### Electromagnetic Probes in Heavy-Ion Collisions II Phenomenology from SIS to LHC energies

#### Hendrik van Hees

Goethe University Frankfurt and FIAS

November 27, 2015





#### Outline

#### Heavy-ion collisions on one slide

2 QCD and ultra-hot and -dense matter

Electromagnetic probes in heavy-ion collisions

- Isimulations for electromagnetic probes in HICs
  - Dileptons at SIS energies (HADES)
  - Dileptons at SPS and RHIC
  - Direct photons at RHIC and LHC: "the flow puzzle"
- 5 Outlook: Signatures of the QCD-phase structure?

#### B References

#### Heavy-Ion collisions in a Nutshell

- theory of strong interactions: Quantum Chromo Dynamics, QCD
- at high densities/temperatures: hadrons dissolve into a QGP
- create QGP in Heavy-Ion Collisions at RHIC (and LHC)
- GSI SIS: pp, dp, pA, AA collisions at low energies ( $E_{kin} = 1.25-3.5 \text{ GeV}$ ) Dielectrons from HADES
- CERN SPS: AA collisions with  $E_{kin} = 158 \text{ GeV}$  per nucleon on a fixed target (center-mass energy:  $\sqrt{s_{NN}} = 17.3 \text{ GeV}$ ) dileptons (particularly  $\mu^+\mu^-$  in In-In collisions from NA60)
- BNL RHIC: Au Au collisions with center-mass energy of  $\sqrt{s_{NN}} = 200 \text{ GeV}$ ; "beam-energy scan"  $\sqrt{s_{NN}} = 7.7-39 \text{ GeV}$ dileptons from STAR and PHENIX; direct photons from PHENIX
- CERN LHC: Pb-Pb collisions at  $\sqrt{s} = 2.76$  TeV per nucleon direct photons from ALICE



#### Phenomenology and Chiral symmetry

- in vacuum: Spontaneous breaking of chiral symmetry
- ⇒ mass splitting of chiral partners



### The QCD-phase diagram

- hot and dense matter: quarks and gluons close together
- highly energetic collisions ⇒ "deconfinement"
- quarks and gluons relevant degrees of freedom  $\Rightarrow$  quark-gluon plasma
- still strongly interacting  $\Rightarrow$  fast thermalization!



## The QCD-phase diagram

- at high temperature/density: restoration of chiral symmetry
- lattice QCD:  $T_c^{\chi} \simeq T_c^{\text{deconf}}$





- mechanism of chiral restoration?
- two main theoretical ideas
  - "dropping masses":  $m_{\rm had} \propto \langle \overline{\psi} \psi \rangle$
  - "melting resonances": broadening of spectra through medium effects

#### Electromagnetic probes in heavy-ion collisions



 $\Psi^{|}$ 

Drell-Yan

< 0.1 fm

mass [GeV/c<sup>2</sup>]

#### Electromagnetic probes from thermal source

- photon and dilepton thermal emission rates given by same electromagnetic-current-correlation function  $(J_{\mu} = \sum_{f} Q_{f} \overline{\psi_{f}} \gamma_{\mu} \psi_{f})$
- McLerran-Toimela formula [МТ85, GK91]

$$\Pi_{\mu\nu}^{<}(q) = \int d^{4}x \exp(iq \cdot x) \langle J_{\mu}(0)J_{\nu}(x) \rangle_{T} = -2f_{B}(q \cdot u) \operatorname{Im} \Pi_{\mu\nu}^{(\operatorname{ret})}(q)$$

$$q_{0} \frac{dN_{\gamma}}{d^{4}xd^{3}\vec{q}} = -\frac{\alpha_{em}}{2\pi^{2}} g^{\mu\nu} \operatorname{Im} \Pi_{\mu\nu}^{(\operatorname{ret})}(q, u) \Big|_{q_{0} = |\vec{q}|} f_{B}(q \cdot u)$$

$$\frac{dN_{e^{+}e^{-}}}{d^{4}xd^{4}k} = -g^{\mu\nu} \frac{\alpha^{2}}{3q^{2}\pi^{3}} \operatorname{Im} \Pi_{\mu\nu}^{(\operatorname{ret})}(q, u) \Big|_{q^{2} = M_{e^{+}e^{-}}^{2}} f_{B}(q \cdot u)$$

- manifestly Lorentz covariant (dependent on four-velocity of fluid cell, *u*)
- $q \cdot u = E_{cm}$ : Doppler blue shift of  $q_T$  spectra!
- to lowest order in  $\alpha$ :  $4\pi \alpha \Pi_{\mu\nu} \simeq \Sigma_{\mu\nu}^{(\gamma)}$
- vector-meson dominance model:

$$\Sigma^{\gamma}_{\mu\nu} = \mathbf{O}_{\mathbf{O}_{\mathbf{O}_{\mathbf{O}}}} \mathbf{O}_{\mathbf{O}_{\mathbf{O}}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}_{\mathbf{O}}} \mathbf{O}_{\mathbf{O}} \mathbf{O}} \mathbf{O}_{\mathbf{O}} \mathbf{O}} \mathbf{O}_{\mathbf{O}}$$

C

•  $\ell^+\ell^-$ -*M* spectra  $\Rightarrow$  in-med. spectral functions of vector mesons  $(\rho, \omega, \phi)$ !

#### Radiation from thermal QGP: $q\bar{q}$ annihilation

• General: McLerran-Toimela formula

$$\frac{\mathrm{d}N_{l+l-}^{(\mathrm{MT})}}{\mathrm{d}^4 x \mathrm{d}^4 q} = -\frac{\alpha^2}{3\pi^3} \frac{L(M^2)}{M^2} g_{\mu\nu} \mathrm{Im} \sum_i \Pi_{\mathrm{em},i}^{\mu\nu} (M,\vec{q}) f_{\mathrm{B}}(q \cdot u)$$

- *i* enumerates partonic/hadronic sources of em. currents
- in-medium em. current-current correlation function

$$\Pi_{\mathrm{em},i}^{\mu\nu} = \mathrm{i} \int \mathrm{d}^4 x \, \exp(\mathrm{i} q \, x) \Theta(x^0) \left\langle \left[ j_{\mathrm{em},i}^{\mu}(x), j_{\mathrm{em},i}^{\nu}(0) \right] \right\rangle$$

- in QGP phase:  $q\bar{q}$  annihilation
- hard-thermal-loop improved electromagnetic current-current correlator

#### Radiation from thermal sources: $\rho$ decays

• model assumption: vector-meson dominance

$$\Sigma_{\mu\nu}^{\gamma} = \mathbf{\mathcal{N}}_{\mu\nu} \mathbf{\mathcal{D}}_{\mu\nu}^{G_{\rho}}$$

$$\frac{\mathrm{d}N_{\rho\to l+l^{-}}}{\mathrm{d}^{4}x\,\mathrm{d}^{4}q} = \frac{M}{q^{0}}\Gamma_{\rho\to l+l^{-}}(M)\frac{\mathrm{d}N_{\rho}}{\mathrm{d}^{3}\vec{x}\,\mathrm{d}^{4}q}$$

$$= -\frac{\alpha^{2}}{3\pi^{3}}\frac{L(M^{2})}{M^{2}}\frac{m_{\rho}^{4}}{g_{\rho}^{2}}g_{\mu\nu}\,\mathrm{Im}\,D_{\rho}^{\mu\nu}(M,\vec{q})f_{\mathrm{B}}\left(\frac{q\cdot u - 2\mu_{\pi}(t)}{T(t)}\right)$$

- special case of McLerran-Toimela (MT) formula
- $M^2 = q^2$ : invariant mass, M, of dilepton pair
- $L(M^2) = (1 + 2m_l^2/M^2)\sqrt{1 4m_l^2/M^2}$ : dilepton phase-space factor
- $D_{\rho}^{\mu\nu}(M, \vec{q})$ : (four-transverse part of) in-medium  $\rho$  propagator at given T(t),  $\mu_{\text{meson/baryon}}(t)$
- $-\text{Im}D_{\rho}$  in-medium  $\rho$ -meson spectral function!
- analogous for  $\omega$  and  $\phi$

## Hadronic many-body theory

- hadronic many-body theory (HMBT) for vector mesons [LK95, CS92, CS93, RCW97, UBRW98, UBW02, UBRW00, Her92, HFN93, GR99, RW99, RW00]
- $\pi\pi$  interactions and baryonic excitations
- effective hadronic models, implementing symmetries
- parameters fixed from phenomenology (photon absorption at nucleons and nuclei,  $\pi N \rightarrow \rho N$ )
- evaluated at finite temperature and density
- self-energies  $\Rightarrow$  mass shift and broadening of particle in the medium



Baryon (resonances) important, even at low **net** baryon density n<sub>B</sub>-n<sub>B̄</sub>
 reason: n<sub>B</sub>+n<sub>B̄</sub> relevant (CP inv. of strong interactions)

#### Meson contributions



#### In-medium spectral functions and baryon effects



- baryon effects important
  - large contribution to broadening of the peak
  - responsible for most of the strength at small M

#### Radiation from thermal sources: multi- $\pi$ processes

- use vector/axial-vector correlators from  $\tau$ -decay data
- Dey-Eletsky-Ioffe mixing:  $\hat{\varepsilon} = 1/2\varepsilon(T, \mu_{\pi})/\varepsilon(T_c, 0)$

$$\Pi_{V} = (1 - \hat{\varepsilon}) z_{\pi}^{4} \Pi_{V,4\pi}^{\text{vac}} + \frac{\hat{\varepsilon}}{2} z_{\pi}^{3} \Pi_{A,3\pi}^{\text{vac}} + \frac{\hat{\varepsilon}}{2} (z_{\pi}^{4} + z_{\pi}^{5}) \Pi_{A,5\pi}^{\text{vac}}$$

• avoid double counting: leave out two-pion piece and  $a_1 \rightarrow \rho + \pi$  (already contained in  $\rho$  spectral function)



Data: [B+98]

#### Bulk evolution with transport and coarse graining

- established transport models for bulk evolution
  - e.g., UrQMD, GiBUU, BAMPS, (p)HSD,...
  - solve Boltzmann equation for hadrons and/or partons
- dilemma: need medium-modified dilepton/photon emission rates
- usually available only in equilibrium QFT calculations
- ways out:
  - use (ideal) hydrodynamics ⇒ local thermal equilibrium
     ⇒ use equilibrium rates
  - use transport-hydro hybrid model: treat early stage with transport, then coarse grain ⇒ switch to hydro
    - $\Rightarrow$  switch back to transport (Cooper-Frye "particlization")
- here: UrQMD transport for entire bulk evolution
  - $\Rightarrow$  use coarse graining in space-time cells  $\Rightarrow$  extract T,  $\mu_B$ ,  $\mu_{\pi}$ , ...
  - $\Rightarrow$  use equilibrium rates locally

# Simulations for em. probes in heavy-ion collisions

- problem with medium modifications of spectral functions/interactions
- only available in equilibrium many-body QFT models
- use "in-medium cross sections" naively: double counting?!?
- way out: map transport to local-equilibrium fluid
- use ensemble of UrQMD runs with an equation of state
- fit temperature, chemical potentials, flow-velocity field from anisotropic energy-momentum tensor [FMRS13]

$$T^{\mu\nu} = (\epsilon + P_{\perp})u^{\mu}u^{\nu} - P_{\perp}g^{\mu\nu} - (P_{\parallel} - P_{\perp})V^{\mu}V^{\nu}$$

- thermal rates from partonic/hadronic QFT become applicable
- extrapolated lattice QGP and Rapp-Wambach hadronic many-body theory
- caveat: consistency between EoS, matter content of QFT model/UrQMD!

•  $T_c = 170 \text{ MeV}; T > T_c \Rightarrow \text{lattice EoS}; T < T_c \Rightarrow \text{HRG EoS}$ 



• pressure anisotropy (In-In collisions (NA60) at SIS)



- energy/baryon density  $\Rightarrow$  *T*,  $\mu_{\rm B}$  (for In+In @ SPS; NA60)
- central "fluid" cell!



• energy ( $\epsilon$ ) and baryon ( $\rho$ ) density profiles (for In+In@SPS; NA60)



# **Dielectrons (SIS/HADES)**

- coarse-graining method works at low energies!
- UrQMD-medium evolution + RW-QFT rates [EHWB15b]



- dielectron spectra from Ar + KCl(1.76 AGeV)  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> (SIS/HADES)
- $m_t$  spectra [EHWB15b]
- $M_{\rm ee} < 0.13 \,{
  m GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV)  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> (SIS/HADES)
- $m_t$  spectra [EHWB15b]
- $0.13 \, \text{GeV} M_{ee} < 0.3 \, \text{GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV)  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> (SIS/HADES)
- $m_t$  spectra [EHWB15b]
- 0.3 GeV $M_{\rm ee}$  < 0.45 GeV



- dielectron spectra from Ar + KCl(1.76 AGeV)  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> (SIS/HADES)
- $m_t$  spectra [EHWB15b]
- $0.45 \, {\rm GeV} M_{\rm ee} < 0.65 \, {\rm GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV)  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> (SIS/HADES)
- $m_t$  spectra [EHWB15b]
- $M_{\rm ee} > 0.65 \,{
  m GeV}$



- dielectron spectra from Ar + KCl(1.76 AGeV)  $\rightarrow$  e<sup>+</sup>e<sup>-</sup> (SIS/HADES)
- $m_t$  spectra [EHWB15b]
- rapidity spectrum ( $M_{\rm ee} < 0.13 \, {\rm GeV}$ )



#### CGUrQMD: Au+Au (1.23 AGeV) (SIS/HADES)



- caveat: pp/np acceptance filter with single-e cut,  $p_t < 100 \text{ MeV}$
- correct filter urgently needed!
- excellent agreement with preliminary HADES data (data points not shown here on request of the HADES collaboration)

#### What to learn about the "bulk dynamics"?

- hadronic observables like *p<sub>T</sub>* spectra: "snapshot" of the stage after kinetic freezeout
- particle abundancies: chemical freezeout
- em. probes: emitted during the whole medium evolution life time of the medium ⇒ "four-volume of the fireball"
- use CGUrQMD to study system-size dependence
- study AA collisions for different A
- hard to quantify "life time" of the "thermal" medium in transport
- here: use time, for which the central cell has  $T \ge 50$  MeV

#### Four Volume





• how to explain "scaling behavior"?

### Lifetime of the central cell

• consider central collisions from C+C to Au+Au at  $E_{kin} = 1.76 AGeV$ 



- $\Delta t \propto A^{1/3}$
- $A \propto V^{(3)}$  of nuclei  $\Rightarrow A^{1/3} \propto d_{\text{nucl}}$
- fireball lifetime  $\propto$  time of nuclei to traverse each other

#### Lifetime of the central cell





- yield<sub>had</sub>  $\propto A \propto V_{\rm fo}^{(3)}$
- yield<sub>non-thermal ee</sub>  $\propto A \propto V_{fo}^{(3)}$  $\Rightarrow$  hadronic decays after kinetic freeze-out

#### Scaling behavior of thermal-dilepton yield



• thermal-dilepton yield roughly  $\propto V_{\rm therm}^{(4)} \propto A^{4/3} \propto A t_{\rm therm} \propto N_{\pi^0}^{4/3}$ 

# Dimuons (SPS/NA60)
• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

- min-bias data (dN<sub>ch</sub>/dy = 120)
  note the importance of baryon effects!



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

- min-bias data  $(dN_{ch}/dy = 120)$ higher IMR: provides averaged true temperature (no blueshifts in the invariant-mass spectra!)



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]



10<sup>-10</sup>

0.2

0.4

0.6

0.8

1.2

Invariant Mass M [GeV]

14

• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60)

• min-bias data 
$$(dN_{ch}/dy = 120)$$



• dimuon spectra from  $\text{In} + \text{In}(158 \,\text{AGeV}) \rightarrow \mu^+ \mu^-$  (NA60)

[EHWB15a]



0.2

0.4

0.8

1.2

Invariant Mass M [GeV]

1 4

0.6

• dimuon spectra from  $\text{In} + \text{In}(158 \,\text{AGeV}) \rightarrow \mu^+ \mu^-$  (NA60)

[EHWB15a]



Invariant Mass M [GeV]

- dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]
- min-bias data ( $dN_{ch}/dy = 120$ )



- dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]
- min-bias data ( $dN_{ch}/dy = 120$ )



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]

• min-bias data ( $dN_{ch}/dy = 120$ )



• dimuon spectra from In + In(158 AGeV)  $\rightarrow \mu^+\mu^-$  (NA60) [EHWB15a]

• min-bias data ( $dN_{ch}/dy = 120$ )



## **Dielectrons at RHIC**

#### Dileptons@RHIC: PHENIX (2007)



model: Rapp, HvH, data [A+10]

- here: thermal-fireball evolution instead of CGUrQMD (work in progress)
- huge enhancement in the LMR explained by new PHENIX results from Sep/2015

#### Dileptons@RHIC: PHENIX (2015)



model: Rapp, HvH, data [A+15]

• here: thermal-fireball evolution instead of CGUrQMD (work in progress)



model: Rapp, HvH, data [A+15]

• here: thermal-fireball evolution instead of CGUrQMD (work in progress)

#### Dileptons@RHIC: STAR (QM 2012)



[Rap13], data: [Zha11]

compatible with medium modifications in model calculation

## Direct photons (RHIC/LHC)

#### Direct Photons at RHIC

- same model [TRG04] for rates as for dileptons
- fireball parametrization with elliptic flow  $v_2$
- photons inherit  $v_2$  from hadronic sources



[HGR11, RHH14, HHR15]

#### Effective slopes vs. temperatures

- effective slopes of photon *p*<sub>T</sub> spectra are NOT temperatures!
- emission from a flowing medium  $\Rightarrow$  Doppler effect



[RHH14]

#### Direct Photons at the LHC

#### same model, fireball adapted to hadron data from ALICE [HHR15]



- large direct-photon  $v_2$
- early buildup of  $v_2$ ; here developed already at end of QGP phase
- emission mostly around  $T_c$  (dual rates!)  $\Rightarrow$
- $\Rightarrow$  source has already developed radial flow and  $v_2$
- Iarge effective slopes include blueshift from radial flow!
- still additional (hadronic?) sources (bremsstrahlung?) missing?!?

# Signatures of the QCD-phase structure?

#### Possible signatures of QCD-phase structure?

- measurement of thermal-dilepton spectra/yields a la NA60
- scaling behavior at low energies studied with one HRG EoS
- beam-energy scan like at RHIC  $\Rightarrow$  deviations from naive scaling behavior?
- possible variations in fireball lifetime due to different phase transitions
- cross over at higher RHIC and LHC energies [RH14]
- deviations in regions of larger  $\mu_{\rm B}$ ?
- possible signature of 1<sup>st</sup>-order line?
- possible signature of critical point through "anomalies in fireball lifetime" due to critical slowing-down???
- NB: ℓ<sup>+</sup>ℓ<sup>−</sup> also "thermometer" from invariant-mass slopes in IMR (needs a good handle on correlated DD decays a la NA60!)

#### Dilepton systematics in the beam-energy scan

- beam-energy scan at RHIC and lower energies at future FAIR and NICA accelerators
- invariant-mass slope in IMR  $\Rightarrow$  true temperature!
- no blue shift from radial flow as in  $p_T/m_T$  spectra



#### Dilepton systematics in the beam-energy scan

- beam-energy scan at RHIC and lower energies at future FAIR and NICA accelerators
- dilepton yield as fireball-lifetime clock



- em. probes,  $\ell^+\ell^-$  and  $\gamma$ : neglible final-state interactions
- probe in-medium electromagnetic current-current correlator over entire history of fireball evolution
- provide insight into fundamental properties of QCD matter
- needs models for electromagnetic radiation from QGP and hadron gas
- medium effects on vector mesons in hot and dense matter
- hint at chiral-symmetry restoration
  - $\Rightarrow$  melting resonances rather than dropping mass
- insight into fireball dynamics (temperature, lifetime)
- possible hints of QCD-phase structure (equation of state)?
- for more details, see website of the HQM Lecture Week spring 2014 http://fias.uni-frankfurt.de/~hees/hqm-lectweek14/index.html

### Bibliography I

[A <sup>+</sup> 10]	A. Adare, et al., Detailed measurement of the $e^+e^-$ pair continuum in p+p and Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV and implications for direct photon production, Phys. Rev. C <b>81</b> (2010) 034911. http://dx.doi.org/10.1103/PhysRevC.81.034911
[A <sup>+</sup> 15]	A. Adare, et al., Dielectron production in Au+Au collisions at $\sqrt{s_{NN}}$ =200 GeV (2015). http://arXiv.org/abs/1509.04667
[B <sup>+</sup> 98]	R. Barate, et al., Measurement of the spectral functions of axial-vector hadronic $\tau$ decays and determination of $\alpha_s(M_{\tau}^2)$ , Eur. Phys. J. C 4 (1998) 409. http: //publish.edpsciences.org/abstract/EPJC/V4/P409
[CS92]	G. Chanfray, P. Schuck, The rho meson mass spectrum in dense matter, Nucl. Phys. A <b>545</b> (1992) 271c. http://dx.doi.org/10.1016/0375-9474(93)90325-R

#### Bibliography II

[CS93] G. Chanfray, P. Schuck, The rho meson in dense matter and its influence on dilepton production rates, Nucl. Phys. A 555 (1993) 329. http://dx.doi.org/10.1016/0375-9474(93)90325-R

- [EHWB15a] S. Endres, H. van Hees, J. Weil, M. Bleicher, Coarse-graining approach for dilepton production at energies available at the CERN Super Proton Synchrotron, Phys. Rev. C 91 (2015) 054911. http://dx.doi.org/10.1103/PhysRevC.91.054911
- [EHWB15b] S. Endres, H. van Hees, J. Weil, M. Bleicher, Dilepton production and reaction dynamics in heavy-ion collisions at SIS energies from coarse-grained transport simulations, Phys. Rev. C 92 (2015) 014911. http://dx.doi.org/10.1103/PhysRevC.92.014911
- [FMRS13] W. Florkowski, M. Martinez, R. Ryblewski, M. Strickland, Anisotropic hydrodynamics, Nucl. Phys. A 904-905 (2013) 803c. http://dx.doi.org/10.1016/j.nuclphysa.2013.02.138

#### **Bibliography III**

- [GK91] C. Gale, J. I. Kapusta, Vector Dominance Model at Finite Temperature, Nucl. Phys. B **357** (1991) 65. http://dx.doi.org/10.1016/0550-3213(91)90459-B
- [GR99] C. Gale, R. Rapp, Rho Properties in a hot Gas: Dynamics of Meson-Resonances, Phys. Rev. C 60 (1999) 024903. http://publish.aps.org/abstract/PRC/v60/e024903
- [Her92] M. Herrmann, Eigenschaften des ρ-Mesons in dichter Kernmaterie, Dissertation, Technische Hochschule Darmstadt, Darmstadt (1992). http://www-lib.kek.jp/cgi-bin/img\_index?200038480
- [HFN93] M. Herrmann, B. L. Friman, W. Nörenberg, Properties of rho mesons in nuclear matter, Nucl. Phys. A 560 (1993) 411. http://dx.doi.org/10.1016/0375-9474(93)90105-7
- [HGR11] H. van Hees, C. Gale, R. Rapp, Thermal Photons and Collective Flow at the Relativistic Heavy-Ion Collider, Phys. Rev. C 84 (2011) 054906. http://dx.doi.org/10.1103/PhysRevC.84.054906

#### Bibliography IV

 [HHR15] H. van Hees, M. He, R. Rapp, Pseudo-Critical Enhancement of Thermal Photons in Relativistic Heavy-Ion Collisions, Nucl. Phys. A 933 (2015) 256. http://dx.doi.org/10.1016/j.nuclphysa.2014.09.009

- [LK95] G.-Q. Li, C. M. Ko, Can dileptons reveal the in-medium properties of vector mesons?, Nucl. Phys. A 582 (1995) 731. http://dx.doi.org/10.1016/0375-9474(94)00500-M
- [MT85] L. D. McLerran, T. Toimela, Photon and dilepton emission from the quark-gluon plasma: some general considerations, Phys. Rev. D 31 (1985) 545. http://link.aps.org/abstract/PRD/V31/P545
- [Rap13] R. Rapp, Dilepton Spectroscopy of QCD Matter at Collider Energies, Adv. High Energy Phys. 2013 (2013) 148253. http://dx.doi.org/10.1155/2013/148253
## Bibliography V

- [RCW97] R. Rapp, G. Chanfray, J. Wambach, Rho meson propagation and dilepton enhancement in hot hadronic matter, Nucl. Phys. A617 (1997) 472. http://arxiv.org/abs/hep-ph/9702210
- [RH14] R. Rapp, H. van Hees, Thermal Dileptons as Fireball Thermometer and Chronometer (2014). http://arxiv.org/abs/1411.4612
- [RHH14] R. Rapp, H. van Hees, M. He, Properties of Thermal Photons at RHIC and LHC, Nucl. Phys. A 931 (2014) 696. http://dx.doi.org/10.1016/j.nuclphysa.2014.08.008
- [RW99] R. Rapp, J. Wambach, Low mass dileptons at the CERN-SPS: Evidence for chiral restoration?, Eur. Phys. J. A 6 (1999) 415. http://dx.doi.org/10.1007/s100500050364
- [RW00] R. Rapp, J. Wambach, Chiral symmetry restoration and dileptons in relativistic heavy-ion collisions, Adv. Nucl. Phys. 25 (2000) 1. http://arxiv.org/abs/hep-ph/9909229

## Bibliography VI

[TRG04] S. Turbide, R. Rapp, C. Gale, Hadronic production of thermal photons, Phys. Rev. C 69 (2004) 014903. http://dx.doi.org/10.1103/PhysRevC.69.014903

- [UBRW98] M. Urban, M. Buballa, R. Rapp, J. Wambach, Momentum dependence of the pion cloud for ρ mesons in nuclear matter, Nucl. Phys. A 641 (1998) 433. http://dx.doi.org/10.1016/S0375-9474(98)00476-X
- [UBRW00] M. Urban, M. Buballa, R. Rapp, J. Wambach, Modifications of the *ρ* meson from the virtual pion cloud in hot and dense matter, Nucl. Phys. A 673 (2000) 357. http://dx.doi.org/10.1016/S0375-9474(00)00125-1

 $[UBW02] M. Urban, M. Buballa, J. Wambach, Temperature dependence of <math>\rho$ and  $a_1$  meson masses and mixing of vector and axial-vector correlators, Phys. Rev. Lett. **88** (2002) 042002. http://dx.doi.org/10.1103/PhysRevLett.88.042002

## [Zha11] J. Zhao, Dielectron continuum production from $\sqrt{s_{NN}} = 200 \text{ GeV}$ p+p and Au+Au collisions at STAR, J. Phys. G **38** (2011) 124134. http://dx.doi.org/10.1088/0954-3899/38/12/124134