

Electromagnetic probes in the GiBUU Transport Model

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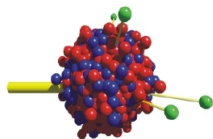
**Institut für
Theoretische Physik**



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- 2 The GiBUU model
 - The Boltzmann-Uehling-Uhlenbeck Equation
 - Off-shell transport: kinetics of broad resonances
- 3 Dileptons
 - pp collisions (HADES)
 - $p\text{Nb}$ (HADES)
- 4 ω production in γA collisions

Motivation for Transport Models

- description of various nuclear reactions within one framework
 - pA , γA , eA , νA , AA
- time evolution of system \Rightarrow need dynamical approach
- **transport models** well suited for Monte-Carlo simulations (test-particle approach)
- strongly interacting many-body system: “medium modifications” of hadrons
- challenging task: description of broad resonance-like excitations
 - off-shell transport with consistent dynamical evolution of spectral properties
 - conservation laws
 - thermodynamic consistency
- in this talk: **GiBUU** model
 - dileptons in pp and $p\text{Nb}$ collisions (HADES)
 - ω production in γA (CBELSA/TAPS)



GiBUU

The Giessen Boltzmann-Uehling-Uhlenbeck Project

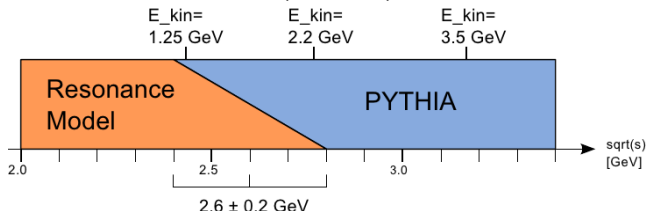
- BUU framework for hadronic transport
- reaction types: pA , πA , γA , eA , νA , AA
- open-source modular Fortran 95/2003 code
- version control via Subversion
- publicly available releases:
<http://gibuu.physik.uni-giessen.de>

The Boltzmann-Uehling-Uhlenbeck Equation

- time evolution of **phase-space distribution functions**

$$[\partial_t + (\vec{\nabla}_p H_i) \cdot \vec{\nabla}_x - (\vec{\nabla}_x H_i) \cdot \vec{\nabla}_p] f_i(t, \vec{x}, \vec{p}) = I_{\text{coll}}[f_1, \dots, f_i, \dots, f_j]$$

- Hamiltonian H_i
 - selfconsistent hadronic mean fields, Coulomb potential, “off-shell potential”
- collision term I_{coll}
 - two- and three-body decays/collisions
 - multiple coupled-channel problem
 - at low reaction energies: resonance model
 - at high reaction energies: (modified) PYTHIA



Transport model for broad resonances

- resonances described with relativistic Breit-Wigner distribution

$$\mathcal{A}(x, p) = -\frac{1}{\pi} \frac{\text{Im } \Pi}{(p^2 - M^2 - \text{Re } \Pi)^2 + (\text{Im } \Pi)^2}; \quad \text{Im } \Pi = -\sqrt{p^2} \Gamma$$

- full off-shell equation from quantum-transport approach [Botermans, Malfliet,...] hard to solve due to “back-reaction term”
- way out: off-shell potential ansatz [Effenberger, Mosel; Leupold; Cassing, Juchem; Buss]
- in test-particle ansatz: **off-shell potential**, $\Delta\mu_i^2$,

$$p_i^2 = M^2 + \text{Re } \Pi + \Delta\mu_i^2, \quad \chi_i = \frac{\Delta\mu_i^2}{\Gamma_i}$$

- off-shell equations of motion

$$\dot{\vec{r}}_i = \frac{1}{1 - C_i} \frac{1}{2E_i} \left[2\vec{p}_i + \vec{\nabla}_{p_i} (\text{Re } \Pi_i + \chi_i \Gamma_i) \right]$$

$$\dot{\vec{p}}_i = -\frac{1}{1 - C_i} \frac{1}{2E_i} \vec{\nabla}_r (\text{Re } \Pi_i + \chi_i \Gamma_i)$$

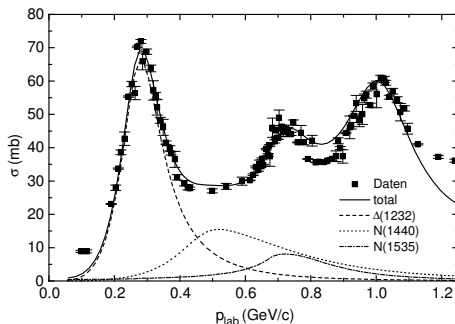
$$C_i = \frac{1}{2E_i} \frac{\partial}{\partial E_i} (\text{Re } \Pi_i + \chi_i \Gamma_i), \quad \dot{\chi}_i = 0$$

Resonance Model

- reactions dominated by resonance scattering: $ab \rightarrow R \rightarrow cd$
- Breit-Wigner cross-section formula

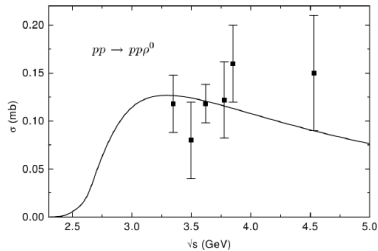
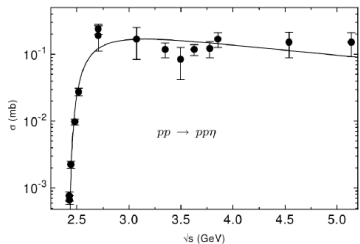
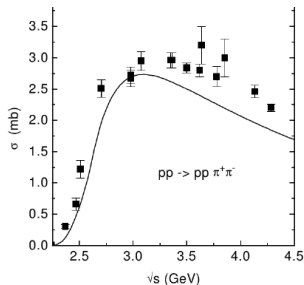
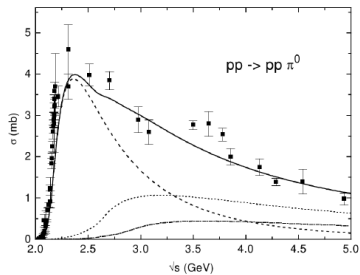
$$\sigma_{ab \rightarrow R \rightarrow cd} = \frac{2s_R + 1}{(2s_a + 1)(2s_b + 1)} \frac{4\pi}{p_{\text{lab}}^2} \frac{s\Gamma_{ab \rightarrow R}\Gamma_{R \rightarrow cd}}{(s - m_R^2)^2 + s\Gamma_{\text{tot}}^2}$$

- applicable for low-energy nuclear reactions $E_{\text{kin}} \lesssim 1.1 \text{ GeV}$
- example: $\sigma_{\pi^- p \rightarrow \pi^- p}$ [Teis (PhD thesis 1996)]



Resonance Model

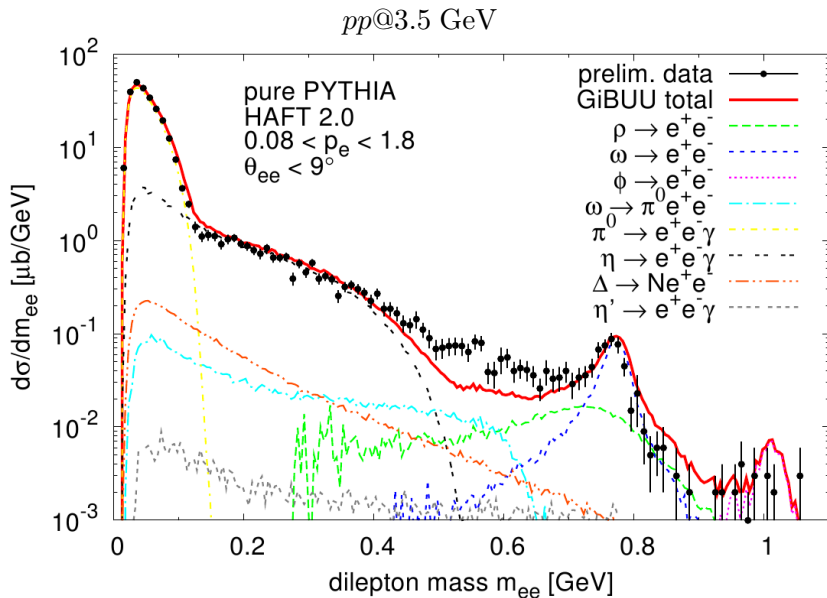
- further cross sections



The Dilepton Probe

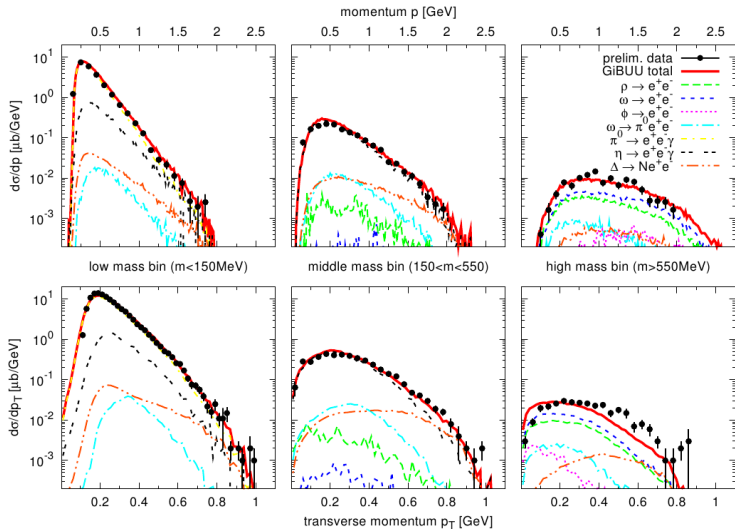
- dileptons valuable probe for **in-medium properties of vector mesons**
- main sources
 - Dalitz decays: $\pi^0, \eta \rightarrow \gamma \ell^+ \ell^-$; $\omega \rightarrow \pi^0 \ell^+ \ell^-$, $\Delta \rightarrow N \ell^+ \ell^-$
 - $\rho, \omega, \phi \rightarrow \ell^+ \ell^-$: invariant mass $\ell^+ \ell^-$ spectra \Rightarrow
spectral properties of vector mesons
- provides **direct access** to in-medium properties of vector mesons, if they decay inside the medium!
- in GiBUU: strict vector-dominance model $J_{em}^{\text{had}} \propto V^\mu$

Comparison to HADES data



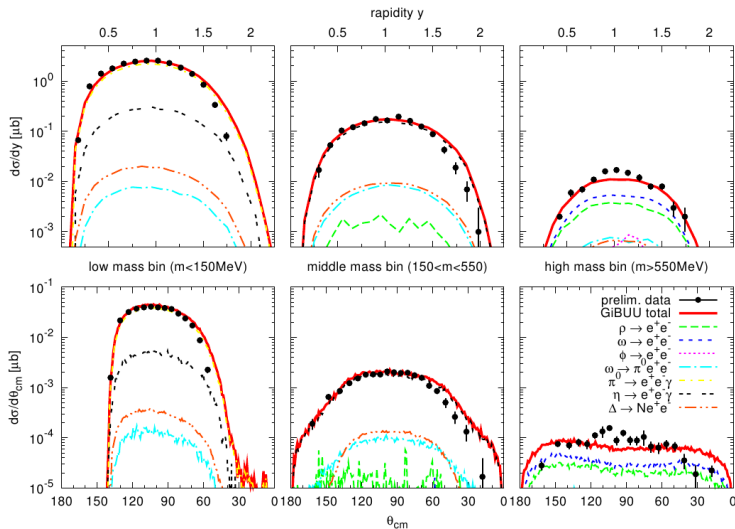
Comparison to HADES data

$pp@3.5$ GeV



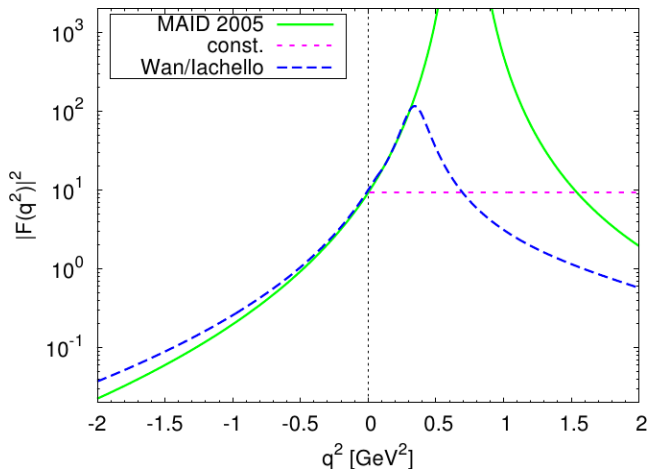
Comparison to HADES data

$pp@3.5$ GeV

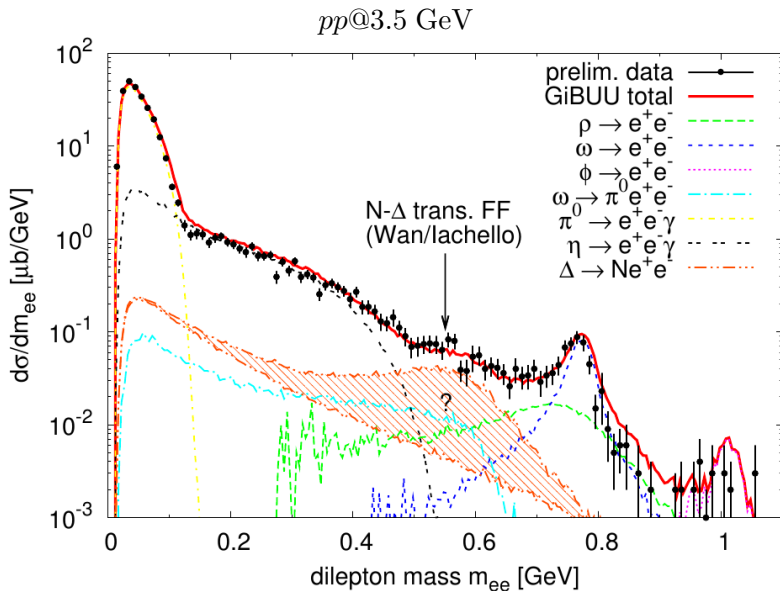


Δ -Dalitz Decay

- transition-form factor $\Delta \rightarrow N\gamma^*$
- unknown in time-like region
- two-component quark model [Wan, Iachello, IJP A 20 (2005)]

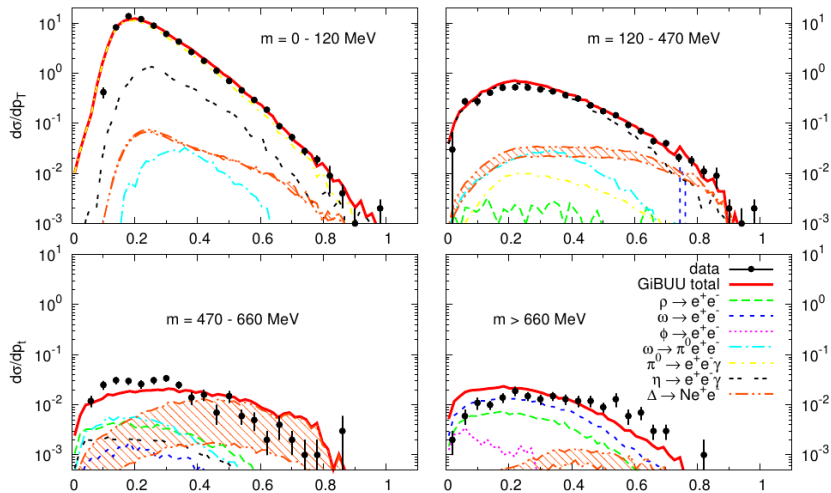


Comparison to HADES data with Δ form factor

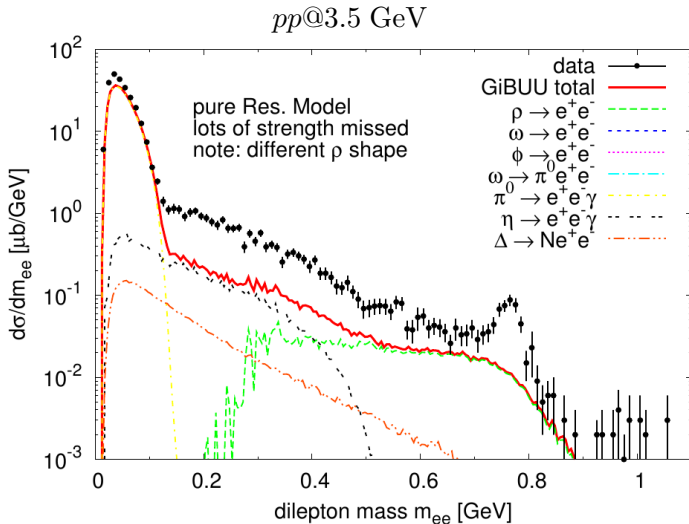


Comparison to HADES data with Δ form factor

$pp@3.5$ GeV
transverse momentum p_T [GeV]



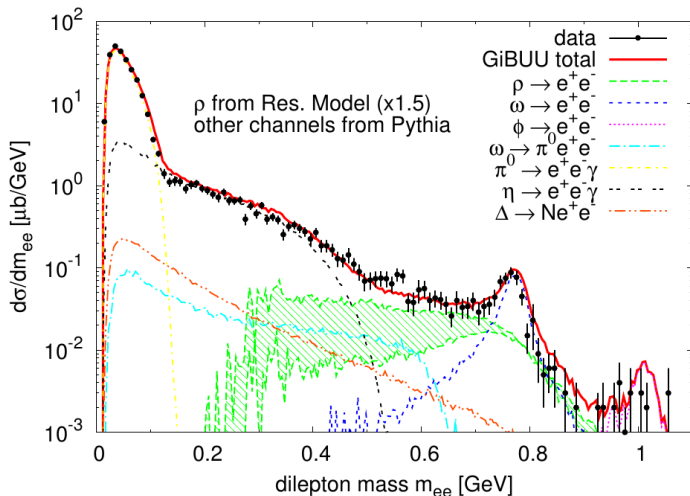
Comparison to HADES data with resonance model



- need higher resonances at this energy
- ρ shape changes

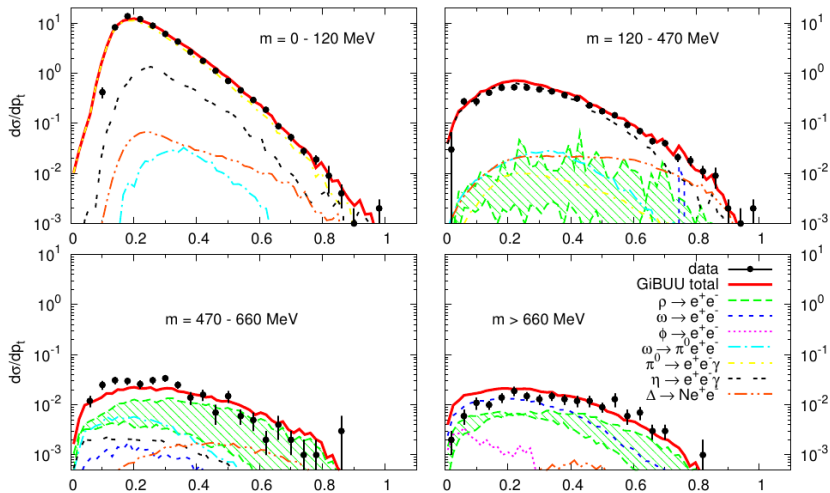
Comparison to HADES data with resonance model+PYTHIA

- use ρ shape from resonance model (rescaled by factor 1.5!)
- use PYTHIA for all other channels as before



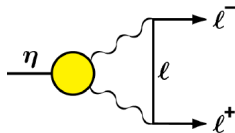
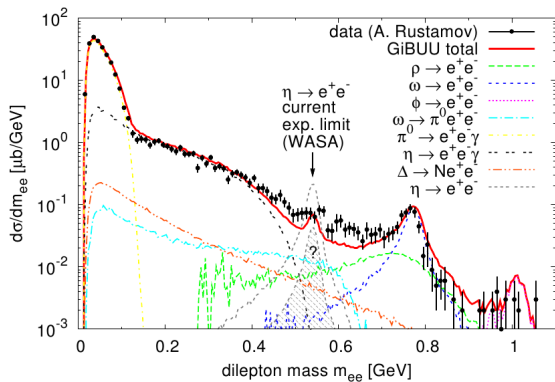
Comparison to HADES data with Δ form factor

$pp@3.5$ GeV
transverse momentum p_t [GeV]

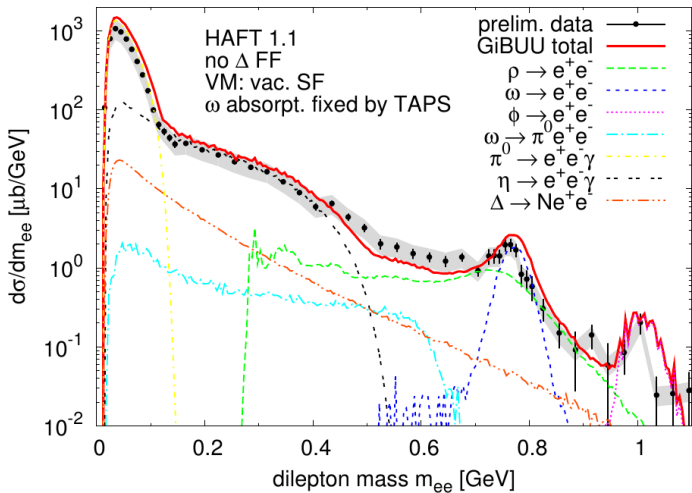


Improved experimental upper limit for $\eta \rightarrow e^+e^-$?

- upper limit from [Berlowski et al [WAFA Collab.], PRD 77 (2008)]:
 $\text{BR}(\eta \rightarrow e^+e^-) < 2.7 \cdot 10^{-5}$
- theoretical prediction [Browder et al, PRD 56 (1997)]: $\text{BR}(\eta \rightarrow e^+e^-) \simeq 10^{-9}$

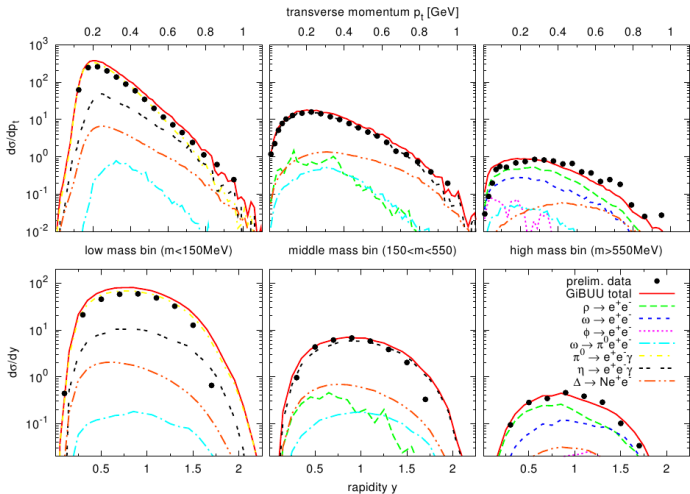


- pp baseline as input (including the discussed uncertainties!)
cross sections, branching ratios, form factors, etc.
- medium effects built in transport model
 - final-state interactions
 - production from secondary collisions
- additional impact from vector-meson spectral functions?

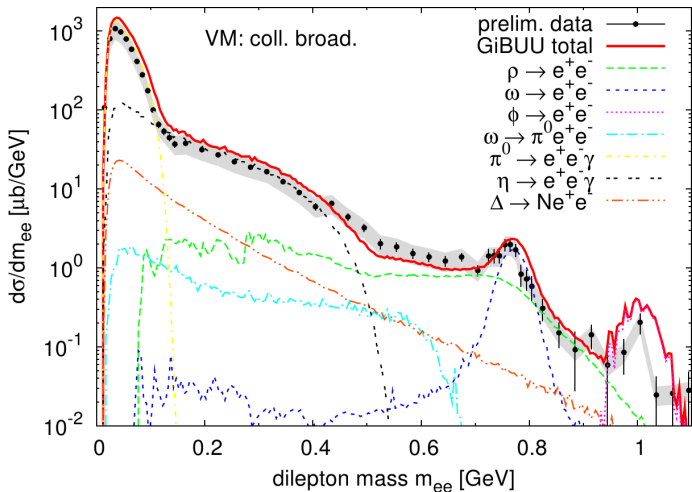


- discrepancy in normalization (π_0 Dalitz?)
- acceptance issue?

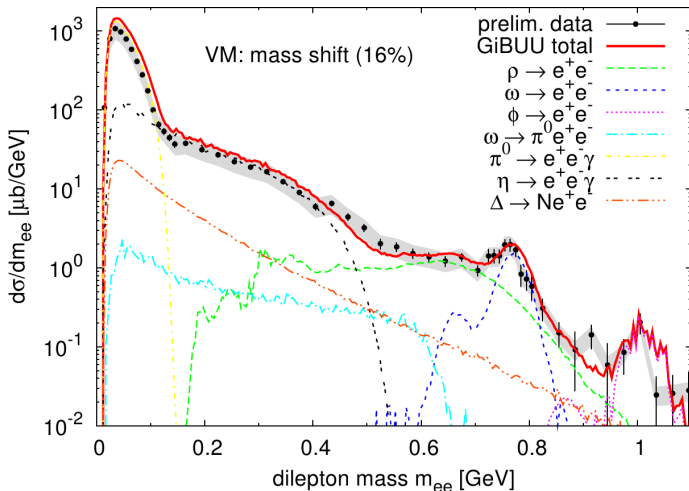
$p\text{Nb@HADES}$ (3.5 GeV)



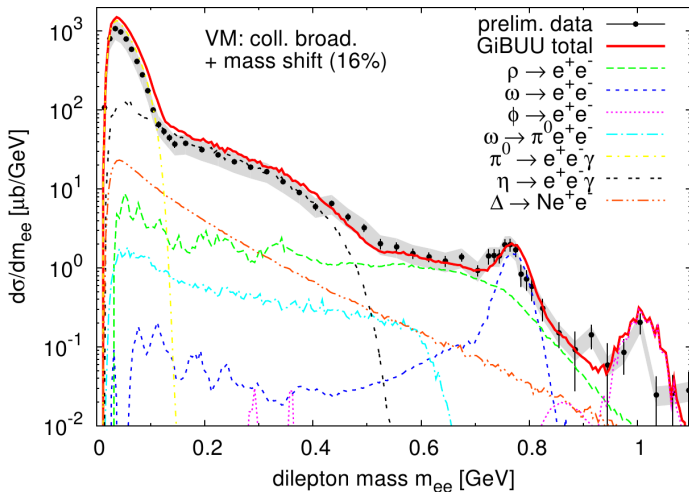
- medium modifications of vector-meson spectral functions?
- collisional broadening



- medium modifications of vector-meson spectral functions?
- dropping mass (16% at nuclear-matter density)

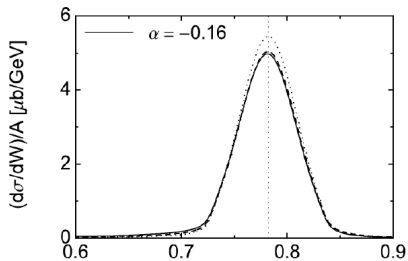
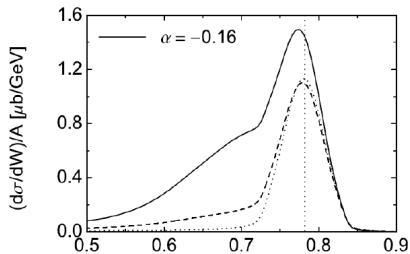


- medium modifications of vector-meson spectral functions?
- dropping mass + collisional broadening



ω production in γA collisions

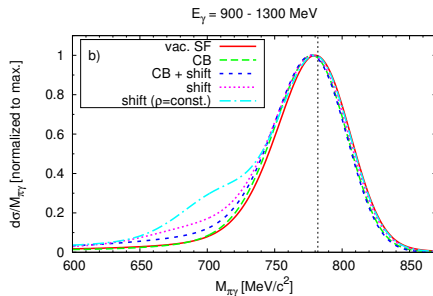
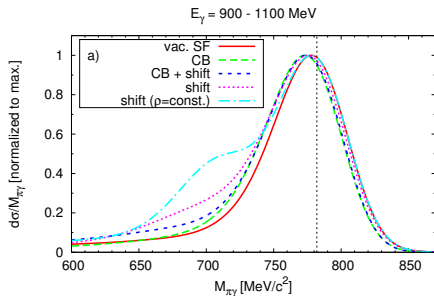
- main motivation: **medium effects on ω spectral function**
- earlier GiBUU simulations by Mühlich
- γ ^{40}Ca , $E_\gamma = 0.9\text{-}1.2$ GeV
- large low-mass tail
- threshold effect
- γ ^{40}Ca , $E_\gamma = 1.5\text{-}2.2$ GeV
- nearly no effect



[Gallmeister, Kaskulov, Mosel, Prog. Part. Nucl. Phys. **61**, 283 (2008)]

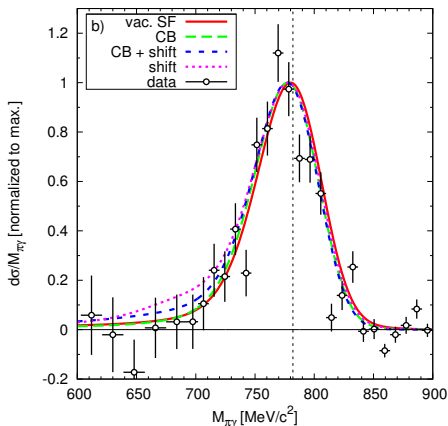
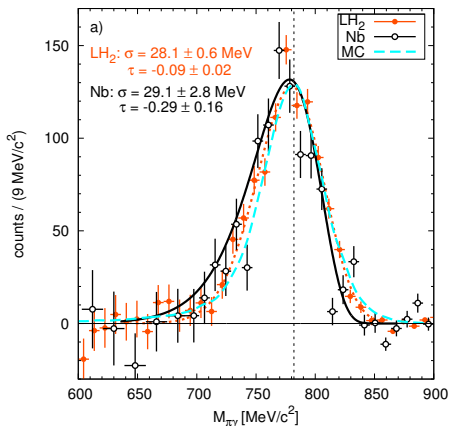
ω production in γA collisions (CBELSA/TAPS)

- improved implementation of **off-shell transport**
- spectral functions relax properly to vacuum shape!



ω production in γA collisions (CBELSA/TAPS)

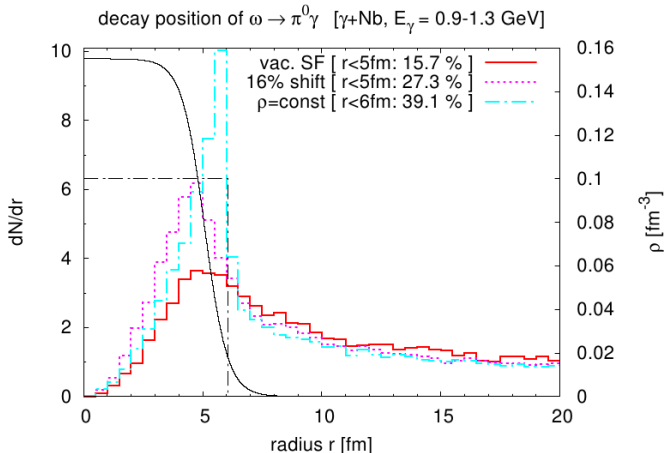
- improved implementation of **off-shell transport**
- spectral functions relax properly to vacuum shape!
- $E_\gamma = 0.9\text{-}1.3$ GeV



[Nanova, Weil et al, Eur. Phys. J. A 47, 16 (2011)]

Position of decaying ω 's

- not so much sensitivity to in-medium effects
 - few ω 's decay inside the nucleus
 - strong **in-medium broadening**
 - density profile of nucleus
- **correct implementation of off-shell transport crucial!**



Conclusions

- GiBUU transport model
 - comprehensive model for pA , πA , γA , eA , νA , AA collisions
 - dynamically consistent transport of broad resonances via “off-shell potential”
 - open-source releases available (Fortran 95/2003)
 - <http://gibuu.physik.uni-giessen.de>
- Dilepton probes@HADES
 - resonance model for VM production ($E_{\text{kin}} \lesssim 1.1$ GeV)
 - vector-meson dominance model for dileptons
 - modified PYTHIA at higher energies
 - pp baseline: still uncertainties in VM region (form factors)
 - pA : within uncertainties no clear indication of medium effects (also in normalization/acceptance)
 - AA : work in progress
- photoproduction of ω mesons on nuclei
 - mass spectra inconclusive wrt. medium effects
 - consistent off-shell transport crucial!
 - transparency ratio: large broadening of ω ($\Gamma_{\omega} \simeq 140$ MeV)