

# 22<sup>nd</sup> Winter Workshop on Nuclear Dynamics La Jolla, CA, 12-18 March, 2006 A Summary

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Stiftung / Foundation



# Outline

Bulk properties

Lattice QCD

Hadronic models

## M. Csanàd: Elliptic analytic hydro solution

$$\begin{aligned}\partial_\mu(nu^\mu) &= 0, & \partial_\mu T^{\mu\nu} &= 0 \\ T^{\mu\nu} &= (\epsilon + p)u^\mu u^\nu - pg^{\mu\nu} \\ \epsilon &= \kappa p, & p &= nT\end{aligned}$$

Class of ellipsoidal scaling solutions

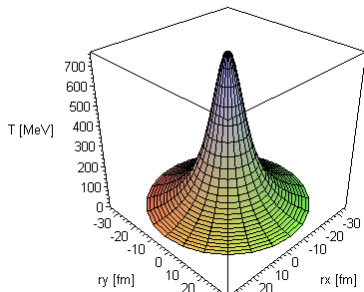
$$s = \frac{x^2}{X^2(\tau)} + \frac{y^2}{Y^2(\tau)} + \frac{z^2}{Z^2(\tau)}$$

Exact solution with arbitrary scaling function  $\nu > 0$

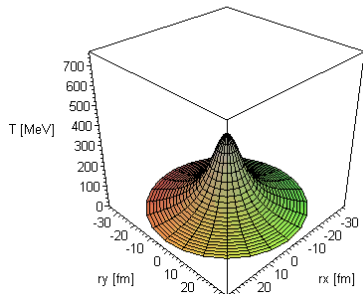
$$\begin{aligned}u^\mu &= \frac{x^\mu}{\tau}, & n &= n_0 \left(\frac{\tau_0}{\tau}\right)^3 \nu(s), \\ p &= p_0 \left(\frac{\tau_0}{\tau}\right)^{3+3/\kappa}, \\ T &= T_0 \left(\frac{\tau_0}{\tau}\right)^3 \frac{1}{\nu(\tau)}\end{aligned}$$

## M. Csanàd: Elliptic analytic hydro solution

Temperature in Au+Au collisions



Temperature in Au+Au collisions



$$\kappa = 3/2$$

- ▶ Different EoS/initial conditions  $\Rightarrow$  same hadronic final state
- ▶ EoS cannot be extracted from hadronic observables

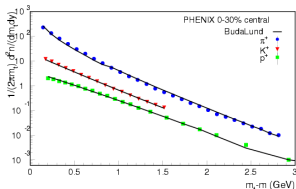
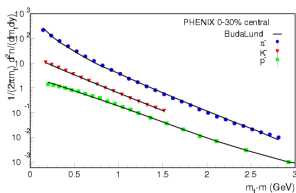
$$\kappa = 3$$

# M. Csanàd: Buda-Lund Model

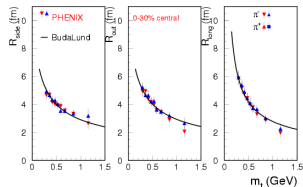
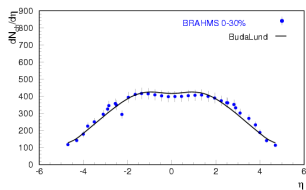
- EoS:  $\kappa = 3/2$ , 3D scaling solution (“anisotropic Hubble expansion”)

$$v_{2n} = \frac{I_n(w)}{I_0(w)}, \quad w = \frac{p_t^2}{4m_t} \left( \frac{1}{\partial_x T} - \frac{1}{\partial_y T} \right)$$

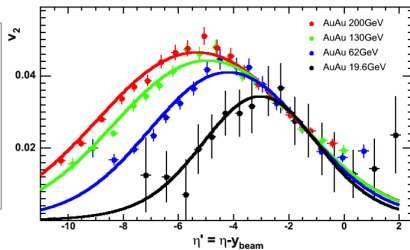
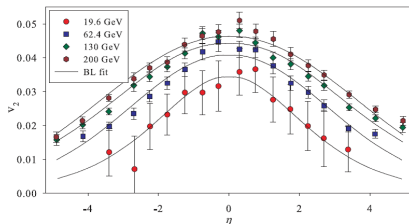
BudaLund v1.5 hydro fits to 200 AGeV Au+Au



BudaLund v1.5 fits to 200 AGeV Au+Au

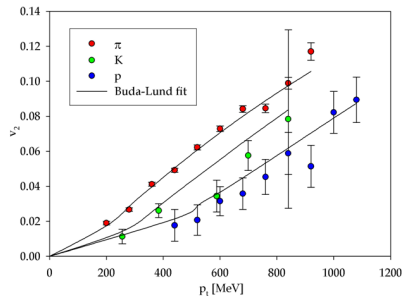
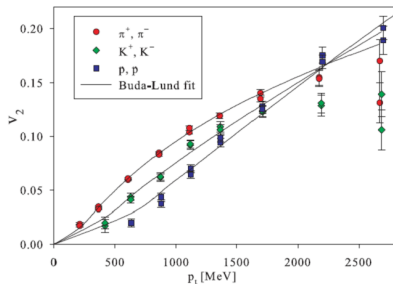


## M. Csanàd: Buda-Lund Model

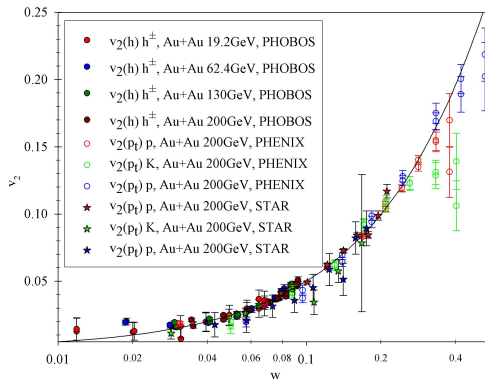


- ▶ high  $\eta \Rightarrow$  emission asymmetry vanishes  $\Rightarrow v_2 \rightarrow 0$
- ▶ Reasons: 3D Hubble flow + finite size

## M. Csanàd: Buda-Lund Model



# M. Csanàd: Buda-Lund Model





# M. Csanàd: Buda-Lund Model

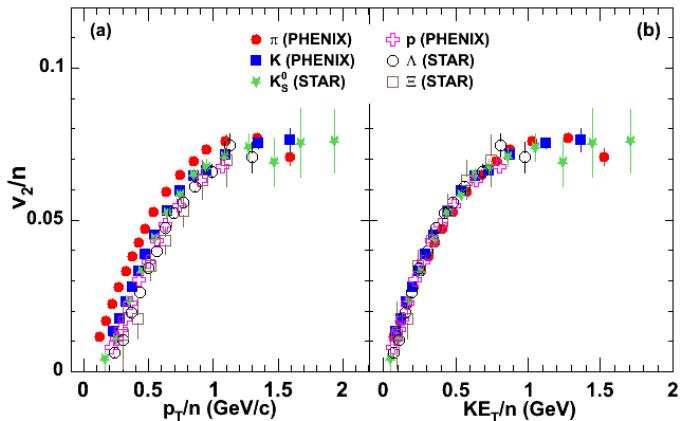
- ▶  $\eta$ -dependence of  $v_2$ 
  - ▶ width determined by longitudinal expansion,  $\Delta\eta$
  - ▶ height determined by eccentricity,  $\epsilon$
  - ▶ **two-parameter fit**
  - ▶  $\Delta\eta, \epsilon$  increase with  $\sqrt{s}$
  - ▶ vanishing at high  $\eta$ : 3D-Hubble expansion + finite long. size
- ▶  $p_T$ -dependence
  - ▶ depends on temperature gradients and transverse flow
  - ▶ **two-parameter fit**
  - ▶ increasing centrality  $\Rightarrow$  increasing transverse flow
  - ▶ inhomogeneous temperature, depending on PID
  - ▶  $v_2$  follows predicted scaling function
  - ▶ perfect fluid at all  $\eta$ !

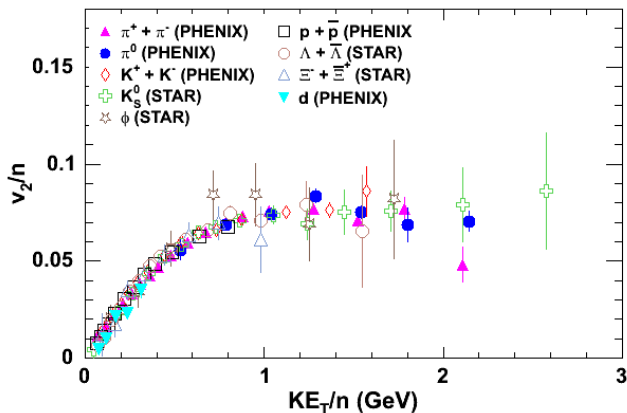
# M. Bleicher: UrQMD

- ▶ reproduce correct non-flow correlations
- ▶ part of  $v_2$  might come from hadronic stage
- ▶ correct mass ordering
- ▶ constituent-quark scaling reproduced without coalescence!
- ▶ transport models without QGP have lack of pressure

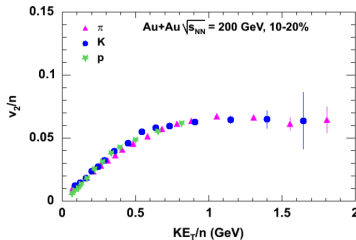
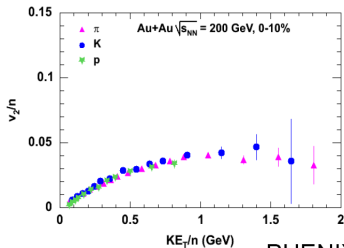
# M. Issah (PHENIX): Scaling characteristics of $v_2$ at RHIC

- ▶ eccentricity scaling holds over broad range of centralities  $\Rightarrow$  **indication for thermalization**
- ▶ comparison to hydro model  $\Rightarrow$  estimate of  $c_s^2 \Rightarrow$  compatible with **soft EoS**
- ▶  $KE_t$  scaling of baryons and mesons together for  $p_T < 1$  GeV  $\Rightarrow$  **indication of partonic dof's**
- ▶ **universal constituent-quark  $KE_t$  scaling** over broad range of centralities and PID

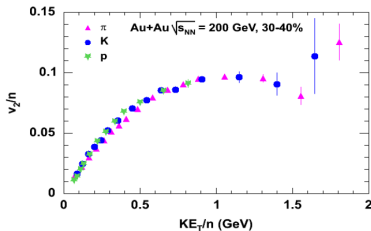
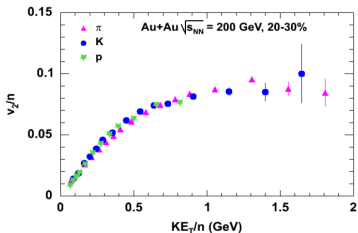
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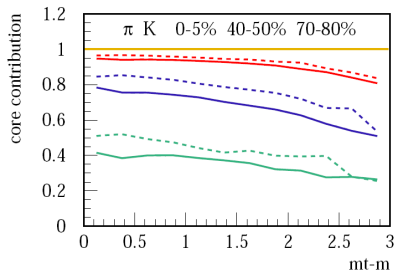
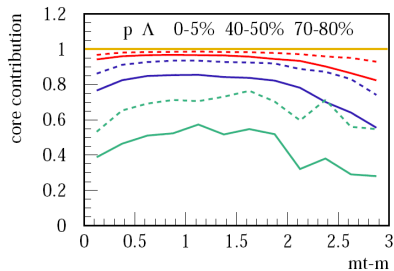
PHENIX preliminary data



## K. Werner: Surface effects in Au-Au at RHIC

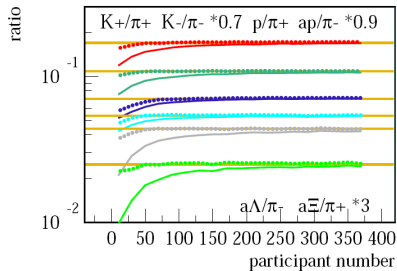
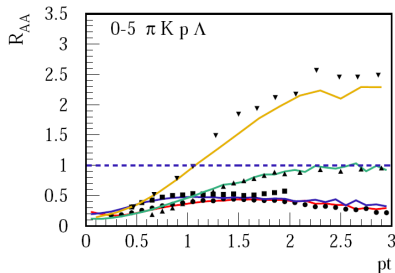
- ▶ peripheral nucleons in AA-collisions perform independent pp- or pA-like collisions
- ▶ goal: subtract this “corona background” from core
- ▶ use EPOS for pp- and pA-collisions
  - ▶ initial binary collisions create partons with initial- and final-state radiation
  - ▶ hadronization via strings
  - ▶ regions with string density  $> \rho_0 = 1\text{fm}^{-3}$ : **core**
  - ▶ rest: **corona**
  - ▶ connected high-density areas: **cluster**
- ▶ clusters hadronize at  $\epsilon_{\text{had}}$  statistically (micro canonical)
- ▶ have radial flow with linear radial rapidity profile ( $y_{\text{rad}}$ )
- ▶ anisotropy by multiplying  $v_x$  and  $v_y$  by  $1 \pm \epsilon f_{\text{ecc}}$

## K. Werner: Surface effects in Au-Au at RHIC





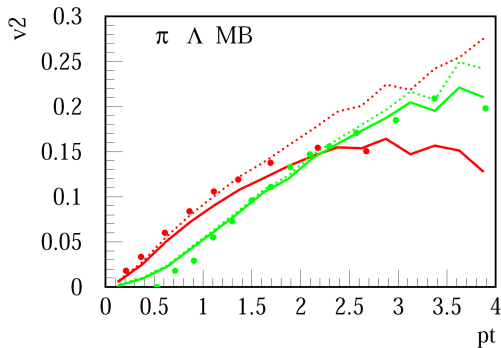
# K. Werner: Surface effects in Au-Au at RHIC



## K. Werner: Surface effects in Au-Au at RHIC

**Elliptical flow in MB AuAu collisions at 200 GeV.**

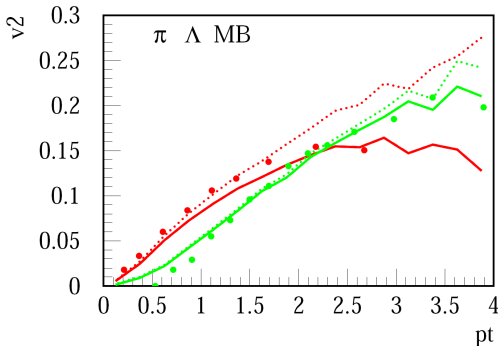
pions (red) and lambdas (green). data: PHENIX/STAR

**Full lines: core + corona; dotted lines: core**

## K. Werner: Surface effects in Au-Au at RHIC

**Elliptical flow in MB AuAu collisions at 200 GeV.**

pions (red) and lambdas (green). data: PHENIX/STAR

**Full lines: core + corona; dotted lines: core**

- ▶ core: **no centrality dependence** (only volume)
- ▶ baryons more suppressed in string fragmentation (pp) than in statistical hadronization (core in AA)
- ▶ core the same at **RHIC and SPS** (modulo 30% more flow at RHIC)

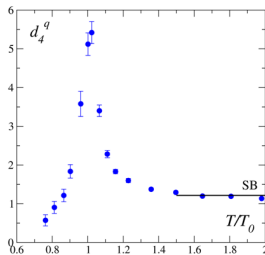
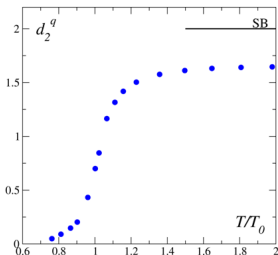
## P. Petrecky: Lattice QCD at finite temperature

- ▶ various **number susceptibilities** in 2-flavor QCD
- ▶ “event-by-event fluctuations”

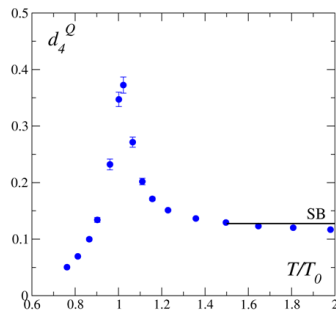
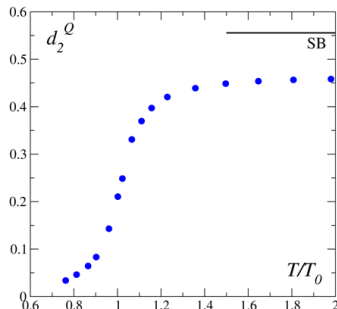
$$d_n^x := \left. \frac{\partial^n [-p(T, \mu_x)]}{\partial (\mu_x/T)^n} \right|_{\mu_x=0}$$

$$d_2^x = \frac{1}{VT^3} \langle N_x^2 \rangle \Big|_{\mu_x=0},$$

$$d_4^x = \frac{1}{VT^3} (\langle N_x^4 \rangle - 3 \langle N_x^2 \rangle) \Big|_{\mu_x=0}$$



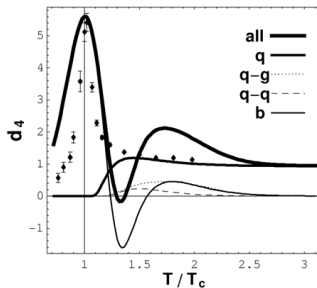
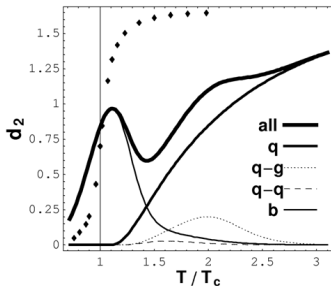
## P. Petrecky: Lattice QCD at finite temperature



- ▶ Close to **Stefan-Boltzmann limit** of parton gas for  $T \gtrsim 1.5 T_c$
- ▶ Relevant degrees of freedom: partonic (quasi) particles

## P. Petrecky: Lattice QCD at finite temperature

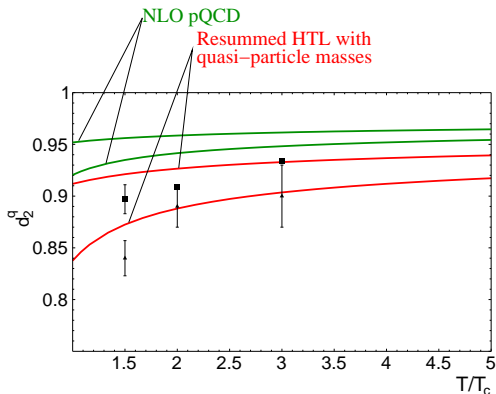
- ▶ Comparison to **sQGP** model  
Lian, Shuryak, PRD **73**, 014509 (2006)
- ▶ significance of **qg-** and **qq-bound states**



- ▶ Bound states **not compatible** with IQCD
- ▶ Ejiri, Karsch, Redlich, PLB **633**, 275 (2006)  
Koch, Majumber, Randrup, PRL **95**, 182301 (2005)

## P. Petrecky: Lattice QCD at finite temperature

- ▶ Comparison to pQCD and CJT-improved HTL
- ▶ different renormalization scales ( $\bar{\mu} = \pi T \dots 4\pi T$ )
- ▶ Lattice data: 2 different continuum extrapolations
- ▶ Blaizot, Iancu, Rebhan hep-ph/0303185



# P. Petrecky: Lattice QCD at finite temperature

- ▶ bulk thermodynamic observables
  - ▶ dominant degrees of freedom for  $T > 1.2T_c$  are quarks and gluons
  - ▶ **perturbation theory** can account for deviation from free-gas limit for  $T > 1.5T_c$
  - ▶ **sQGP models** inconsistent with lattice data
- ▶ Heavy quarks
  - ▶ no evidence for “strongly coupled Coulomb phase”,  
 $\alpha_s(r, T) < \alpha_s(r, T = 0)$
  - ▶ 1S charmonia ( $J/\psi, \eta_c$ ) survive till  $T > 1.5T_c$
  - ▶ 1P charmonia melt ( $\chi_{c0}, \chi_{c1}$ ) at  $T \gtrsim 1.1T_c$
  - ▶ 1S bottomonia ( $\Upsilon, \eta_c$ ) survive till  $T \gtrsim 3T_c$
  - ▶ 1P bottomonia melt at  $T \gtrsim 1.5T_c$
- ▶ light meson correlators
  - ▶ no evidence for bound states
  - ▶ low-mass dilepton rates **suppressed in IQCD**  
(artifact, generation of quasi-particle masses?)

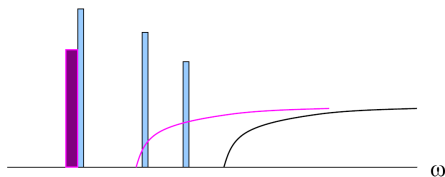


# À. Mòcsy: Quarkonia above deconfinement

- use simple toy model to compare **lattice correlators** to **potential models**

$$G_H(\tau, T) := \left\langle \mathbf{j}_H(\tau) \mathbf{j}_H^\dagger(0) \right\rangle_T = \int d\omega \sigma(\omega, T) K(\tau, \omega, T)$$

$$K(\tau, \omega, T) = \frac{\cosh[\omega(\tau - 1/(2T))]}{\sinh[\omega/(2T)]}$$



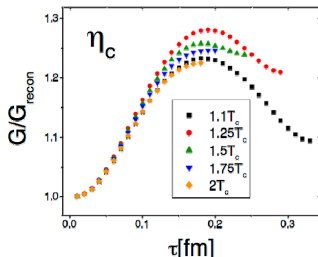
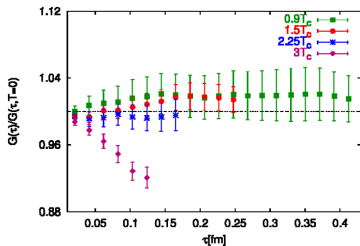
$$\sigma(\omega) = \sum_i 2M_i F_i^2 \delta(\omega^2 - M_i^2) + \frac{3}{8\pi^2} \omega^2 \Theta(\omega - s_0) f(\omega, s_0),$$

$$f(\omega) = \left( a_H + b_H \frac{s_0}{\omega^2} \right) \sqrt{1 - \frac{s_0^2}{\omega^2}}$$

# À. Mòcsy: Quarkonia above deconfinement

For potential models:

$$s_0(T) = 2m + V_\infty(T), \quad M_i = 2m + E_i$$



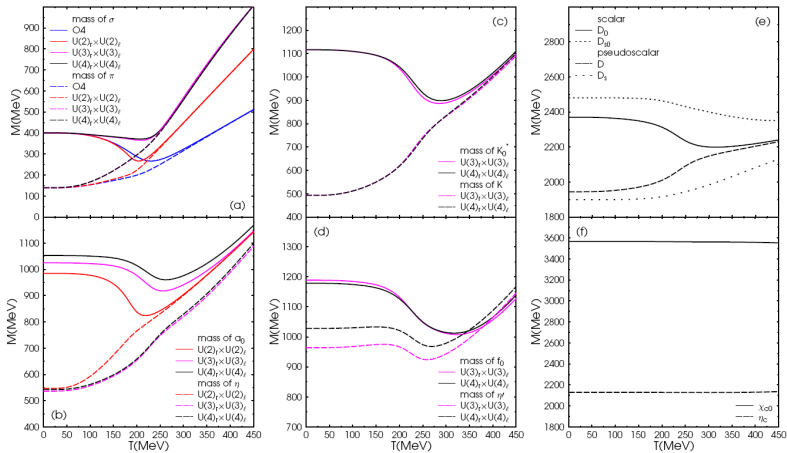
- ▶  $J/\psi$ ; lattice: no change up to  $T = 2T_c$
- ▶ potential mod.: first increase due to threshold reduction, then increase due to amplitude reduction
- ▶ **no agreement with lattice**

## À. Mòcsy: Quarkonia above deconfinement

- ▶ works with toy model
  - ▶ no temperature dependent screening
  - ▶ continuum threshold reduction
  - ▶ no modification of 1s properties
  - ▶ melting of 2s and 3s states
  - ▶ melting of 1p state
- ▶  $T$ -dependent lattice quarkonia correlators neither explained by screened Cornell potential nor lattice internal energy
- ▶ simple model without screening works
- ▶ screening not responsible for quarkonia suppression

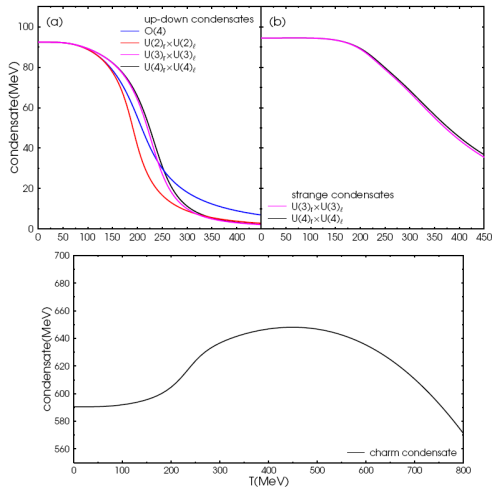
D. Rischke: Chiral symmetry restoration in linear  $\sigma$  models

Masses in HF approximation: Dirk Röder, Jörg Ruppert, DHR, PRD 68 (2003) 016003



D. Rischke: Chiral symmetry restoration in linear  $\sigma$  models

## Condensates



# D. Rischke: Chiral symmetry restoration in linear $\sigma$ models

## Chiral symmetry restoration in linear sigma models:

### 1. Scalar and pseudoscalar mesons:

- $O(4)$  and  $U(N_f)_r \times U(N_f)_\ell$  models ( $N_f = 2, 3, 4$ ) in Hartree-Fock approximation
- $O(4)$  model in 2-loop approximation ( $\text{Re } \Pi \equiv \Pi_{\text{tadpole}}$ )
- Inclusion of energy-momentum dependent part of  $\text{Re } \Pi$
- $U(N_f)_r \times U(N_f)_\ell$  models in 2-loop approximation

### 2. Vector and axialvector mesons:

- $U(2)_r \times U(2)_\ell$  model in HF approximation
- Full 2-loop approximation
- Extension to  $N_f = 3, 4$

### 3. Baryons

### 4. Coupling to photon

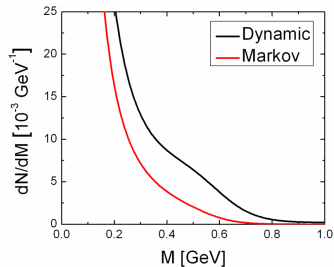
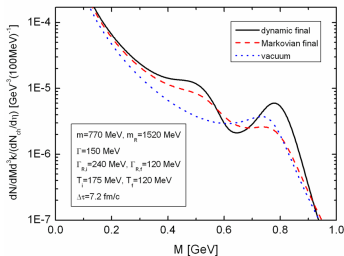
### 5. Dilepton rate, spectrum

## C. Greiner: Nonequilibrium dilepton production

- ▶ Kadanoff-Baym equation for vector mesons (**real-time contour**)

$$\hat{D}_1 G(1, 1') = \delta_{\mathcal{C}}^{(4)}(1 - 1') + \Sigma(1, 2) \otimes G(2, 1')$$

- ▶ nonlocal in time  $\Rightarrow$  **memory effects**
- ▶ put in  $\text{Im} \Sigma_{\rho}^R$  by hand
- ▶ use **equilibrium distribution** in matrix formalism



## C. Greiner: Nonequilibrium dilepton production

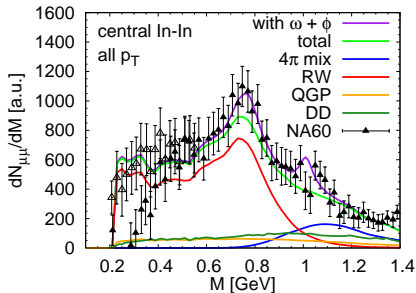
- ▶ time scales of **retardation**  $\approx c/\Gamma_{\text{vac}}$  with  $c = 2 \dots 3$
- ▶ **quantum mechanical interference effects** (in Wigner transform)  
**Yields positive!**
- ▶ **Non-equilibrium effects on yields** compared to adiabatic approximation
- ▶ **Memory effects** important for correct treatment of in-medium modifications



# HvH: Medium modifications of hadrons and em. probes

- ▶ intermediate mass range: **Mixing** of  $\Pi_V$  with  $\Pi_A$  (Dey, Eletsky, Ioffe '90)

$$\Pi_V^{(T)} = (1 - \epsilon)\Pi_V + \epsilon\Pi_A, \quad \epsilon = \frac{1}{2} \frac{\mathcal{T}_\pi(T, \mu_\pi)}{\mathcal{T}_\pi(T_c, 0)} \propto \text{diagram}$$




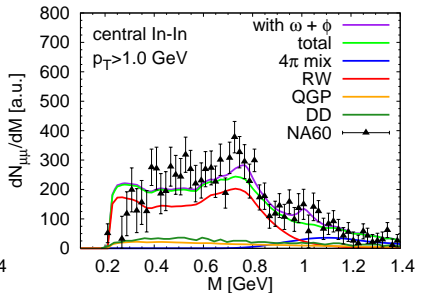
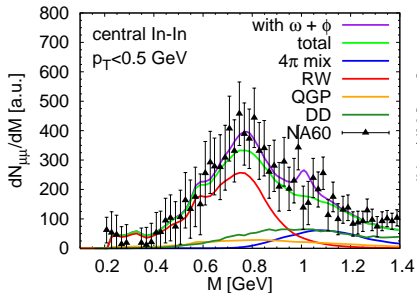
(hep-ph/0603084)

- ▶ **Fireball model**  $\Rightarrow$  time evolution
- ▶ **absolute normalization!**
- ▶ **good overall agreement with data**
- ▶ **sensitive to  $\omega$  and  $\phi$ !**
- ▶  $\omega$ : similar model as for  $\rho$
- ▶  $\phi$ : less well known; width assumed  $\simeq 80$  MeV

# HvH: Medium modifications of hadrons and e.m. probes

- ▶  $2\pi$  contributions +  $\rho B$  interactions from Rapp+Wambach '99
- ▶ intermediate mass range: **Mixing** of  $\Pi_V$  with  $\Pi_A$

$$\Pi_V^{(T)} = (1 - \epsilon)\Pi_V + \epsilon\Pi_A, \quad \epsilon = \frac{1}{2} \frac{\mathcal{T}_\pi(T, \mu_\pi)}{\mathcal{T}_\pi(T_c, 0)} \propto \text{Diagram}$$




- ▶ **same absolute normalization!**
- ▶ “Corona effect” for high  $p_T$ ?

# HvH: Medium modifications of hadrons and e.m. probes

- ▶ chiral symmetry: important feature to connect QCD ↔ hadronic effective models
- ▶ important property of (s)QGP: How is chiral symmetry restored?
- ▶ electromagnetic probes may provide most direct insight
  - ▶ invariant-mass spectra for chiral partners: here  $\rho$  and  $a_1$
  - ▶ low-energy photons ↔ dileptons (puzzle?)
- ▶ a lot to do also for theory
  - ▶ consistent chiral scheme for hadrons
  - ▶ self-consistent treatment of (axial-) vector particles
  - ▶ equation of state including in-medium modifications vs. statistical models with “free hadron properties”

## Final hint

transparencies/presentations online

<http://rhic.physics.wayne.edu/~bellwied/sandiego06/program.html>