

# Charm and beauty production in AA collisions in a Fokker-Planck approach

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# Outline

## 1 Heavy-quark interactions in the sQGP

- Heavy quarks in heavy-ion collisions
- Heavy-quark diffusion: The Langevin Equation

## 2 Non-perturbative HQ interactions

- Resonance model for HQ-q Scattering
- T-matrix approach with lQCD potentials

## 3 Comparison with data

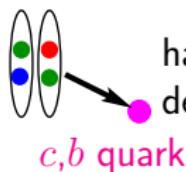
- Nonphotonic electrons at RHIC
- D mesons at LHC
- Predictions for D mesons at FAIR
- Dileptons from correlated D  $\bar{D}$  decays

## 4 Summary and Outlook

# Motivation

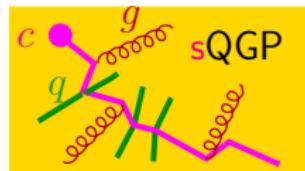
- Fast equilibration of hot and dense matter in heavy-ion collisions:  
collective flow (nearly ideal hydrodynamics)  $\Rightarrow$  sQGP
- Heavy quarks as calibrated probe of QGP properties
  - produced in early hard collisions: well-defined initial conditions
  - not fully equilibrated due to large masses
  - **heavy-quark diffusion**  $\Rightarrow$  probes for QGP-transport properties
- Langevin simulation within UrQMD-hydro hybrid model
- sensitivity to medium evolution
  - $\Rightarrow$  [P. B. Gossiaux, S. Vogel, HvH, J. Aichelin, R. Rapp, M. He, M. Bluhm, arXiv: 1102.1114 [hep-ph]]
- drag and diffusion coefficients
  - $T$ -matrix approach with static lattice-QCD **heavy-quark potentials**
  - **resonance formation** close to  $T_c$
  - mechanism for **non-perturbative strong interactions**

# Heavy Quarks in Heavy-Ion collisions

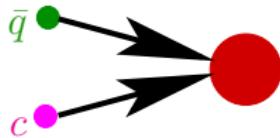


hard production of HQs  
described by PDF's + pQCD (PYTHIA)

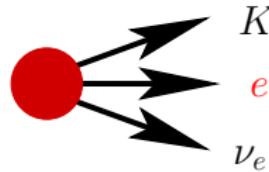
c,b quark



HQ rescattering in QGP: Langevin simulation  
drag and diffusion coefficients from  
microscopic model for HQ interactions in the sQGP



Hadronization to  $D, B$  mesons via  
quark coalescence + fragmentation



$K \rightarrow e^\pm \nu_e$   
semileptonic decay  $\Rightarrow$   
“non-photonic” electron observables  
 $R_{AA}^{e^+e^-}(p_T), v_2^{e^+e^-}(p_T)$

# Relativistic Langevin process

- Langevin process: friction force + Gaussian random force
- in the (local) rest frame of the heat bath

$$d\vec{x} = \frac{\vec{p}}{E_p} dt,$$

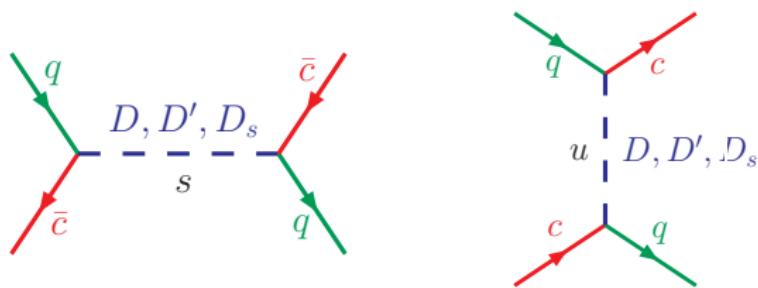
$$d\vec{p} = -A \vec{p} dt + \sqrt{2dt} [\sqrt{B_0} P_{\perp} + \sqrt{B_1} P_{\parallel}] \vec{w}$$

- $\vec{w}$ : normal-distributed random variable
- $A$ : friction (drag) coefficient
- $B_{0,1}$ : diffusion coefficients
- Einstein dissipation-fluctuation relation  $B_1 = E_p T A$ .
- flow via Lorentz boosts between “heat-bath frame” and “lab frame”
- $A$  and  $B_0$  from microscopic models for  $qQ, gQ$  scattering
- background medium: UrQMD → hydro → UrQMD

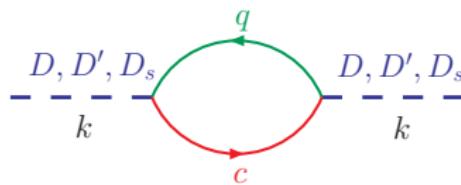
[R. Rapp, HvH, R. C. Hwa and X. N. Wang (eds.), Quark-Gluon Plasma Vol. IV, World Scientific (2010), arXiv: 0903.1096 [hep-ph]; M. He, HvH, P. B. Gossiaux, R. J. Fries, R. Rapp, Phys. Rev. E 88, 032138 (2013)]

# Non-perturbative interactions: Resonance Scattering

- General idea: Survival of  $D$ - and  $B$ -meson like **resonances** above  $T_c$
- model based on chiral symmetry (light quarks) HQ-effective theory
- **elastic heavy-light-(anti-)quark scattering**



- $D$ - and  $B$ -meson like resonances in sQGP

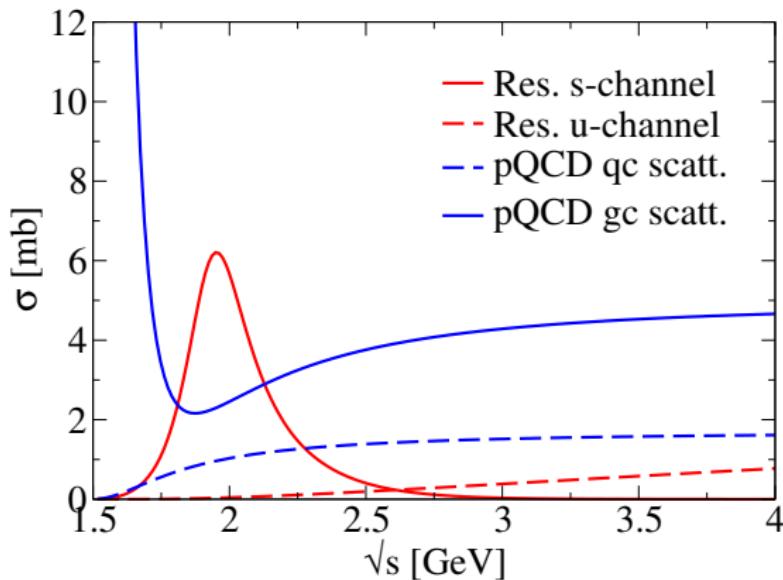


- parameters

- $m_D = 2 \text{ GeV}, \Gamma_D = 0.4 \dots 0.75 \text{ GeV}$
- $m_B = 5 \text{ GeV}, \Gamma_B = 0.4 \dots 0.75 \text{ GeV}$

[HvH, R. Rapp, Phys. Rev. C 71, 034907 (2005); HvH, V. Greco, R. Rapp, Phys. Rev. C 73, 034913 (2006) ]

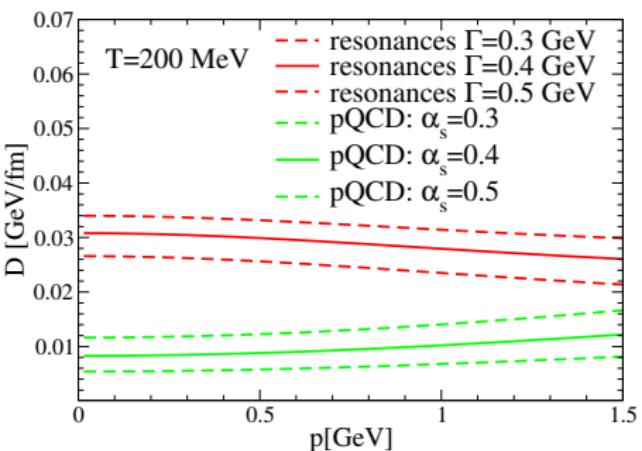
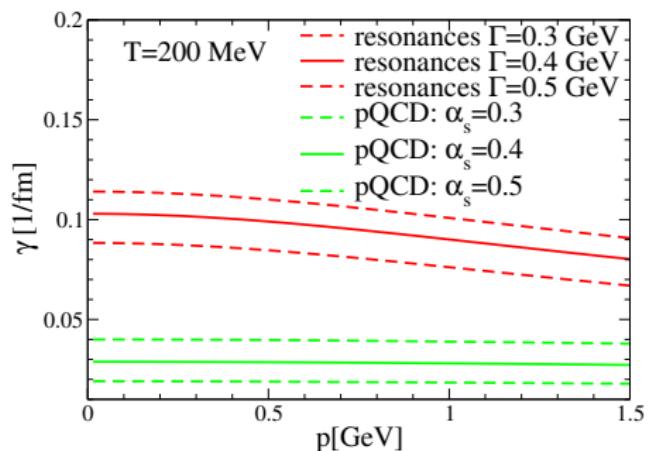
# Cross sections



- total pQCD and resonance cross sections: comparable in size
- BUT pQCD forward peaked  $\leftrightarrow$  resonance isotropic
- resonance scattering more effective for friction and diffusion

# Transport coefficients: pQCD vs. resonance scattering

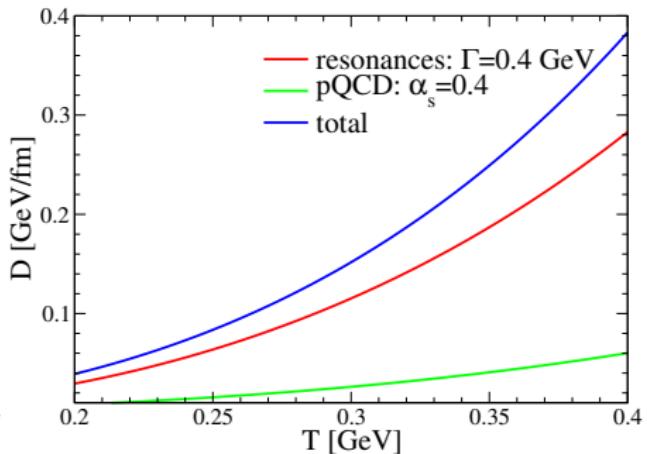
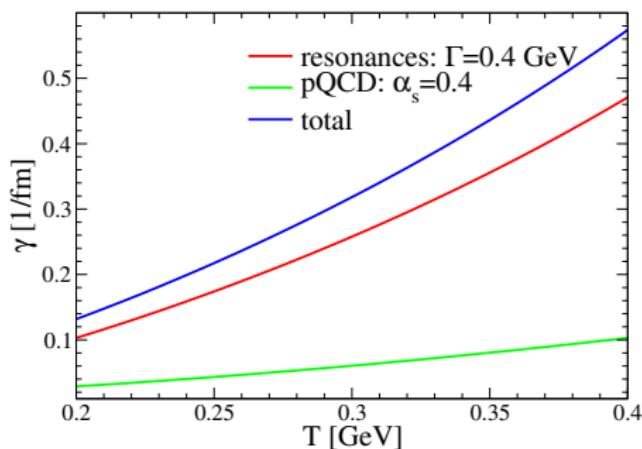
- three-momentum dependence



- resonance contributions factor  $\sim 2 \dots 3$  higher than pQCD!

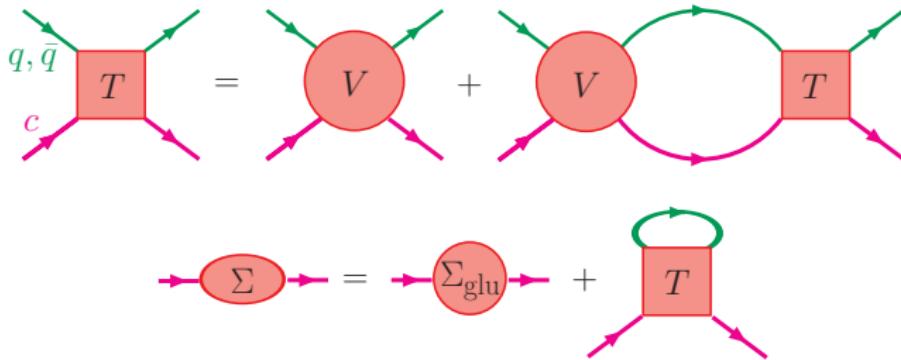
# Transport coefficients: pQCD vs. resonance scattering

- Temperature dependence



# T-matrix

- Brueckner many-body approach for elastic  $Qq, Q\bar{q}$  scattering

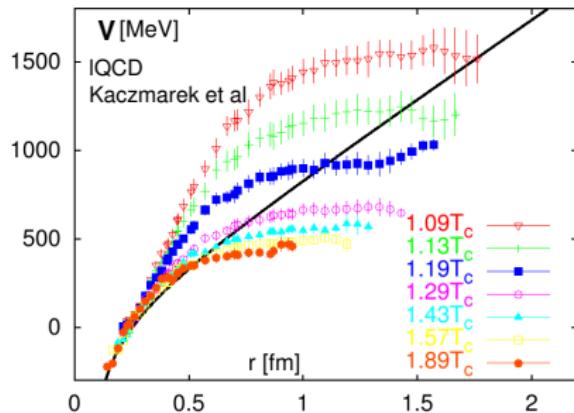


- $V$ : static  $q\bar{q}$  potential from lattice QCD ( $F$  and  $U$ )
- reduction scheme: 4D Bethe-Salpeter  $\rightarrow$  3D Lipmann-Schwinger
- $S$ - and  $P$  waves
- Relation to invariant **matrix elements**

$$\sum_q |\mathcal{M}(s)|^2 \propto \sum_a d_a \left( |T_{a,l=0}(s)|^2 + 3|T_{a,l=1}(s)|^2 \cos \theta_{\text{cm}} \right)$$

[HvH, M. Mannarelli, V. Greco, R. Rapp, Phys. Rev. Lett. **100**, 192301 (2008)]

# Static heavy-quark potentials from lattice QCD



- color-singlet free energy from lattice  $\rightarrow$  internal energy

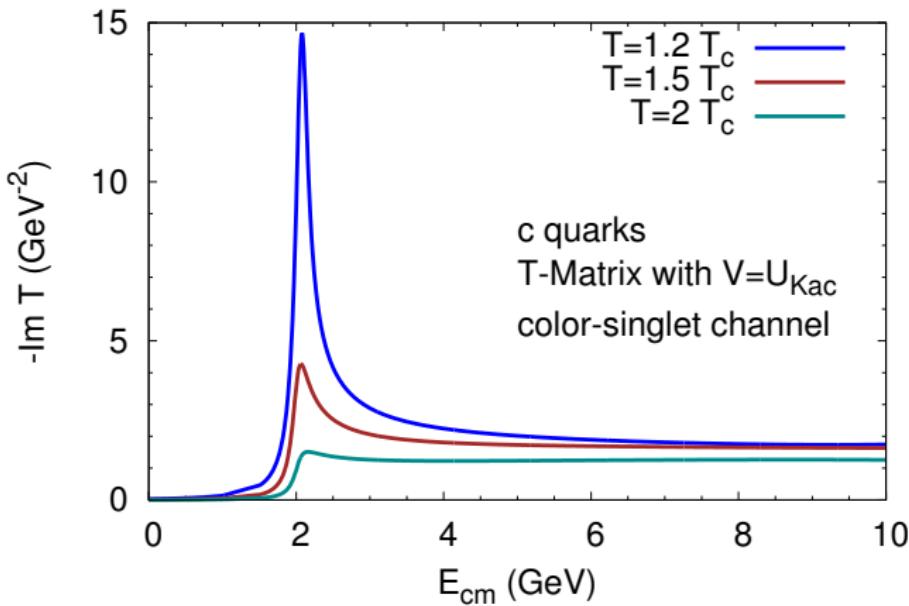
$$U_1(r, T) = F_1(r, T) - T \frac{\partial F_1(r, T)}{\partial T},$$

$$V_1(r, T) = U_1(r, T) - U_1(r \rightarrow \infty, T)$$

- Casimir scaling of Coulomb part for other color channels; confining part color blind [[F. Riek, R. Rapp, Phys. Rev. C 82, 035201 \(2010\)](#)].

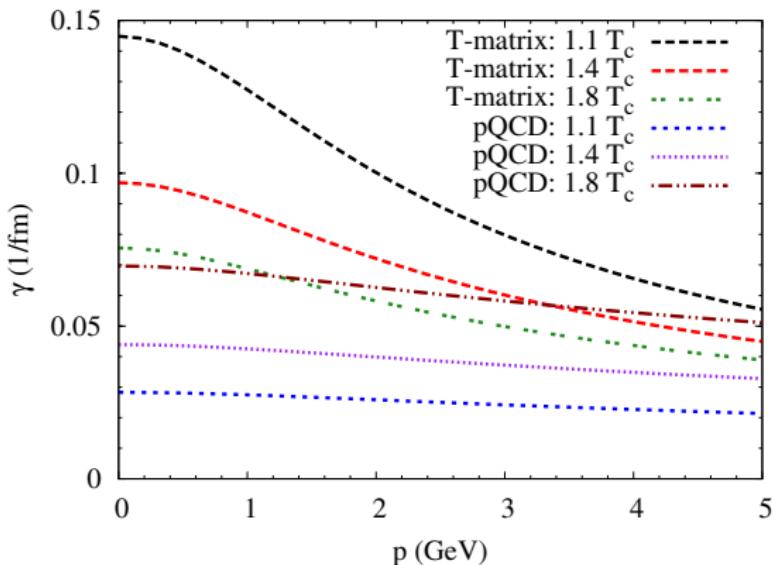
$$V_{\bar{3}} = \frac{1}{2} V_1, \quad V_6 = -\frac{1}{4} V_1, \quad V_8 = -\frac{1}{8} V_1$$

# T-matrix results



- **resonance formation** at lower temperatures  $T \simeq T_c$
- melting of resonances at higher  $T$
- model-independent assessment of elastic  $Qq, Q\bar{q}$  scattering!

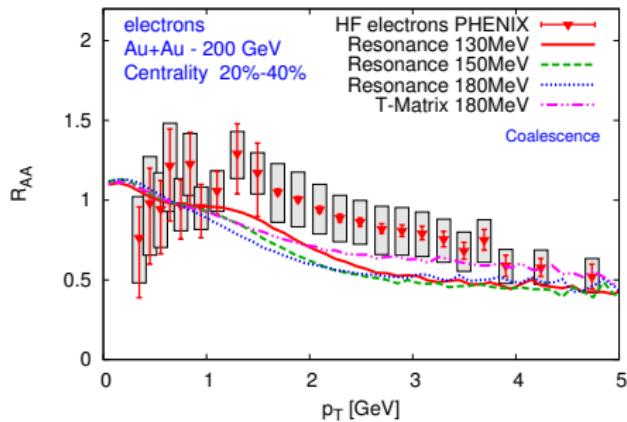
# Transport coefficients



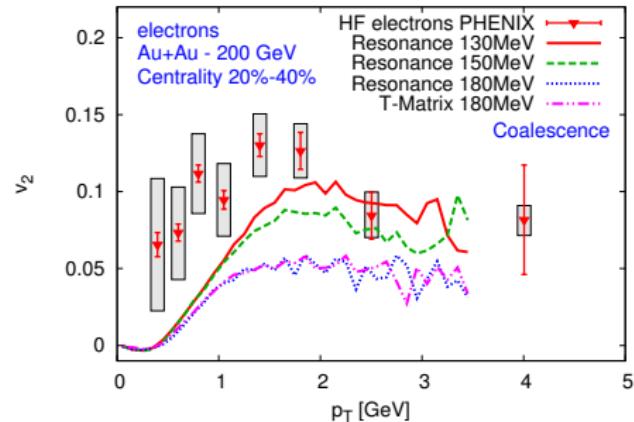
- $T$ -matrix resonance-scattering coefficients: **decrease** with  $T$
- from **non-pert.** interactions reach  $A_{\text{non-pert}} \simeq 1/(7 \text{ fm}/c) \simeq 4 A_{\text{pQCD}}$
- results for **free-energy potential,  $F$**  considerably smaller

# Nonphotonic electrons at RHIC

- form D and B mesons via **quark-antiquark coalescence**
- use PYTHIA for semi-leptonic decays
- comparison to single-electron data from PHENIX  
(200 AGeV Au-Au collisions)

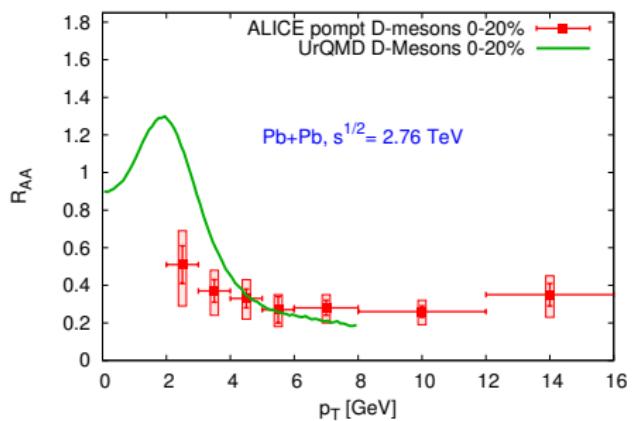


[T. Lang, HvH, J. Steinheimer, M. Bleicher, arXiv: 1211.6912 [hep-ph]]

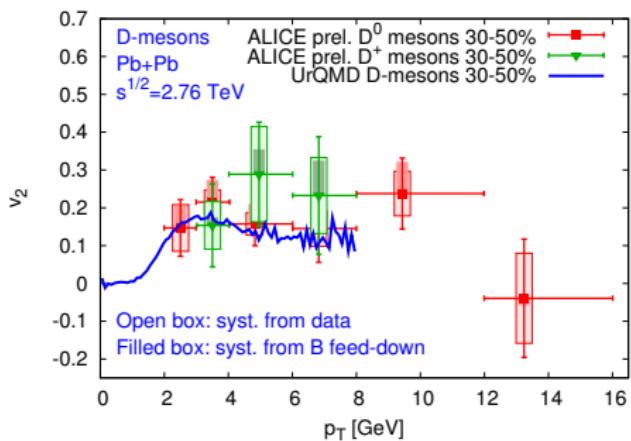


# D mesons at LHC

- form D via **quark-antiquark coalescence**
- comparison to D-meson data from ALICE (2.76 ATeV Pb-Pb collisions)

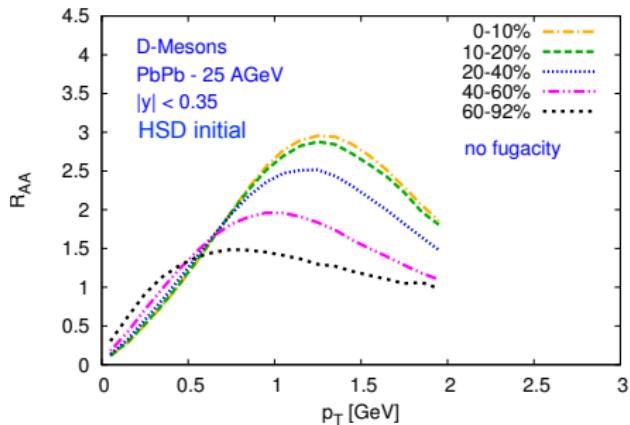


[T. Lang, HvH, J. Steinheimer, M. Bleicher, arXiv: 1211.6912 [hep-ph]]

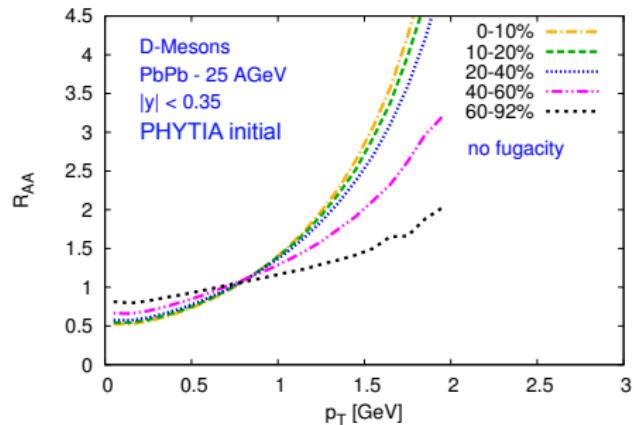


# D mesons at FAIR

- form D via **quark-antiquark coalescence**
- large sensitivity to initial HQ distributions  
(use estimates from HSD and PYTHIA)

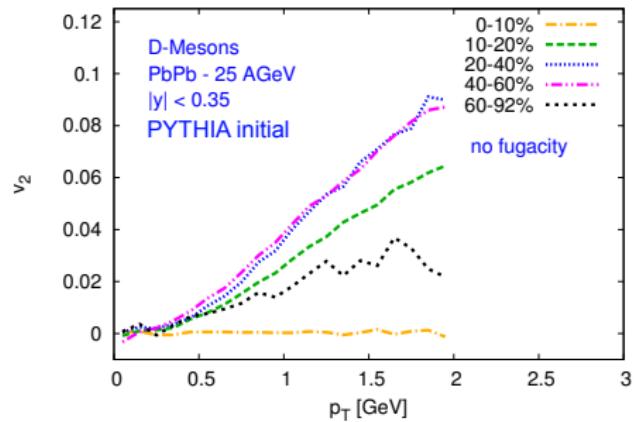
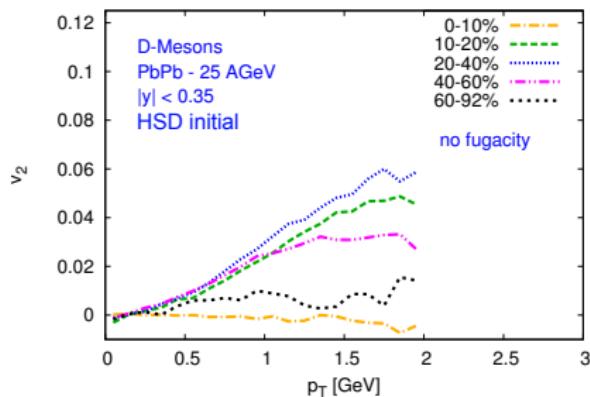


[T. Lang, HvH, J. Steinheimer, M. Bleicher, arXiv: 1305.1797 [hep-ph]]



# D mesons at FAIR

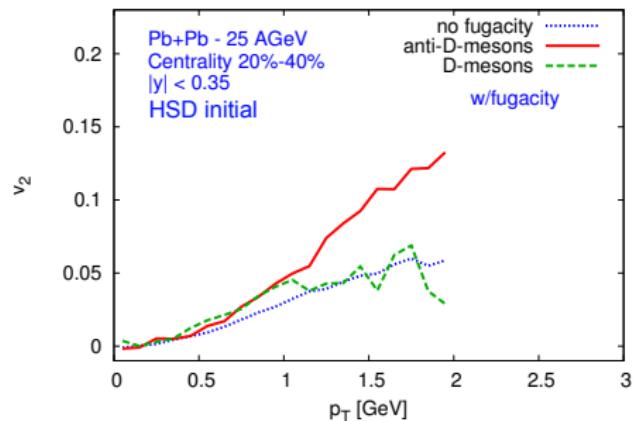
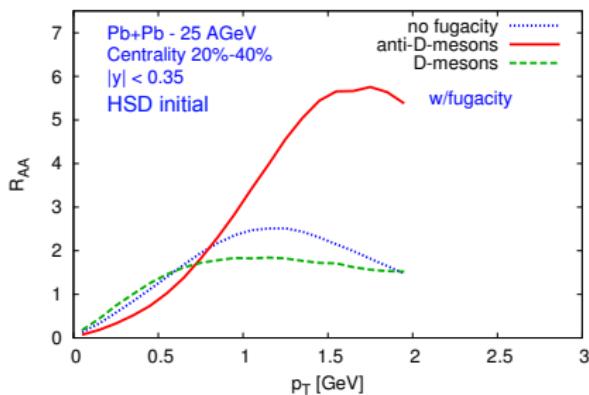
- form D via **quark-antiquark coalescence**
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# D mesons at FAIR

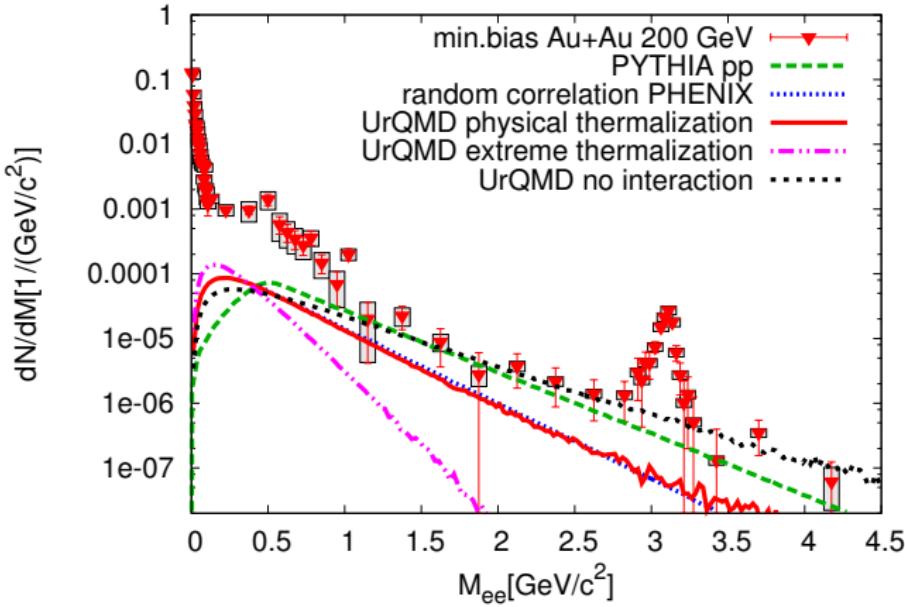
- form D via **quark-antiquark coalescence**
- large sensitivity to initial HQ distributions  
(use estimates from HSD and PYTHIA)
- large  $\mu_B$  in resonance model:  $\bar{c}$  more dragged than  $c$



[T. Lang, HvH, J. Steinheimer, M. Bleicher, arXiv: 1305.1797 [hep-ph]]

# Dileptons from correlated D $\bar{D}$ decays

- for  $m_\phi \lesssim M_{\ell^+ \ell^-} \lesssim m_{J/\psi}$ :  
dilepton emission from thermal QGP and from correlated D  $\bar{D}$  decays
- medium modifications of D and  $\bar{D}$  destroy correlations



[T. Lang, HvH, J. Steinheimer, M. Bleicher, arXiv: 1305.7377 [hep-ph]]

# Summary and Outlook

- Heavy quarks in the sQGP
- non-perturbative interactions
  - mechanism for strong coupling: resonance formation at  $T \gtrsim T_c$
  - lattice-QCD potentials parameter free
  - also provides “natural” mechanism for quark coalescence

[R. Ravagli, HvH, R. Rapp, Phys. Rev. C 79, 064902 (2009)]

- Comparison to data and predictions for FAIR
  - $R_{AA}$  and  $v_2$  of non-photonic electrons at RHIC
  - $R_{AA}$  and  $v_2$  for D mesons at LHC
  - $R_{AA}$  and  $v_2$  for D mesons at FAIR (pp baseline mandatory!)
  - impact of medium modifications on correlated  $D\bar{D}$  decays to dileptons
- Outlook
  - implementation of hadronic cross sections for D/B-meson diffusion
  - include inelastic heavy-quark processes (gluo-radiative processes)
  - implement resonance-recombination model for hadronization
  - charmonium/bottomonium suppression/regeneration