

# Beam energy scan in a UrQMD+hydro hybrid model

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FIAS Frankfurt Institute  
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# Outline

Introduction

Hybrid model

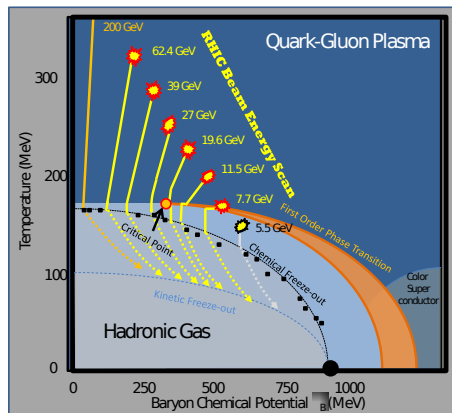
Results

Summary

## Beam energy scan

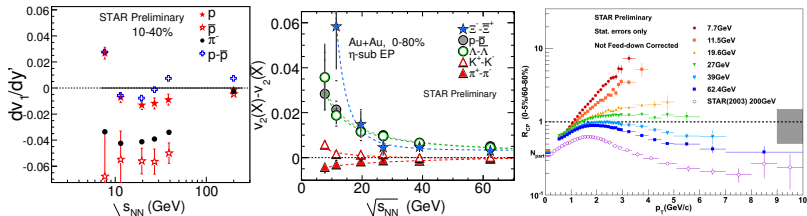
First order phase transition  
with critical point?

QGP volume and lifetime  
decreases with decreasing  
 $\sqrt{s_{NN}} \Rightarrow$  completely vanishes  
at some point?



Picture taken from G. Odyniec, Acta Phys. Polon. B 43, 627 (2012).

# Beam energy scan



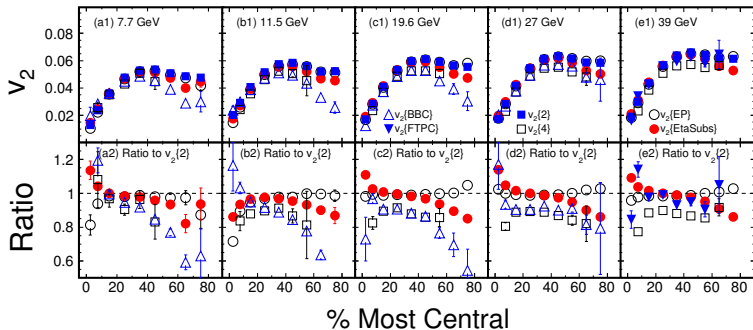
Some interesting findings:

- Non-monotonic  $\sqrt{s_{NN}}$  dependence of net-proton  $v_1$
- Difference in particle and antiparticle  $v_2$  at lower energies
- $R_{CP}$  suppression turns to enhancement between  $\sqrt{s_{NN}} = 39$  and 27 GeV

$v_1$  and  $v_2$  figures from L. Kumar [STAR Collaboration], arXiv:1211.1350 [nucl-ex],

$R_{CP}$  from Hot Quarks 2012 talk by S. Horvat.

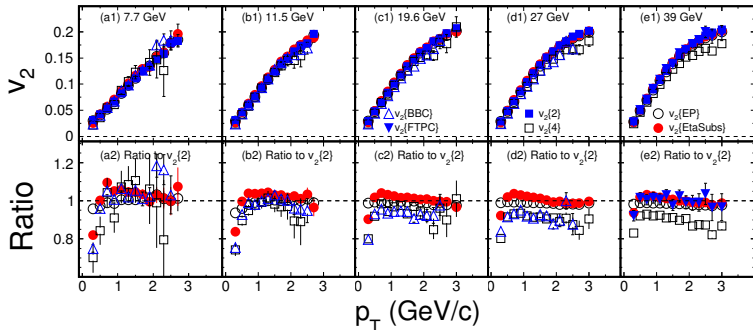
# Beam energy scan



Charged hadron  $v_2$  shows weak collision energy dependence.

L. Adamczyk et al. [STAR Collaboration], Phys. Rev. C 86, 054908 (2012).

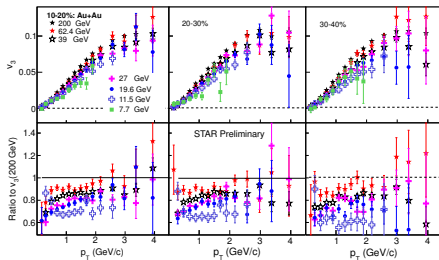
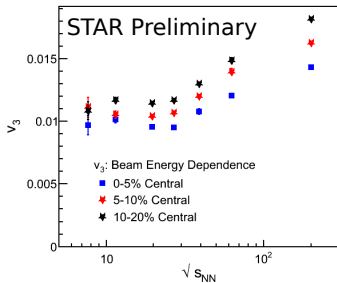
# Beam energy scan



Differential  $v_2$  almost identical for all  $\sqrt{s_{NN}}$ .

L. Adamczyk et al. [STAR Collaboration], Phys. Rev. C 86, 054908 (2012).

# Beam energy scan



$v_3$  more sensitive to beam energy?

Y. Pandit [STAR Collaboration], QM2012 talk; arXiv:1210.5315.

# Hybrid model



# Transport + hydrodynamics hybrid model

H. Petersen, J. Steinheimer, G. Burau, M. Bleicher and H. Stoecker, Phys. Rev. C **78**, 044901 (2008).

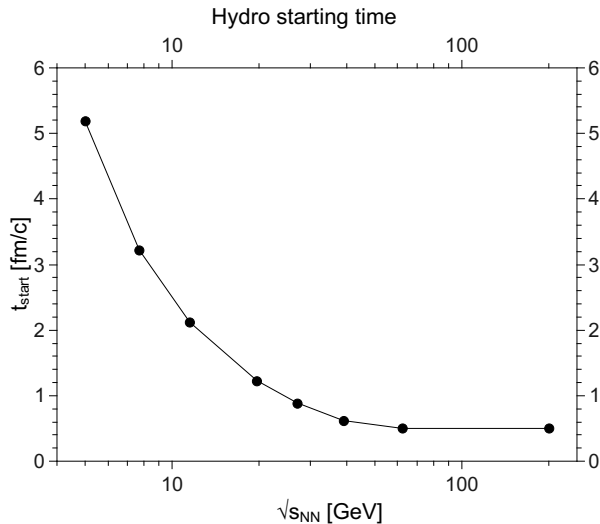
Initial State from UrQMD<sup>1</sup> string/hadronic cascade

- Start the hydrodynamical evolution when nuclei have passed through each other:  $t_{\text{start}} = \max\left\{\frac{2R_{\text{nuclei}}}{\sqrt{\gamma_{CM}^2 - 1}}, 0.5 \text{ fm}\right\}$ .
- Energy-, momentum- and baryon number densities (3D Gaussians) are mapped onto the **hydro grid**
- **Event-by-event fluctuations** are taken into account (width of Gaussians  $\sigma = 1.0 \text{ fm}$ .)
- Spectators are propagated separately in the cascade

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<sup>1</sup>S. A. Bass *et al.*, Prog. Part. Nucl. Phys. **41**, 255 (1998), M. Bleicher *et al.*, J. Phys. G **25**, 1859 (1999).

# Hydro starting times



# Transport + hydrodynamics hybrid model

H. Petersen, J. Steinheimer, G. Burau, M. Bleicher and H. Stoecker, Phys. Rev. C 78, 044901 (2008).

## Hydrodynamical evolution

- (3+1)D ideal hydrodynamics using SHASTA<sup>2</sup>
- Equation of state<sup>3</sup>:
  - Chiral model coupled to Polyakov loop to include the deconfinement phase transition
  - Qualitative agreement with lattice QCD data at  $\mu_B = 0$
  - Applicable also at finite baryon densities
  - Has the same degrees of freedom as UrQMD in hadronic phase

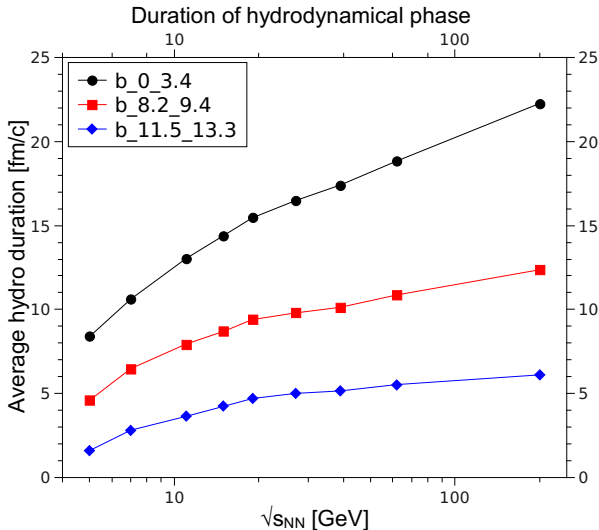
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<sup>2</sup>D. H. Rischke, S. Bernard and J. A. Maruhn, Nucl. Phys. A 595, 346 (1995),

D. H. Rischke, Y. Pursun and J. A. Maruhn, Nucl. Phys. A 595, 383 (1995).

<sup>3</sup>J. Steinheimer, S. Schramm and H. Stoecker, J. Phys. G 38, 035001 (2011).

# Hydro duration in computational frame



# Transport + hydrodynamics hybrid model

H. Petersen, J. Steinheimer, G. Burau, M. Bleicher and H. Stoecker, Phys. Rev. C 78, 044901 (2008).

## Freeze-out Procedure

- Transition from hydro to transport (“particlization”) when energy density  $\epsilon$  is smaller than critical value  $x\epsilon_0$ , where  $\epsilon_0 = 146 \text{ MeV}/\text{fm}^3$  represents the nuclear ground state and  $x \geq 1$ .<sup>4</sup>
- Particle distributions are generated according to the Cooper-Frye formula
- Rescatterings and final decays calculated via hadronic cascade (UrQMD)

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<sup>4</sup>In this study  $x = 2$ , corresponding to temperature  $T \approx 154 \text{ MeV}$ .

# Transport + hydrodynamics hybrid model

## Cornelius hypersurface finding algorithm

P. Huovinen and H. Petersen, arXiv:1206.3371.

A method for finding the elements of 3D particlization hypersurface in 4D space for the Cooper-Frye procedure, without holes or double counting

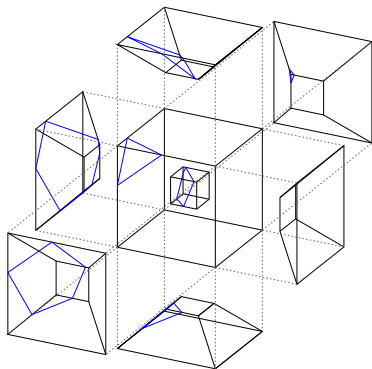
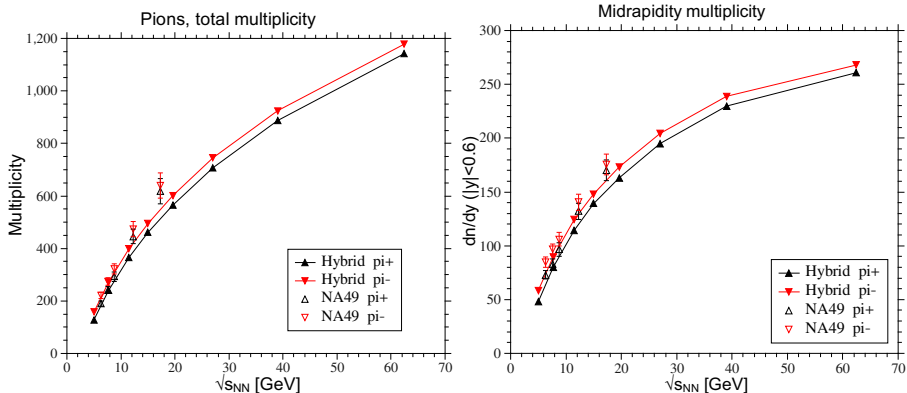


Fig. 9. Reduction of a four dimensional problem into a series of three dimensional problems.

# Results

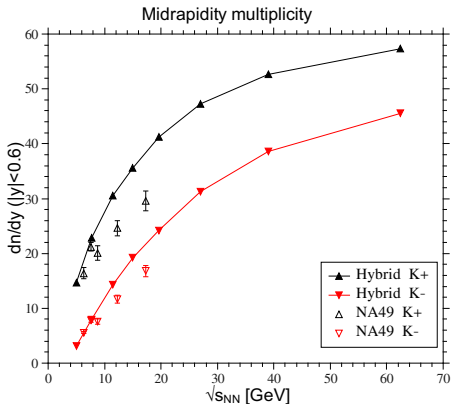
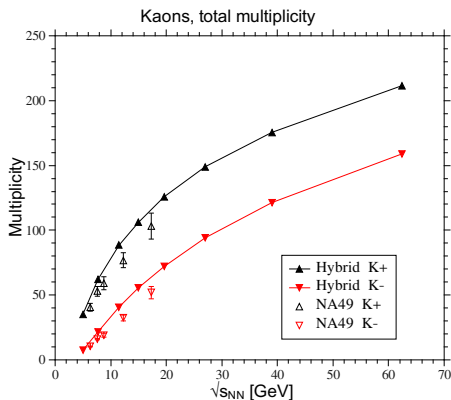
# Particle multiplicity



Charged pion multiplicity as a function of  $\sqrt{s_{NN}}$ .



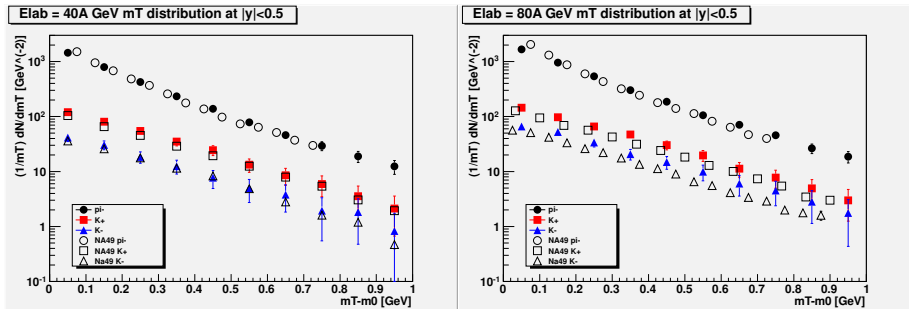
# Particle multiplicity



Charged kaon multiplicity as a function of  $\sqrt{s_{NN}}$ .

Particle  $m_T$  spectra

(0-7)% centrality.



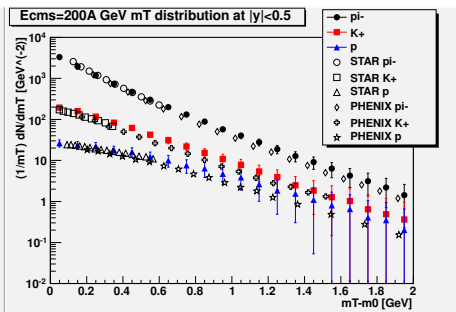
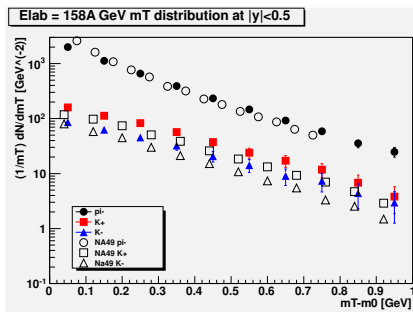
Left:  $\pi^-$ ,  $K^+$ ,  $K^-$  at  $\sqrt{s_{NN}} \approx 9$  GeV.  
Right:  $\pi^-$ ,  $K^+$ ,  $K^-$  at  $\sqrt{s_{NN}} \approx 12$  GeV.

S. V. Afanasiev *et al.* [NA49 Collaboration], Phys. Rev. C 66, 054902 (2002).

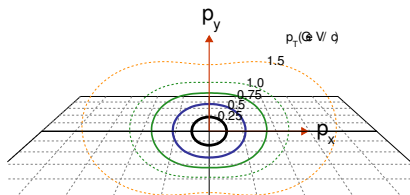
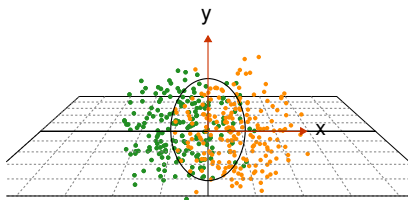
Particle  $m_T$  spectra

(0-7)% centrality.

(0-5)% centrality.

Left:  $\pi^-$ ,  $K^+$ ,  $K^-$  at  $\sqrt{s_{NN}} \approx 17$  GeV.Right:  $\pi^-$ ,  $K^+$ ,  $p$  at  $\sqrt{s_{NN}} = 200$  GeV.S. V. Afanasiev *et al.* [NA49 Collaboration], Phys. Rev. C 66, 054902 (2002).J. Adams *et al.* [STAR Collaboration], Phys. Rev. Lett. 92, 112301 (2004),S. S. Adler *et al.* [PHENIX Collaboration], Phys. Rev. C 69, 034909 (2004).

# Elliptic flow

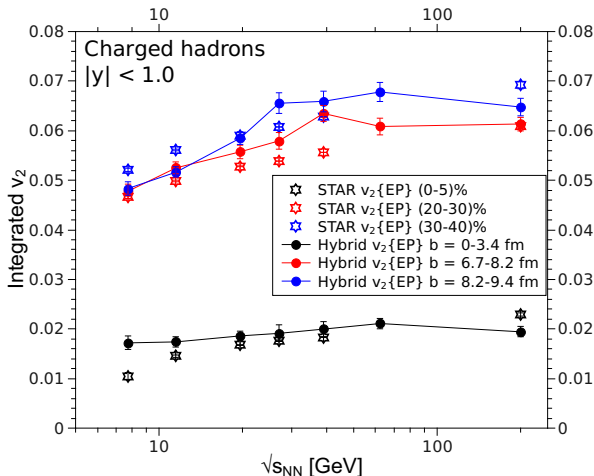


P. Sorensen, arXiv:0905.0174 [nucl-ex].

Initial spatial asymmetry: eccentricity  $\epsilon_2 = \frac{\sqrt{\langle r^2 \cos(2\phi) \rangle^2 + \langle r^2 \sin(2\phi) \rangle^2}}{\langle r^2 \rangle}$ .

Final momentum anisotropy:  $v_2\{\text{EP}\} = \frac{v_2\{\text{observed}\}}{R_2} = \frac{\langle \cos[2(\phi_i - \psi_2)] \rangle}{\langle \cos[2(\psi_2 - \psi_2^{\text{true}})] \rangle}$

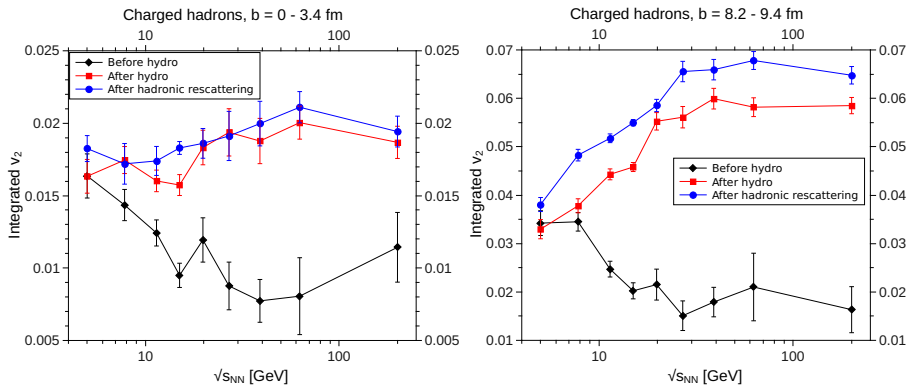
# Elliptic flow



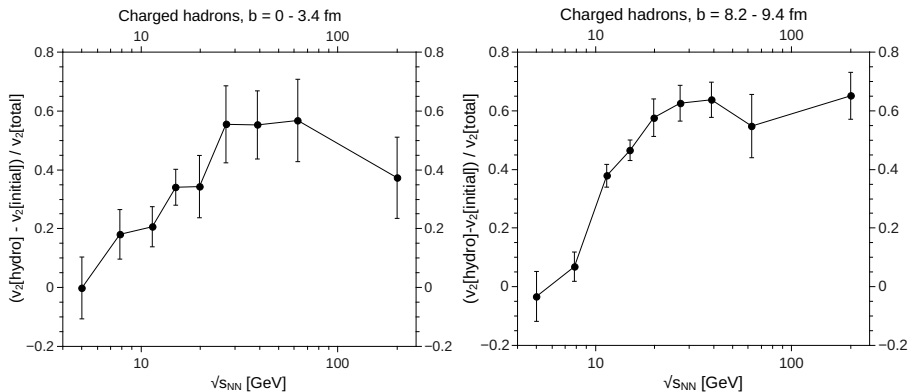
Rising slope in 0-5% centrality not reproduced; rough agreement at midcentrality.

L. Adamczyk *et al.* [STAR Collaboration], Phys. Rev. C 86, 054908 (2012).

## Elliptic flow

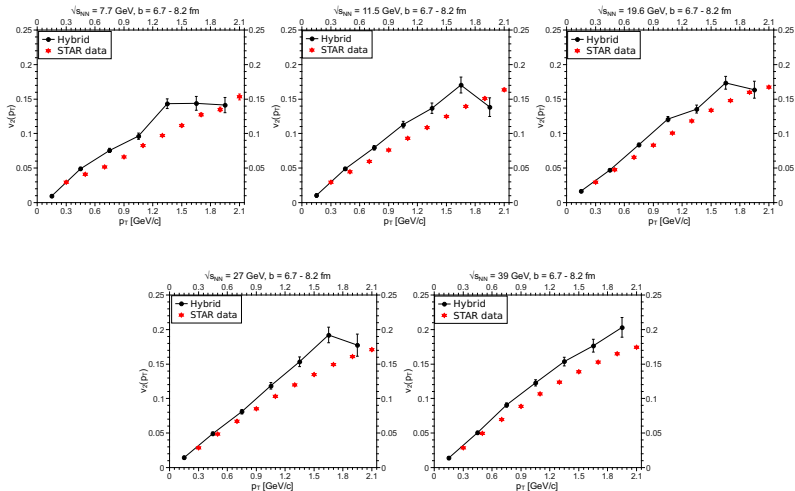


No contribution from hadronic rescattering in most central collisions.  
Pre-equilibrium dynamics become more important at lower energies.

Hydro contribution on  $v_2$ 

Hydro contribution to  $v_2$  negligible at  $\sqrt{s_{NN}} = 5$  GeV; roughly 60% at highest energies.

## Elliptic flow

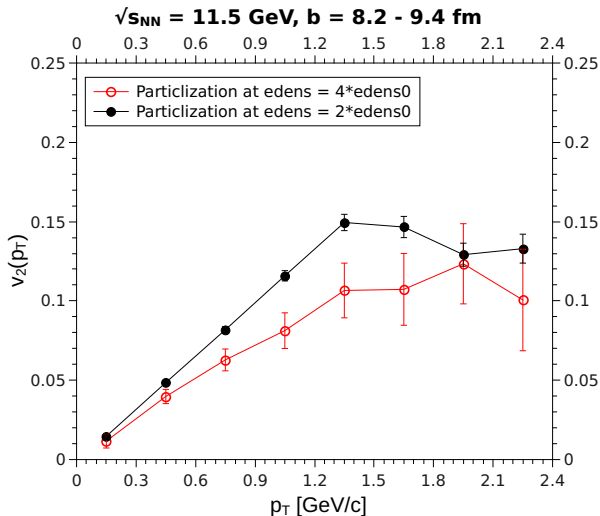


$v_2(p_T)$  overestimated at higher  $p_T$ .

L. Adamczyk et al. [STAR Collaboration], Phys. Rev. C 86, 054908 (2012).

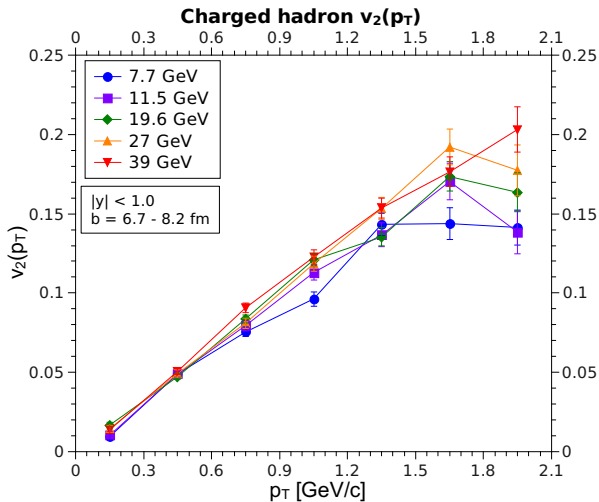


# Effect of hydro ending condition on elliptic flow



Revision of hydro-to-cascade transition condition could fix  $v_2(p_T)$ .

# Elliptic flow



No clear energy dependence on differential flow.

# Triangular flow

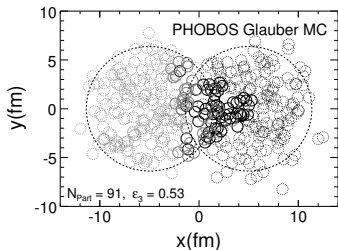


FIG. 3: Distribution of nucleons on the transverse plane for a  $\sqrt{s_{NN}} = 200$  GeV Au+Au collision event with  $\epsilon_3=0.53$  from Glauber Monte Carlo. The nucleons in the two nuclei are shown in gray and black. Wounded nucleons (participants) are indicated as solid circles, while spectators are dotted circles.

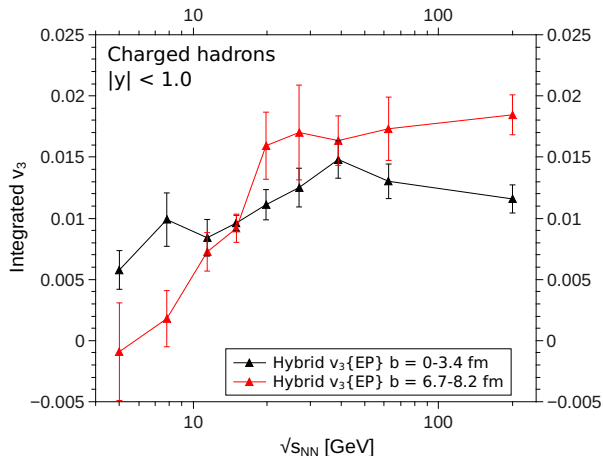
B. Alver and G. Roland, Phys. Rev. C 81, 054905 (2010), [arXiv:1003.0194].

Triangularity:

$$\epsilon_3 = \frac{\sqrt{\langle r^3 \cos(3\phi) \rangle^2 + \langle r^3 \sin(3\phi) \rangle^2}}{\langle r^3 \rangle}$$

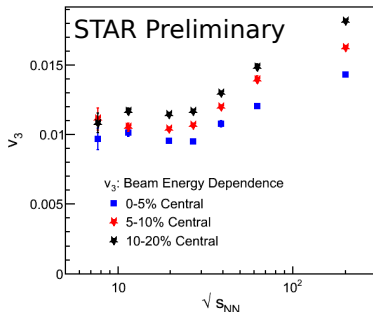
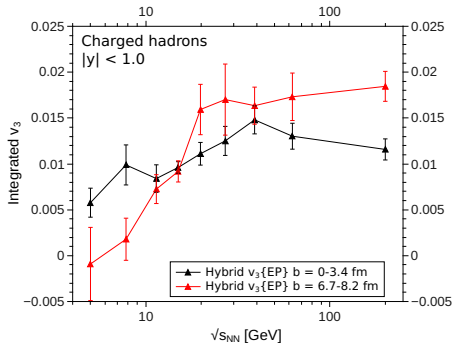
$$v_3\{\text{EP}\} = \frac{\langle \langle \cos[3(\phi_i - \psi_3)] \rangle \rangle}{\langle \cos[3(\psi_3 - \psi_3^{\text{true}})] \rangle}$$

# Triangular flow



Midcentral  $v_3$  rises from  $\approx 0$  to  $\approx 0.015 - 0.02$ .

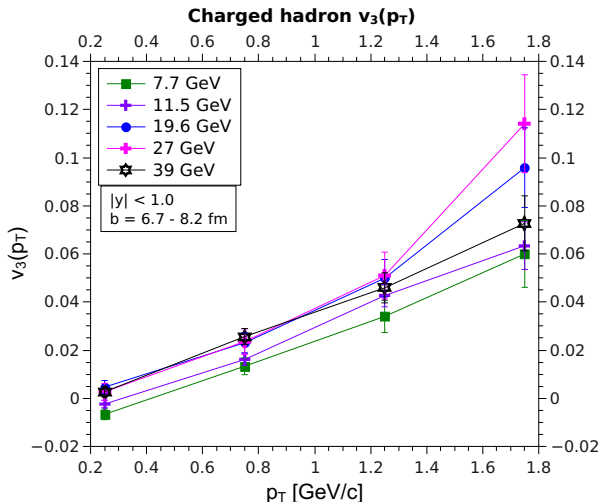
# Triangular flow



Preliminary data displays quite different behavior, however.

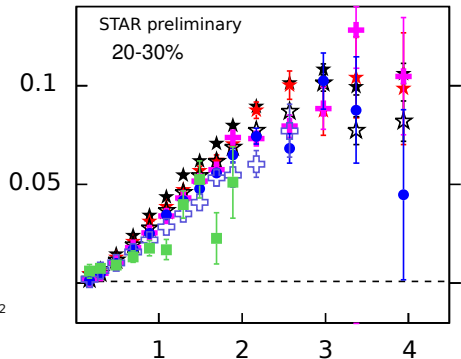
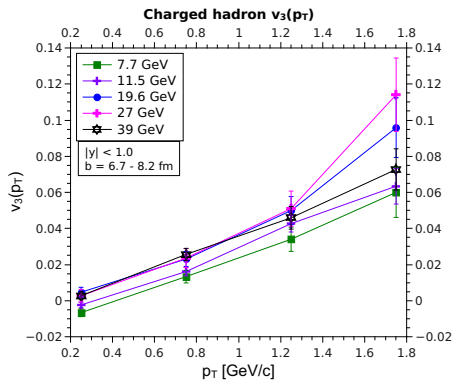
Y. Pandit [STAR Collaboration], QM2012 talk.

$$v_3(p_T)$$



Increase at lower values of  $\sqrt{s_{NN}}$ ; no change after 19.6 GeV.

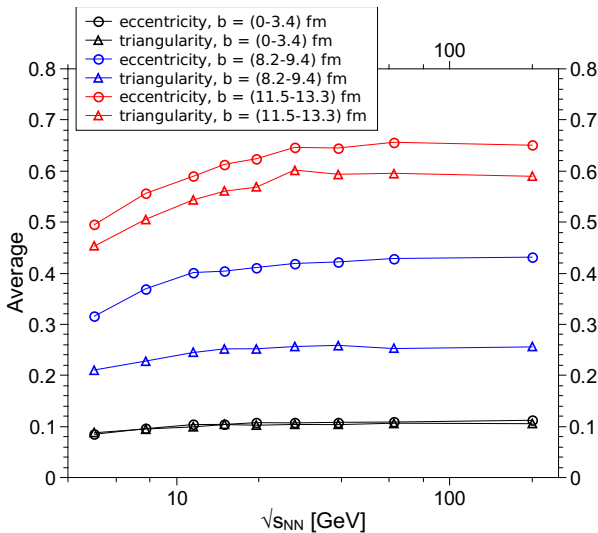
$$v_3(p_T)$$



Comparison with preliminary STAR data.

Y. Pandit [STAR Collaboration], arXiv:1210.5315.

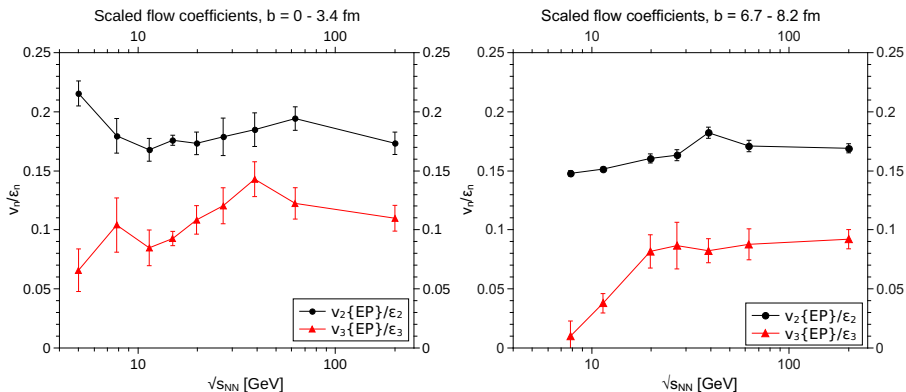
# Collision geometry



$\epsilon_2$  more sensitive than  $\epsilon_3$  to changes on  $b$  and  $\sqrt{s_{NN}}$ .



# Scaled flow coefficients



$v_2$  response to  $\epsilon_2$  remains roughly the same in both centrality classes and all energies.

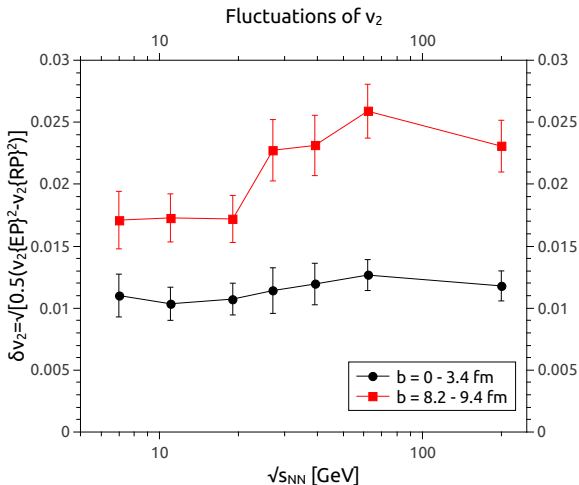
Energy dependence of  $v_3$  persists through scaling.

# Summary

- **Multiplicities:** Pion production in reasonable agreement with data, kaons overproduced.
- **Elliptic flow:** Integrated  $v_2$  similar to the STAR data,  $v_2(p_T)$  overshoots the data (particization at higher energy density?).
- **Triangular flow:**  $v_3 \approx 0$  at  $\sqrt{s_{NN}} = 5$  GeV, then rises until reaches value 0.015 - 0.02 at  $\sqrt{s_{NN}} = 19.6$  GeV.  
**Qualitative disagreement** with preliminary STAR data, which has flat  $v_3$  at low  $\sqrt{s_{NN}}$  and begins increasing at 27 GeV.

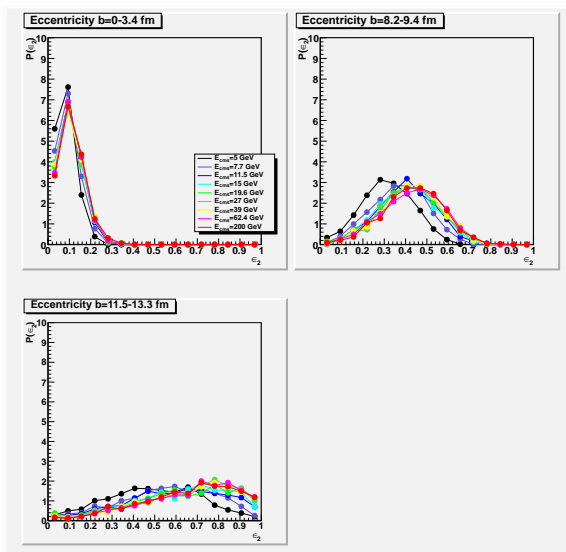
# Extra slides

# $v_2$ fluctuations

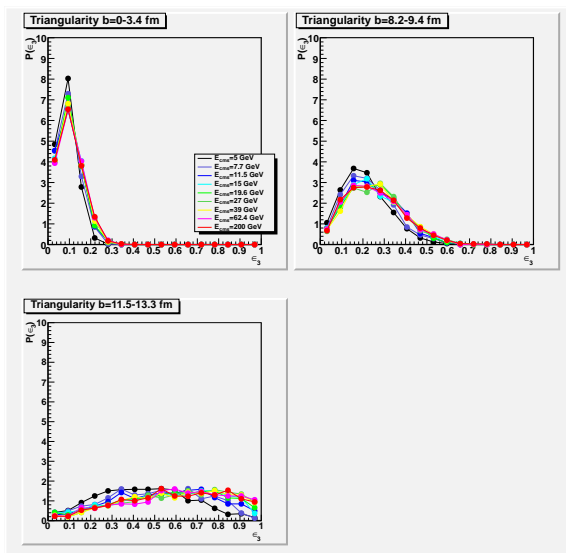


$\delta v_2$  visibly energy-dependent on midcentral collisions; equal to  $v_3$  in magnitude in central collisions.

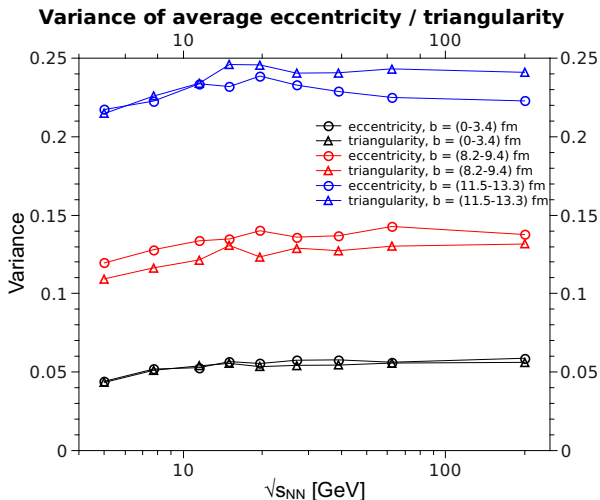
# Eccentricity probability distributions



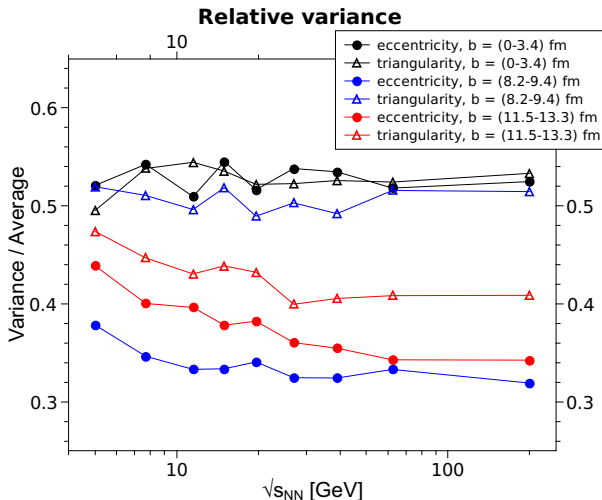
# Triangularity probability distributions



(Square root of) variances of  $\langle \epsilon_2 \rangle$  and  $\langle \epsilon_3 \rangle$



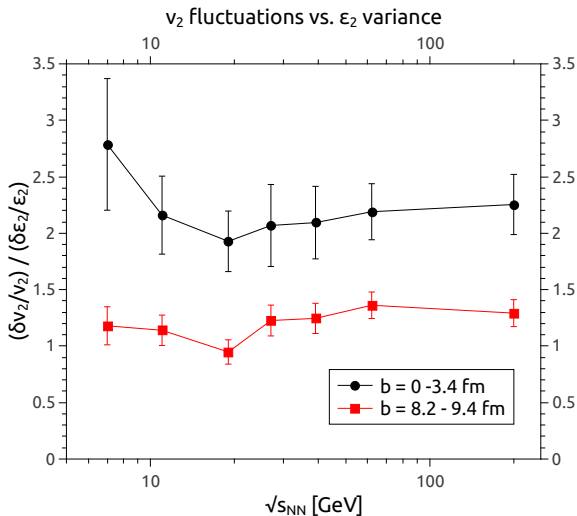
Both eccentricity and triangularity have variances of same size.

Relative variances of  $\langle \epsilon_2 \rangle$  and  $\langle \epsilon_3 \rangle$ 

Triangularity has larger relative variance than eccentricity; remains practically same from most central to midcentral collisions.



# Relative variance of $\langle \epsilon_2 \rangle$ and $v_2$ fluctuations



$$\frac{\delta v_2}{v_2} \approx \frac{\delta \epsilon_2}{\epsilon_2} \text{ in midcentrality.}$$

## Energy-momentum tensor anisotropy

$$\epsilon_p = \frac{\langle T^{xx} - T^{yy} \rangle}{\langle T^{xx} + T^{yy} \rangle}$$

