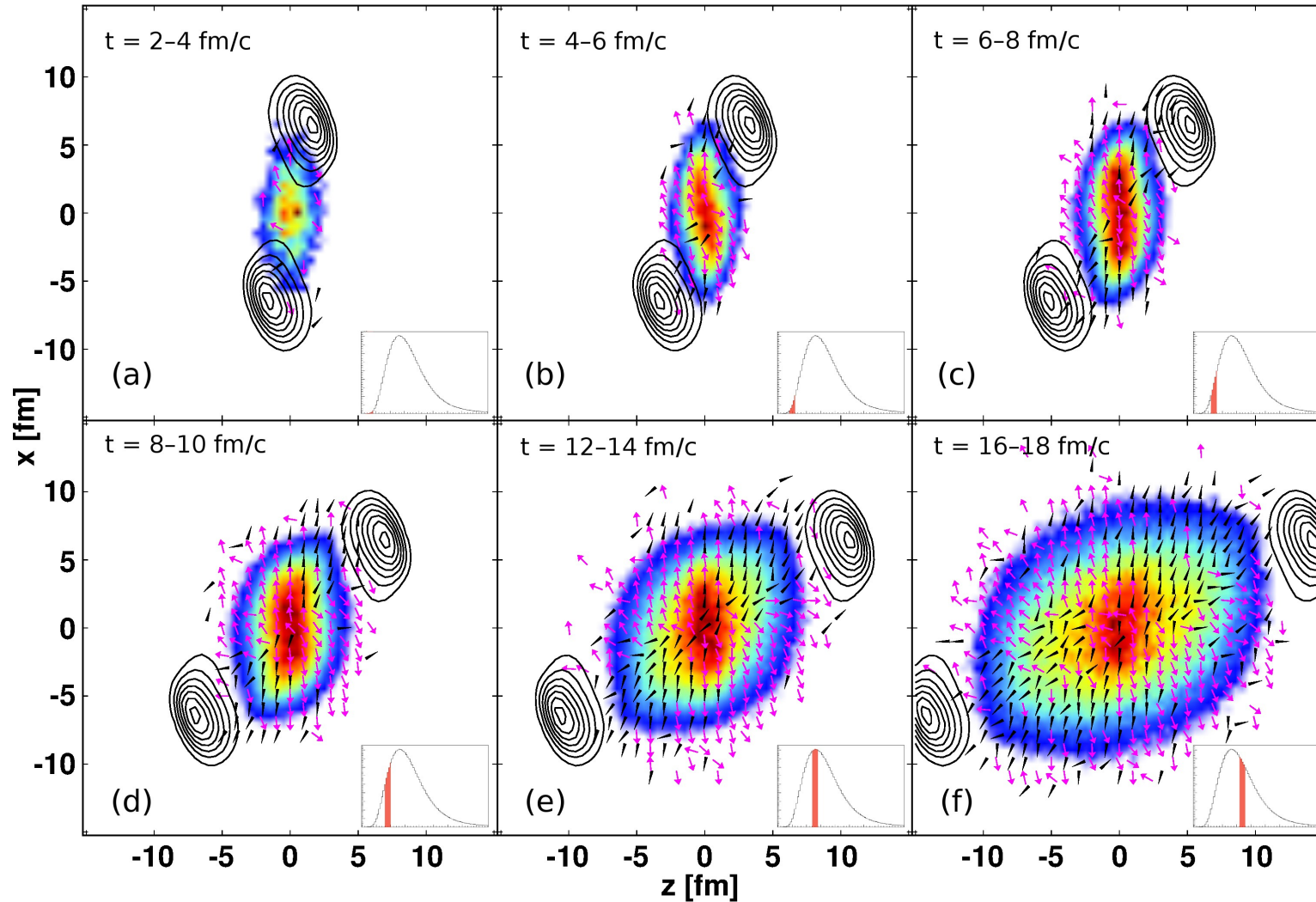
Transformation $r = \frac{1}{q_{fit}}$

- Measurable via asHBT
- Twist caused by Shadowing and Squeeze-out
- Most prominent at FAIR energies



[G. G., M. Lisa, M. Bleicher, arXiv:1302.3408, submitted to PRC]

Shadowing, Flow, Squeeze-out



[G. G., M. Lisa, M. Bleicher, arXiv:1302.3408, submitted to PRC]

Summary

- p+p at LHC suggests $\tau_f < 0.8$ fm/c
 - Scaling depends on energy as well
 - Eccentricity well described, decreases with energy
 - Tilt is biggest at FAIR energies
 - New observable: Twist
-
- Measure the Twist in experiment at FAIR
 - Analyse LHC results with partonic phase