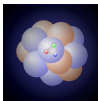


# Heavy-Quark Transport in the QGP

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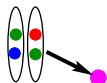


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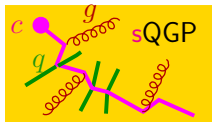
- Fast equilibration of hot and dense matter in heavy-ion collisions: collective flow (nearly ideal hydrodynamics)  $\Rightarrow$  sQGP
- Heavy quarks as calibrated probe of QGP properties
  - produced only in early hard collisions: well-defined initial conditions
  - not fully equilibrated due to large masses
  - **heavy-quark diffusion**  $\Rightarrow$  probes for QGP-transport properties
- Langevin simulation
- drag and diffusion coefficients
  - $T$ -matrix approach with static lattice-QCD **heavy-quark potentials**
  - **resonance formation** close to  $T_c$
  - mechanism for **non-perturbative strong interactions**

# Heavy Quarks in Heavy-Ion collisions



$c, b$  quark

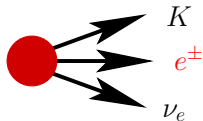
hard production of HQs  
described by PDF's + pQCD (PYTHIA)



HQ rescattering in QGP: Langevin simulation  
drag and diffusion coefficients from  
microscopic model for HQ interactions in the sQGP



Hadronization to  $D, B$  mesons via  
quark coalescence + fragmentation



semileptonic decay  $\Rightarrow$   
“non-photonic” electron observables  
 $R_{AA}^{e^+e^-}(p_T), v_2^{e^+e^-}(p_T)$

# Relativistic Langevin process

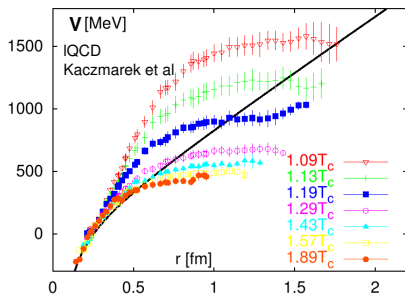
- **Langevin process**: friction force + Gaussian random force
- in the (local) rest frame of the heat bath

$$d\vec{x} = \frac{\vec{p}}{E_p} dt,$$

$$d\vec{p} = -A\vec{p}dt + \sqrt{2dt}[\sqrt{B_0}P_\perp + \sqrt{B_1}P_\parallel]\vec{w}$$

- $\vec{w}$ : normal-distributed random variable
- $A$ : friction (drag) coefficient
- $B_{0,1}$ : diffusion coefficients
- Einstein dissipation-fluctuation relation  $B_1 = E_p T A$ .
- flow via Lorentz boosts between “heat-bath frame” and “lab frame”
- $A$  and  $B_0$  from microscopic models for  $qQ$ ,  $gQ$  scattering

# Microscopic model: Static potentials from lattice QCD



- color-singlet free energy from lattice  $\rightarrow$  internal energy

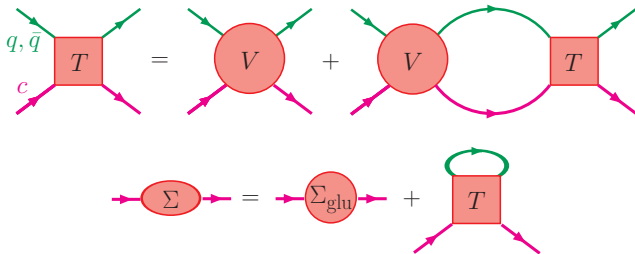
$$U_1(r, T) = F_1(r, T) - T \frac{\partial F_1(r, T)}{\partial T},$$

$$V_1(r, T) = U_1(r, T) - U_1(r \rightarrow \infty, T)$$

- Casimir scaling of Coulomb part for other color channels; confining part color blind [F. Riek, R. Rapp, Phys. Rev. C **82**, 035201 (2010)].

$$V_{\bar{3}} = \frac{1}{2}V_1, \quad V_6 = -\frac{1}{4}V_1, \quad V_8 = -\frac{1}{8}V_1$$

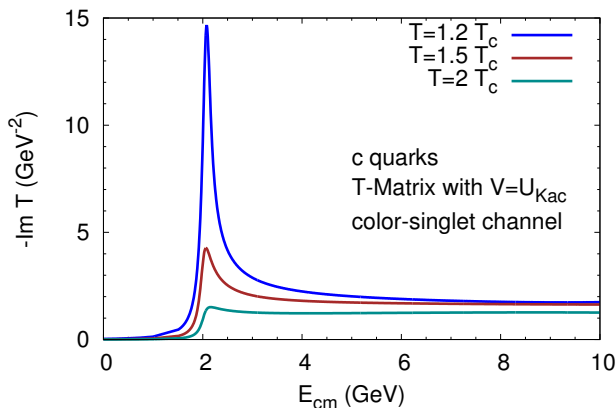
- Brueckner many-body approach for elastic  $Qq$ ,  $Q\bar{q}$  scattering



- reduction scheme: 4D Bethe-Salpeter  $\rightarrow$  3D Lipmann-Schwinger
- $S$ - and  $P$  waves
- Relation to invariant **matrix elements**

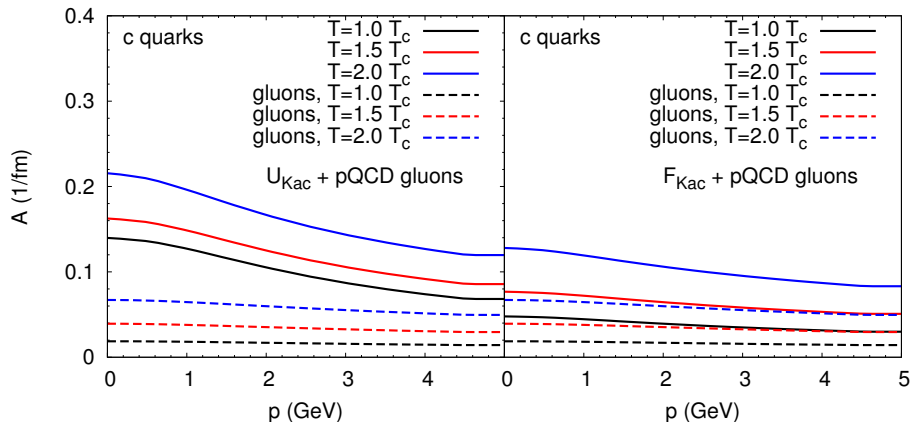
$$\sum |\mathcal{M}(s)|^2 \propto \sum_q d_a (|T_{a,l=0}(s)|^2 + 3|T_{a,l=1}(s)|^2 \cos^2 \theta_{\text{cm}})$$

# T-matrix results



- **resonance formation** at lower temperatures  $T \simeq T_c$
- melting of resonances at higher  $T$
- model-independent assessment of elastic  $Qq$ ,  $Q\bar{q}$  scattering!

# Transport coefficients

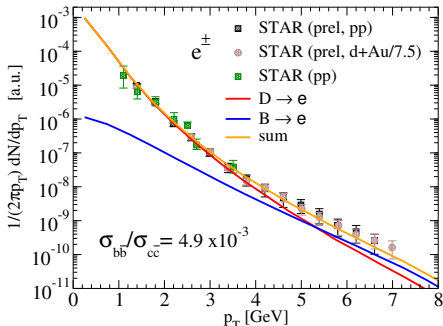
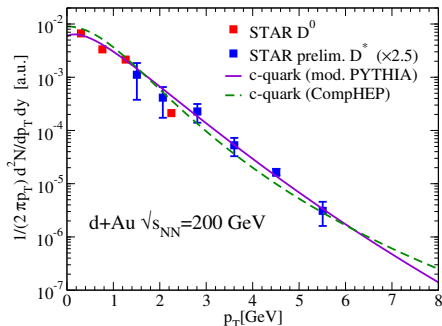


- from **non-pert.** interactions reach  $A_{\text{non-pert}} \simeq 1/(7 \text{ fm}/c) \simeq 4A_{\text{pQCD}}$
- results for **free-energy potential,  $F$**  considerably smaller

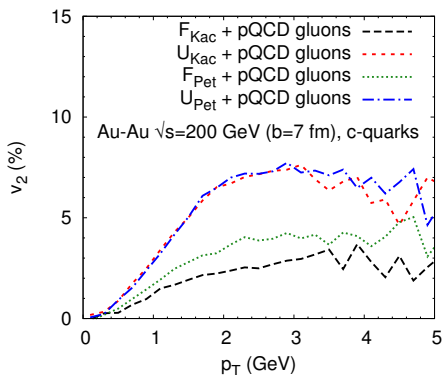
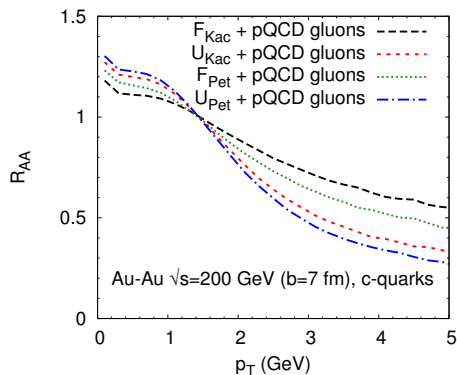


# Bulk evolution and initial conditions

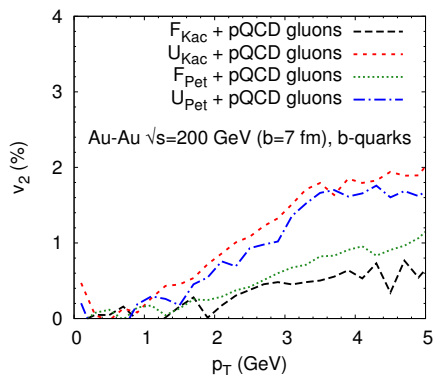
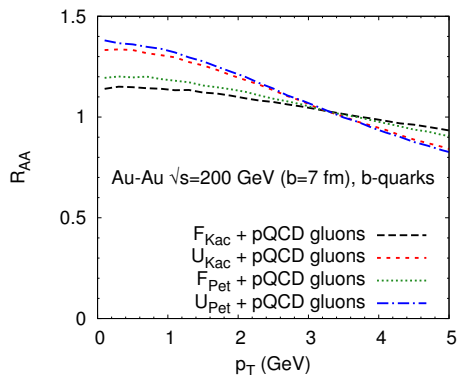
- bulk evolution as elliptic **thermal fireball**
- **isentropic expansion** with **QGP Equation of State**
- initial  $p_T$ -spectra of **charm** and **bottom** quarks
  - (modified) PYTHIA to describe exp. **D** meson spectra, assuming  **$\delta$ -function fragmentation**
  - exp. **non-photonic single- $e^\pm$**  spectra: Fix bottom/charm ratio



# Spectra and elliptic flow for c-quarks

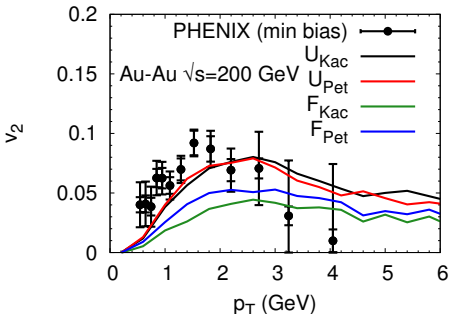
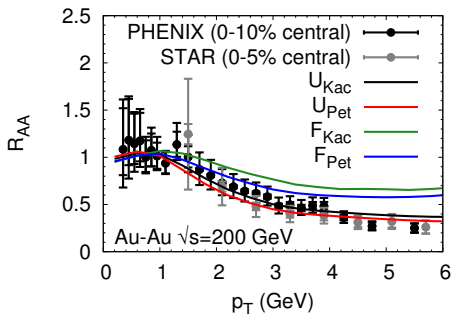


# Spectra and elliptic flow for $b$ -quarks



# Non-photonic electrons at RHIC

- quark **coalescence**+**fragmentation**  $\rightarrow D/B \rightarrow e + X$



- coalescence** crucial for description of data
- increases **both**,  $R_{AA}$  and  $v_2 \Leftrightarrow$  “momentum kick” from light quarks!
- “resonance formation” **towards  $T_c$**   $\Rightarrow$  **coalescence natural**

[L. Ravagli, HvH, R. Rapp, Phys. Rev. C **79**, 064902 (2009)]

# Summary and Outlook

- Heavy quarks in the sQGP
- non-perturbative interactions
  - mechanism for strong coupling: resonance formation at  $T \gtrsim T_c$
  - lattice-QCD potentials parameter free
  - resonances melt at higher temperatures  
 $\Leftrightarrow$  consistency betw.  $R_{AA}$  and  $v_2$ !
- also provides “natural” mechanism for quark coalescence
- resonance-recombination model [L. Ravagli, HvH, R. Rapp, Phys. Rev. C **79**, 064902 (2009)]
- potential approach at finite  $T$ :  $F$ ,  $V$  or combination?
- Outlook
  - include inelastic heavy-quark processes (gluo-radiative processes)
  - other heavy-quark observables like charmonium suppression/regeneration