

## EXAM II Physics 208

Name.....Section Number.....

### USEFUL INFORMATION

For two point particles

$$\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}$$

$$\frac{d\vec{r}}{dt} = \frac{dx}{dt} \vec{i}_x + \frac{dy}{dt} \vec{i}_y = \frac{dr}{dt} \vec{i}_r + r \frac{d\theta}{dt} \vec{i}_\theta$$

$$V(\vec{r}_2) - V(\vec{r}_1) = - \int_{\vec{r}_1}^{\vec{r}_2} \vec{E} \cdot d\vec{r}$$

$$C = \frac{Q}{V} \quad R = \rho \frac{l}{A}$$

$$\oint \vec{E} \cdot d\vec{S} = \frac{Q_{\text{inside}}}{\epsilon_0}$$

$$V = iR \quad \vec{E} = \rho \vec{j}$$

1.

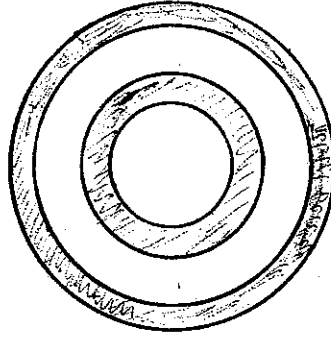
2.

3.

4.

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1. (25 points) A conducting spherical shell has inner radius  $A$  and thickness  $T$ . There is a larger concentric spherical conducting shell with inner radius  $B$  and thickness  $T$ . The inner shell is given a charge  $Q$ .



- a. Find the charge per unit area everywhere.
- b. Find the electric potential difference between a point on the inside surface of the inner shell and a point on the outside surface of the outer shell.
- c. What is the capacitance of this system?

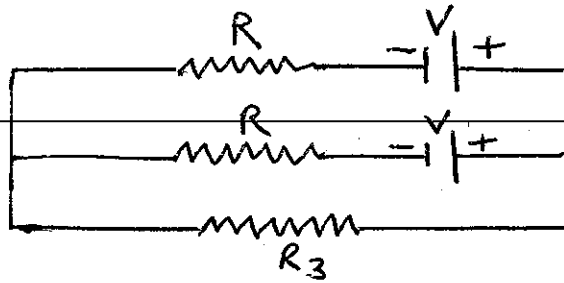
2. (25 points) A very, very long insulating cylinder of radius  $A$  and length  $L$  has a charge  $Q$  uniformly spread throughout its volume. For the two questions that follow consider only points very far from the ends so that the cylinder can be assumed to be infinitely long.



- a. Find the electric field as a function of  $r$ , the distance from the axis of the cylinder, for all values of  $r$ .

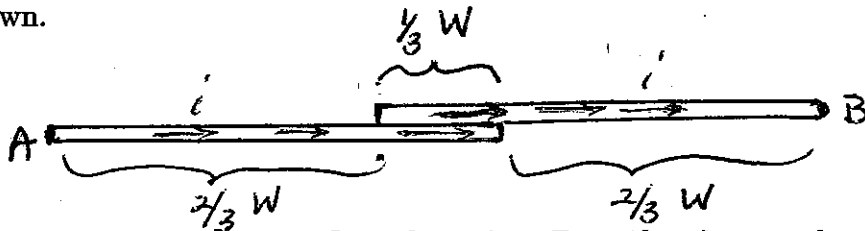
- b. Find the difference in the electric potential between a point on the axis, at the center of the cylinder, and a point  $b$  a distance  $5A$  from the axis of the cylinder.

3. (25 points) In the circuit below,  $R$ , and  $R_3$  and  $V$  are known. Find the current in the resistor  $R_3$ .



If one of the resistors,  $R$ , is replaced by a capacitor, capacitance  $C$ , find the current in  $R_3$  and the charges on  $C$ .

4. It is necessary to connect two points A and B so that a current will flow. There are two identical wires available that are too short. They have length  $W$ , cross-sectional area  $A$ , and are made of material with resistivity  $\rho$ . They are soldered together as shown.



Assume a known current  $i$  flows from A to B, uniformly spread over the cross-section of the wires, as indicated.

- What is the current density vector at all points in the wires?
- What is the difference in the electrical potential between the points A and B?
- What is the resistance between the points A and B?