

Dileptons in heavy-ion collisions with transport models

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Outline

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 - Em. current correlation function and electromagnetic probes
 - Sources of dilepton emission in heavy-ion collisions
 - Sources of thermal photons in heavy-ion collisions

- 2 Dileptons in pp, pn, pA, AA in pure transport (GiBUU with J. Weil)
 - GiBUU
 - Dalitz decays of hadron resonances
 - Baryon-resonance model at SIS energies
 - Dielectrons (SIS/NA60)

- 3 Dileptons in AA in coarse-grained transport (with S. Endres)
 - Models for bulk-medium evolution
 - Dielectrons (SIS/NA60)
 - Dimuons (SPS/NA60)

- 4 Conclusions and Outlook

Em. current correlator $\ell^+ \ell^-$ and γ rates

Electromagnetic probes in heavy-ion collisions

- γ, ℓ^\pm : no strong interactions
- reflect whole “history” of collision:
 - from pre-equilibrium phase
 - from thermalized medium
QGP and hot hadron gas
 - from VM decays after thermal freezeout

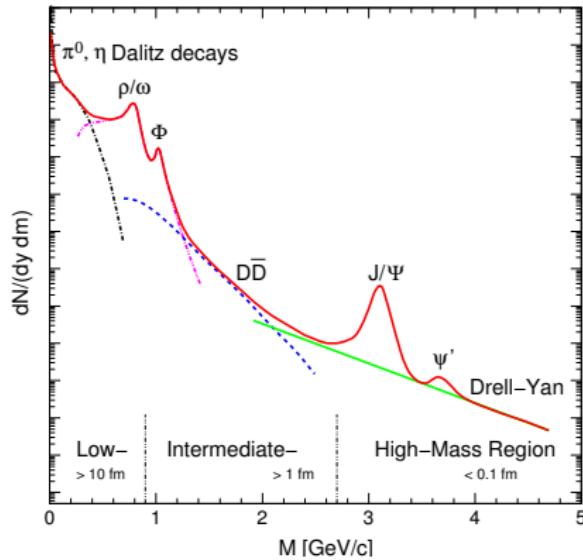
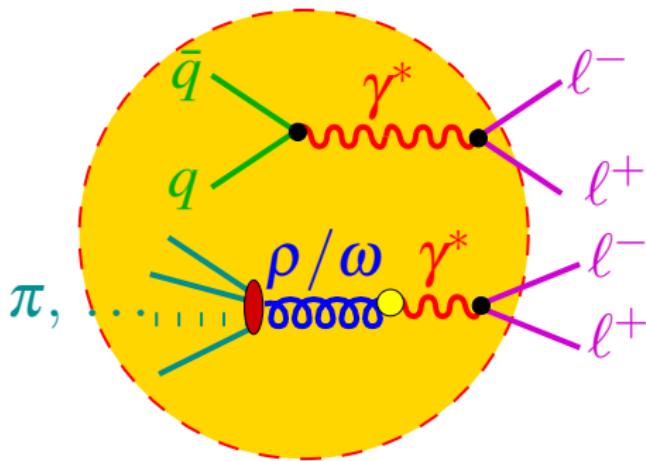


Fig. by A. Drees

Em. current correlation function and electromagnetic Probes

- photon and dilepton thermal emission rates given by same electromagnetic-current-correlation function ($J_\mu = \sum_f Q_f \bar{\psi}_f \gamma_\mu \psi_f$)

[MT85, Wel90, GK91]

$$\Pi_{\mu\nu}^{<}(q) = \int d^4x \exp(iq \cdot x) \langle J_\mu(0) J_\nu(x) \rangle_T = -2 f_B(q \cdot u) \text{Im} \Pi_{\mu\nu}^{(\text{ret})}(q)$$
$$q_0 \frac{dN_\gamma}{d^4x d^3\vec{q}} = -\frac{\alpha}{2\pi^2} g^{\mu\nu} \text{Im} \Pi_{\mu\nu}^{(\text{ret})}(q) \Big|_{q_0=|\vec{q}|} f_B(q \cdot u)$$
$$\frac{dN_{e^+e^-}}{d^4x d^4q} = -g^{\mu\nu} \frac{\alpha^2}{3q^2\pi^3} \text{Im} \Pi_{\mu\nu}^{(\text{ret})}(q) \Big|_{q^2=M_{e^+e^-}^2} f_B(q \cdot u)$$

- u : four-velocity of the fluid cell; $p \cdot u = p_0^{\text{hb}}$ energy in “heat-bath frame”
- to lowest order in α : $e^2 \Pi_{\mu\nu} \simeq \Sigma_{\mu\nu}^{(\gamma)}$
- vector-meson dominance model:

$$\Sigma_{\mu\nu}^{\gamma} = G_\rho$$

Sources of dilepton emission in heavy-ion collisions

- ➊ initial hard processes: Drell Yan
- ➋ “core” \Leftrightarrow emission from thermal source

$$\frac{1}{q_T} \frac{dN^{(\text{thermal})}}{dM dq_T} = \int d^4x \int dy \int M d\varphi \frac{dN^{(\text{thermal})}}{d^4x d^4q}$$

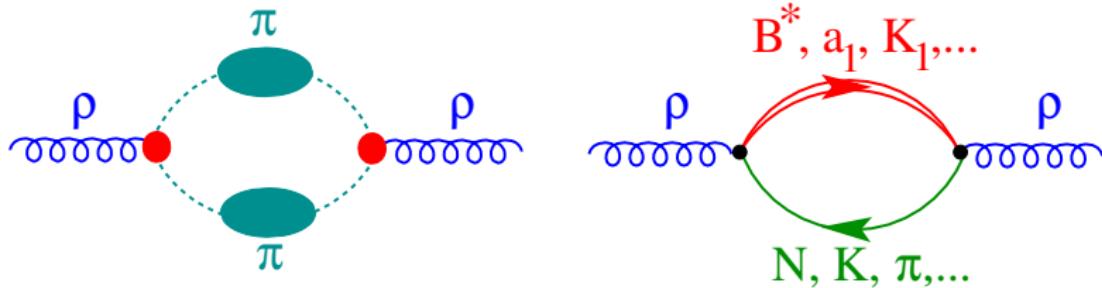
- ➌ “corona” \Leftrightarrow emission from “primordial” mesons (jet-quenching)
- ➍ after thermal freeze-out \Leftrightarrow emission from “freeze-out” mesons

[CF74]

$$N^{(\text{fo})} = \int \frac{d^3q}{q_0} \int q_\mu d\sigma^\mu f_B(u_\mu q^\mu / T) \frac{\Gamma_{\text{meson} \rightarrow \ell^+ \ell^-}}{\Gamma_{\text{meson}}}$$

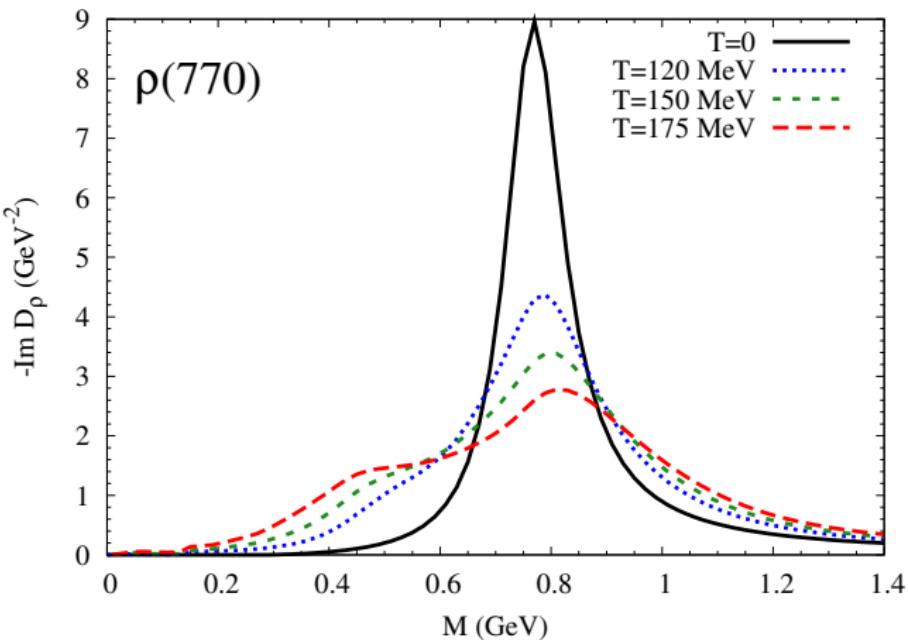
Hadronic many-body theory

- HMBT for vector mesons [Ko et al, Chanfray et al, Herrmann et al, Rapp et al, ...]
- $\pi\pi$ interactions and baryonic excitations



- +corresponding vertex corrections \Leftrightarrow gauge invariance
- **Baryon (resonances)** important, even at RHIC with low **net** baryon density
 $n_B - n_{\bar{B}}$
- reason: $n_B + n_{\bar{B}}$ relevant (CP inv. of strong interactions)

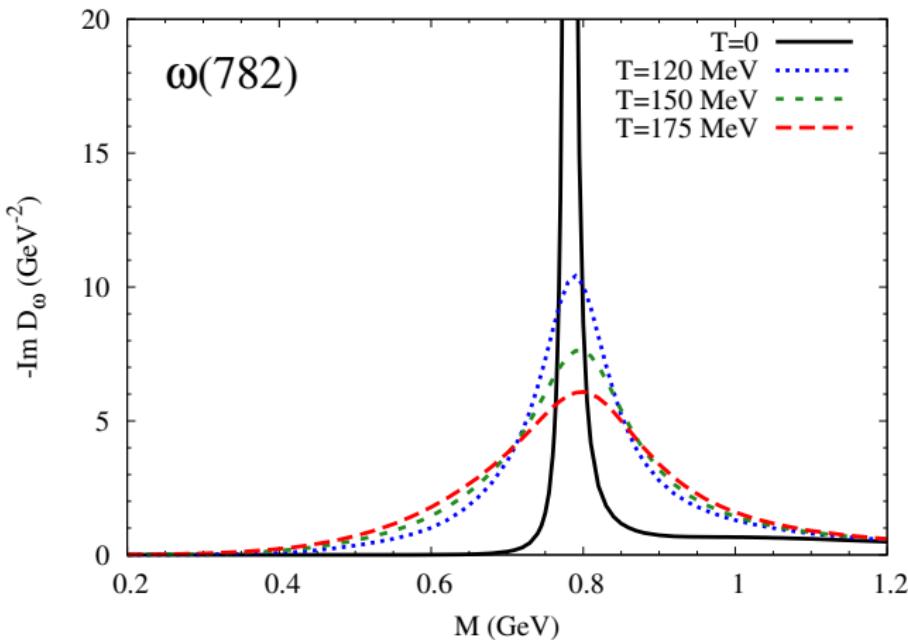
In-medium spectral functions and baryon effects



[R. Rapp, J. Wambach 99]

- baryon effects important
 - large contribution to broadening of the peak
 - responsible for most of the strength at small M

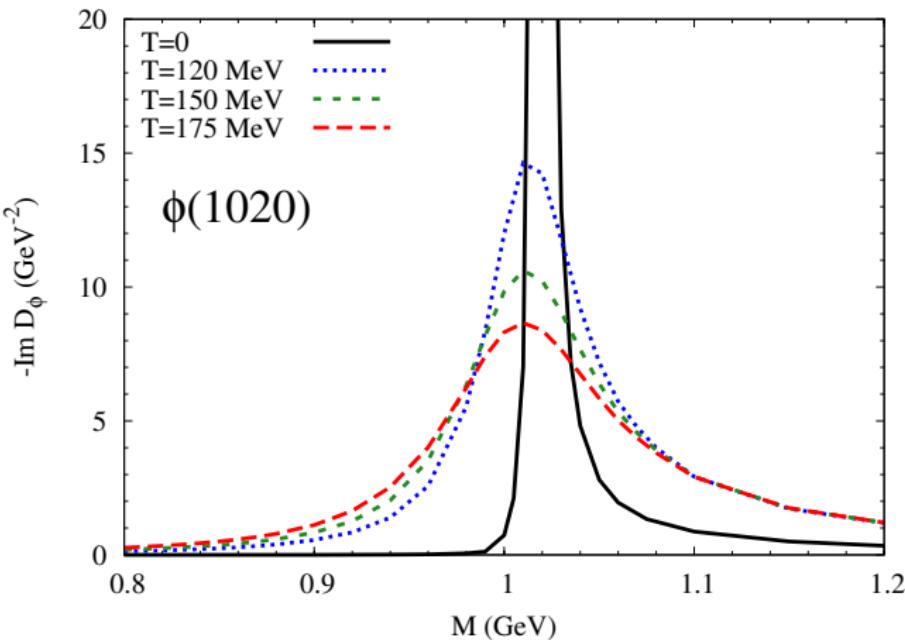
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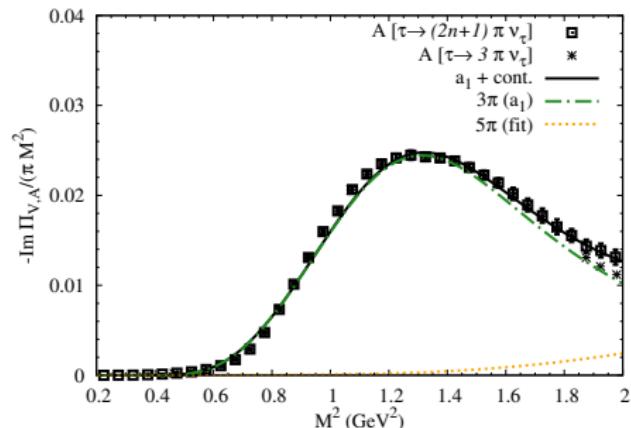
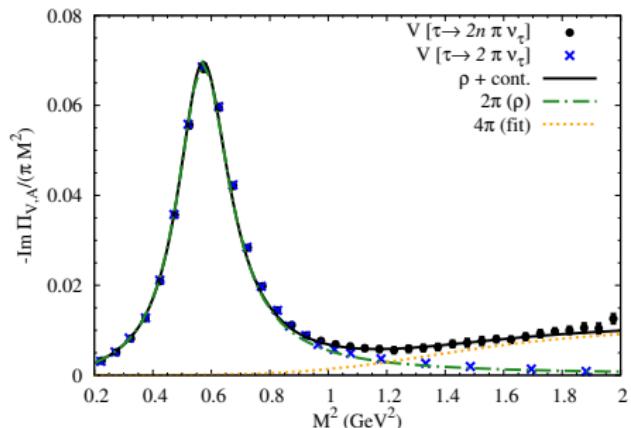


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Intermediate masses: hadronic “ 4π contributions”

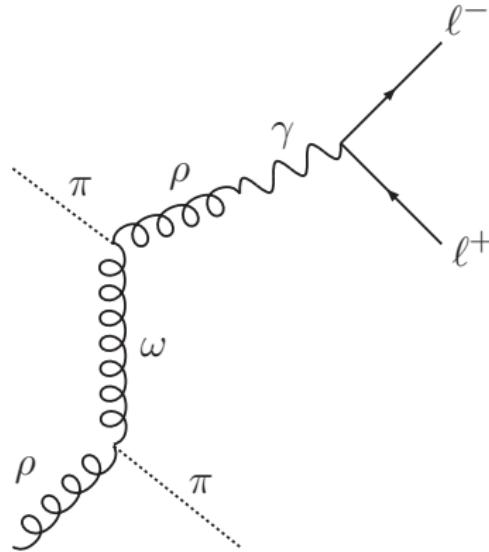
- e.m. current-current correlator $\Leftrightarrow \tau \rightarrow 2n\pi$



- “ 4π contributions”: $\pi + \omega, a_1 \rightarrow \mu^+ + \mu^-$
- leading-order virial expansion for “four-pion piece”
- additional strength through “chiral mixing”

Radiation from thermal sources: Meson t-channel exchange

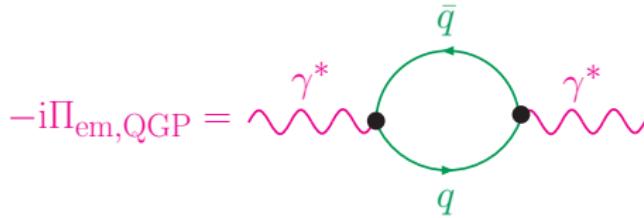
- motivation: q_T spectra too soft compared to NA60 data
- **thermal contributions** not included in models so far



- also for π, a_1

Dileptons from thermal QGP

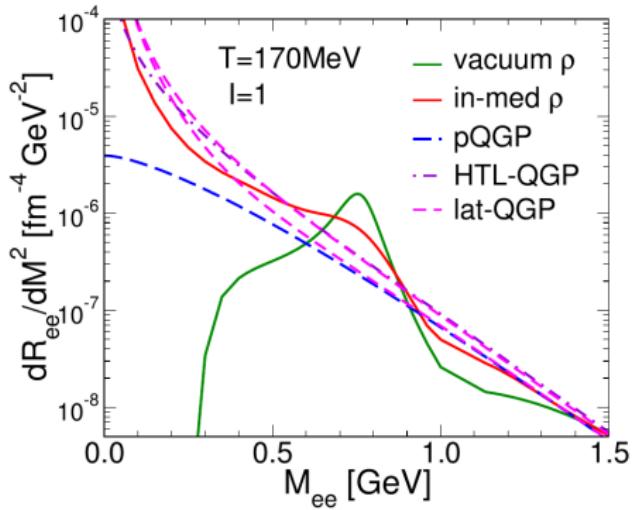
- in **QGP** phase: $q\bar{q}$ annihilation
- HTL improved electromagnetic current correlator



- or electromagnetic current correlator from the **lattice** [H.-T. Ding, A. Francis et al (Bielefeld) 2011]
(extrapolated to finite q)
- “quark-hadron duality” around T_c

Dilepton rates: Hadron gas \leftrightarrow QGP

- in-medium hadron gas matches with QGP
- similar results also for γ rates
- “quark-hadron duality”?

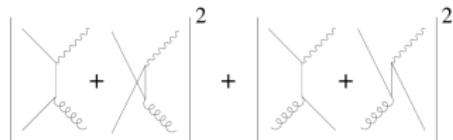


[R. Rapp, arXiv: 1304.2309 [hep-ph]]

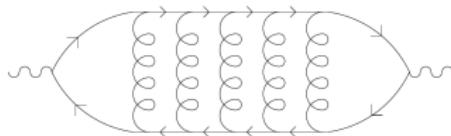
Sources of thermal photons in heavy-ion collisions

- **QGP:** rates from [Arnold, Moore, Yaffe, JHEP **12**, 009 (2001)]

- $q\bar{q} \rightarrow \gamma g, qg \rightarrow \gamma q$

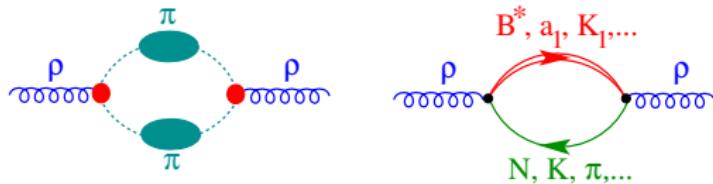


- resummation of soft-gluon bremsstrahlung contributions
- Landau-Pomeranchuk-Migdal effect



- **hadronic matter** from [Turbide, Rapp, Gale, PRC **69**, 014903 (2004); Rapp, Wambach EPJ A **6**, 415 (1999)]

- pion-cloud dressing + vector meson-baryon/meson interactions

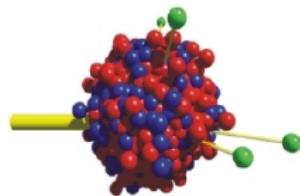


- $\pi\rho a_1, \omega$ -t-channel exchange

Dileptons in pp, pn, pA, AA

pure transport: GiBUU (with Janus Weil)

The GiBUU Model



GiBUU

The Giessen Boltzmann-Uehling-Uhlenbeck Project

- Boltzmann-Uehling-Uhlenbeck (BUU) framework for hadronic transport
- reaction types: pA , πA , γA , eA , vA , AA
- open-source modular Fortran 95/2003 code
- version control via Subversion
- publicly available releases: <https://gibuu.hepforge.org>
- Review on hadronic transport (GiBUU): [BGG⁺12]
- all calculations for dileptons: J. Weil

The Boltzmann-Uehling-Uhlenbeck Equation

- time evolution of phase-space distribution functions

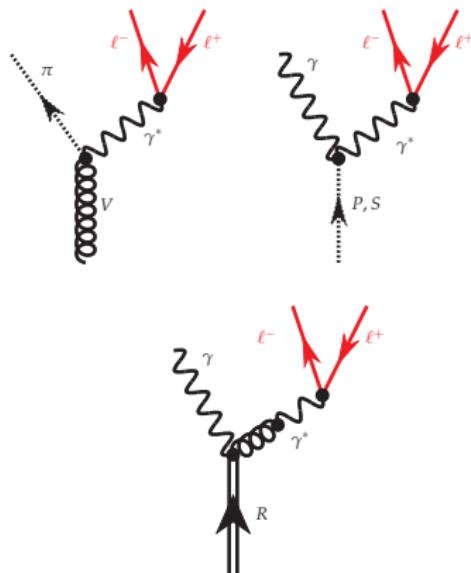
$$[\partial_t + (\vec{\nabla}_p H_i) \cdot \vec{\nabla}_x - (\vec{\nabla}_x H_i) \cdot \vec{\nabla}_p] f_i(t, \vec{x}, \vec{p}) = I_{\text{coll}}[f_1, \dots, f_i, \dots, f_j]$$

- use Monte-Carlo simulation for test particles
- transition probability W in collision term used to define stochastic process (“random numbers” on the computer)
- Hamiltonian H_i
 - selfconsistent hadronic mean fields, Coulomb potential, “off-shell potential”
- collision term I_{coll}
 - two- and three-body decays/collisions
 - multiple coupled-channel problem
 - resonances described with relativistic Breit-Wigner distribution

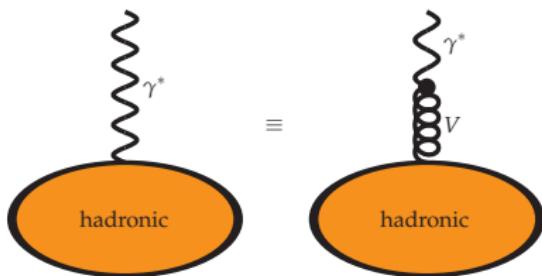
$$\mathcal{A}(x, p) = -\frac{1}{\pi} \frac{\text{Im} \Pi}{(p^2 - M^2 - \text{Re} \Pi)^2 + (\text{Im} \Pi)^2}; \quad \text{Im} \Pi = -\sqrt{p^2} \Gamma$$

- off-shell propagation: test particles with off-shell potential

Dalitz decays



- **Dalitz decay:**
1 particle \rightarrow 3 particles
- $V: \omega \rightarrow \pi + \gamma^* \rightarrow \pi + \ell^+ + \ell^-$
- $P, S: \pi, \eta \rightarrow \gamma + \gamma^* \rightarrow \gamma + \ell^+ + \ell^-$
- R : Baryon resonances
 $\Delta, N^* \rightarrow N + V \rightarrow N + \gamma^* \rightarrow N + \ell^+ + \ell^-$
- vector-meson dominance



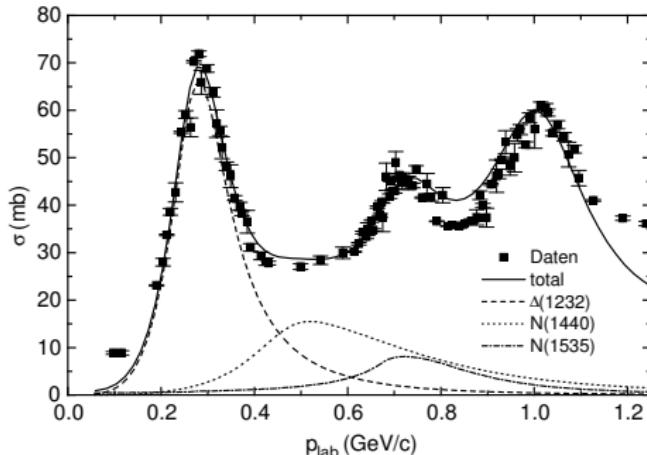
- NB: vector-meson resonances “produced” from stable particles
- Fermi’s golden rule: **equivalent to self-energies** for vector mesons!
- **cutting self-energy diagrams \Rightarrow elementary processes**

Resonance Model

- reactions dominated by resonance scattering: $ab \rightarrow R \rightarrow cd$
- Breit-Wigner cross-section formula

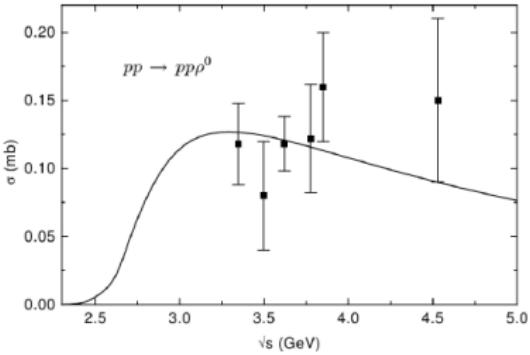
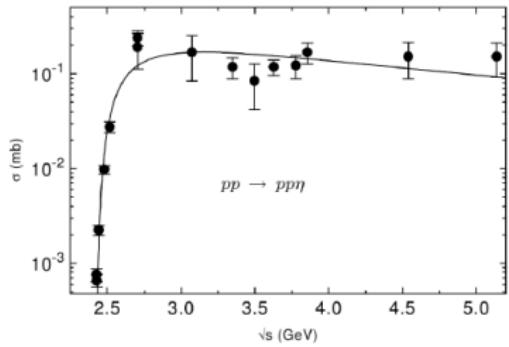
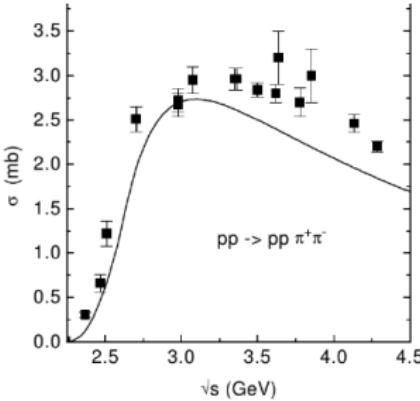
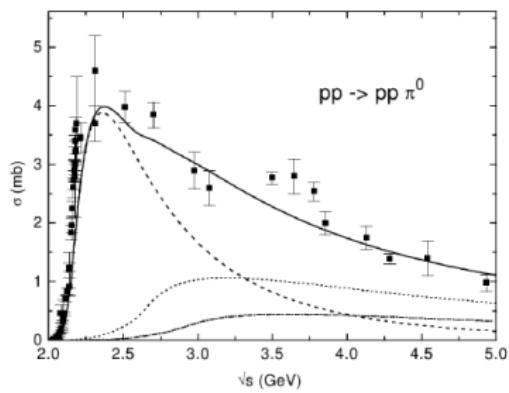
$$\sigma_{ab \rightarrow R \rightarrow cd} = \frac{2s_R + 1}{(2s_a + 1)(2s_b + 1)} \frac{4\pi}{p_{\text{lab}}^2} \frac{s\Gamma_{ab \rightarrow R}\Gamma_{R \rightarrow cd}}{(s - m_R^2)^2 + s\Gamma_{\text{tot}}^2}$$

- applicable for low-energy nuclear reactions $E_{\text{kin}} \lesssim 1.1 \text{ GeV}$
- example: $\sigma_{\pi^- p \rightarrow \pi^- p}$ [Teis (PhD thesis 1996), data: Baldini et al, Landolt-Börnstein **12** (1987)]



GiBUU: Resonance Model

- further cross sections



GiBUU: Extension to HADES energies

- [WHM12, WM13]

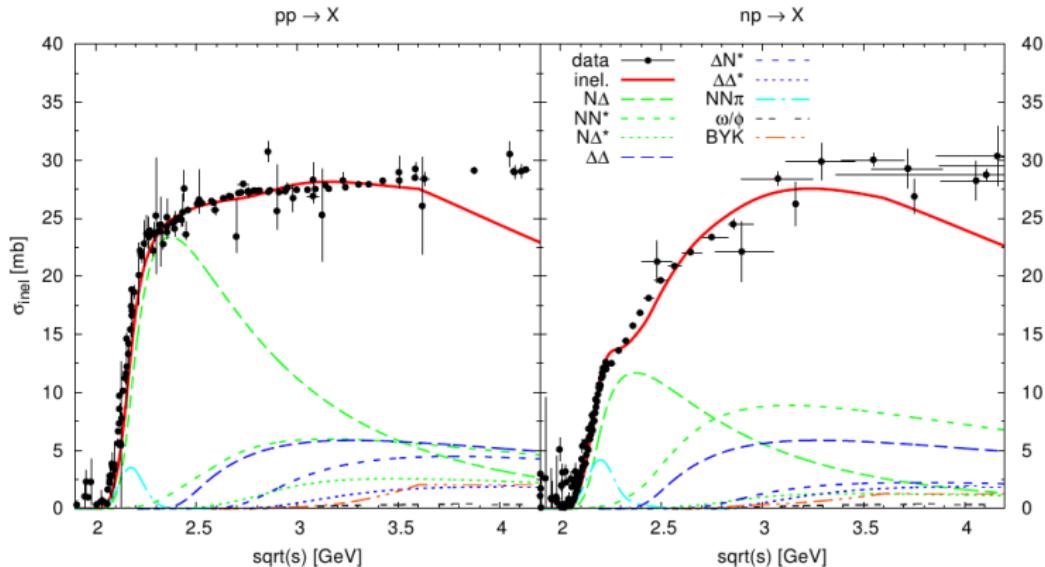
- keep same resonances (parameters from Manley analysis)

	rating	M_0	Γ_0	$ \mathcal{M}^2 /16\pi$ [mb GeV 2]	πN	ηN	$\pi \Delta$	branching ratio in %			
		[MeV]	[MeV]	NR				ρN	σN	$\pi N^*(1440)$	$\sigma \Delta$
P ₁₁ (1440)	****	1462	391	70	—	69	—	22 _P	—	9	—
S ₁₁ (1535)	***	1534	151	8	60	51	43	—	2 _S + 1 _D	1	2
S ₁₁ (1650)	****	1659	173	4	12	89	3	2 _D	3 _D	2	1
D ₁₃ (1520)	****	1524	124	4	12	59	—	5 _S + 15 _D	21 _S	—	—
D ₁₅ (1675)	****	1676	159	17	—	47	—	53 _D	—	—	—
P ₁₃ (1720)	*	1717	383	4	12	13	—	—	87 _P	—	—
F ₁₅ (1680)	****	1684	139	4	12	70	—	10 _P + 1 _F	5 _P + 2 _F	12	—
P ₃₃ (1232)	****	1232	118	OBE	210	100	—	—	—	—	—
S ₃₁ (1620)	**	1672	154	7	21	9	—	62 _D	25 _S + 4 _D	—	—
D ₃₃ (1700)	*	1762	599	7	21	14	—	74 _S + 4 _D	8 _S	—	—
P ₃₁ (1910)	****	1882	239	14	—	23	—	—	—	67	10 _P
P ₃₃ (1600)	***	1706	430	14	—	12	—	68 _P	—	20	—
F ₃₅ (1905)	***	1881	327	7	21	12	—	1 _P	87 _P	—	—
F ₃₇ (1950)	****	1945	300	14	—	38	—	18 _F	—	—	44 _F

- production channels in Teis: $NN \rightarrow N\Delta$, $NN \rightarrow NN^*$, $N\Delta^*$, $NN \rightarrow \Delta\Delta$
- extension to $NN \rightarrow \Delta N^*$, $\Delta\Delta^*$, $NN \rightarrow NN\pi$, $NN \rightarrow NN\rho$, $NN\omega$, $NN\pi\omega$, $NN\phi$, $NN \rightarrow BYK$ ($B = N, \Delta, Y = \Lambda, \Sigma$)

GiBUU Extension to HADES energies

- good description of total pp, pn (inelastic) cross section



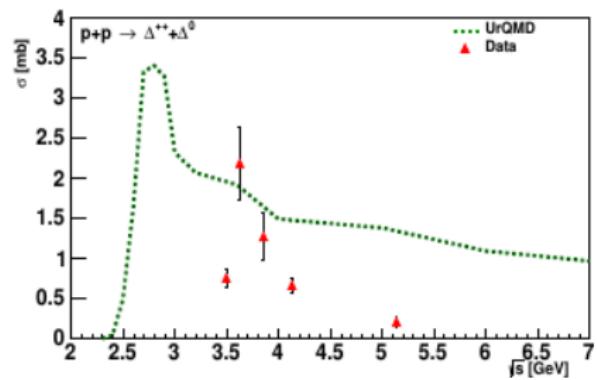
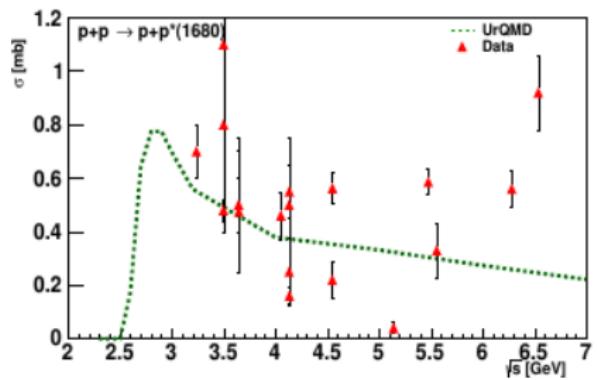
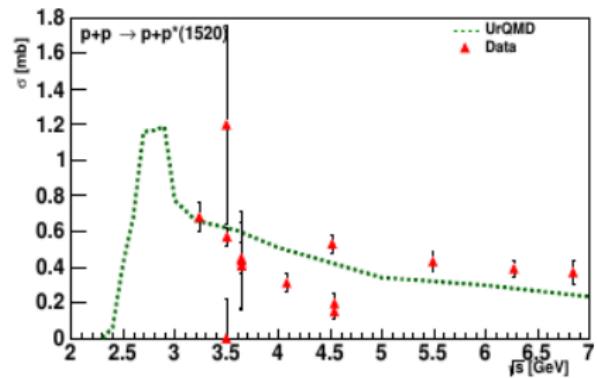
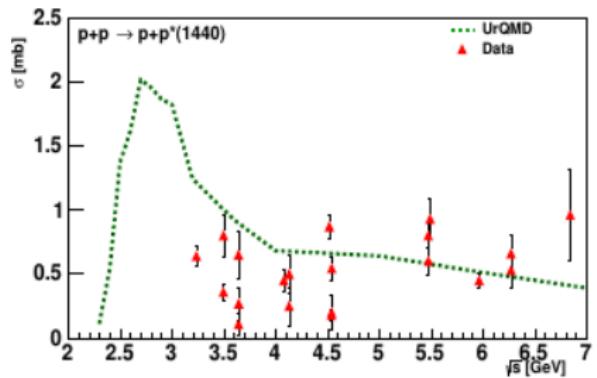
- dilepton sources

- Dalitz decays: $\pi^0, \eta \rightarrow \gamma \ell^+ \ell^-$; $\omega \rightarrow \pi^0 \ell^+ \ell^-$, $\Delta \rightarrow N \ell^+ \ell^-$
- $\rho, \omega, \phi \rightarrow \ell^+ \ell^-$: invariant mass $\ell^+ \ell^-$ spectra \Rightarrow spectral properties of vector mesons
- for details, see [WHD12]

UrQMD: Baryon resonances

Resonance	Mass	Width	$N\pi$	$N\eta$	$N\omega$	$N\varrho$	$N\pi\pi$	$\Delta_{1232}\pi$	$N_{1440}^*\pi$	ΔK	ΣK	$f_0 N$	$a_0 N$
N_{1440}^*	1.440	350	0.65				0.10	0.25					
N_{1520}^*	1.515	120	0.60			0.15	0.05	0.20					
N_{1535}^*	1.550	140	0.60	0.30			0.05		0.05				
N_{1650}^*	1.645	160	0.60	0.06		0.06	0.04	0.10	0.05	0.07	0.02		
N_{1675}^*	1.675	140	0.40					0.55	0.05				
N_{1680}^*	1.680	140	0.60			0.10	0.10	0.15	0.05				
N_{1700}^*	1.730	150	0.05			0.20	0.30	0.40	0.05				
N_{1710}^*	1.710	500	0.16	0.15		0.05	0.21	0.20	0.10	0.10	0.03		
N_{1720}^*	1.720	550	0.10			0.73	0.05			0.10	0.02		
N_{1900}^*	1.850	350	0.30	0.14	0.39	0.15					0.02		
N_{1990}^*	1.950	500	0.12			0.43	0.19	0.14	0.05	0.03		0.04	
N_{2080}^*	2.000	550	0.42	0.04	0.15	0.12	0.05	0.10			0.12		
N_{2190}^*	2.150	470	0.29			0.24	0.10	0.15	0.05	0.12			
N_{2220}^*	2.220	550	0.29		0.05	0.22	0.17	0.20			0.12		
N_{2250}^*	2.250	470	0.18			0.25	0.20	0.20	0.05	0.12			
Δ_{1232}	1.232	115	1.00										
Δ_{1600}^*	1.700	350	0.10				0.65	0.25					
Δ_{1620}^*	1.675	160	0.15			0.05		0.65	0.15				
Δ_{1700}^*	1.750	350	0.20			0.25		0.55					
Δ_{1900}^*	1.840	260	0.25			0.25		0.25	0.25				
Δ_{1905}^*	1.880	350	0.18			0.80		0.02					
Δ_{1910}^*	1.900	250	0.30			0.10		0.35	0.25				
Δ_{1920}^*	1.920	200	0.27				0.40	0.30	0.03				
Δ_{1930}^*	1.970	350	0.15			0.22		0.20	0.28	0.15			
Δ_{1950}^*	1.990	350	0.38			0.08		0.20	0.18	0.12		0.04	

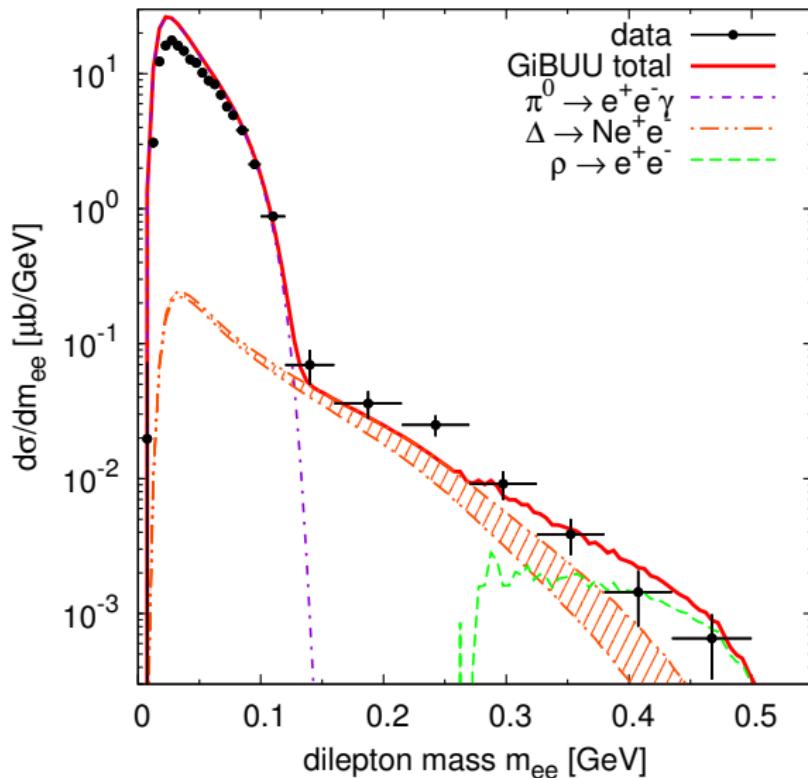
UrQMD: Baryon resonances



Dileptons in pp, pA, and AA collisions at SIS energies

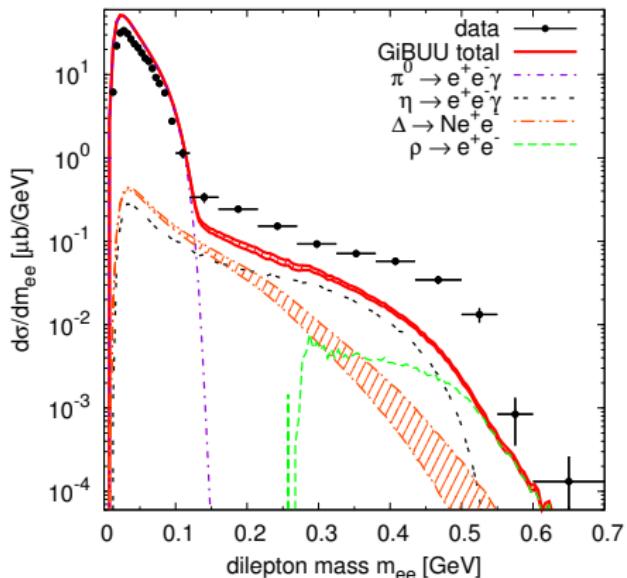
GiBUU: p+p (1.25 GeV) (SIS/HADES)

p + p at 1.25 GeV



d+p (1.25 GeV) (SIS/HADES)

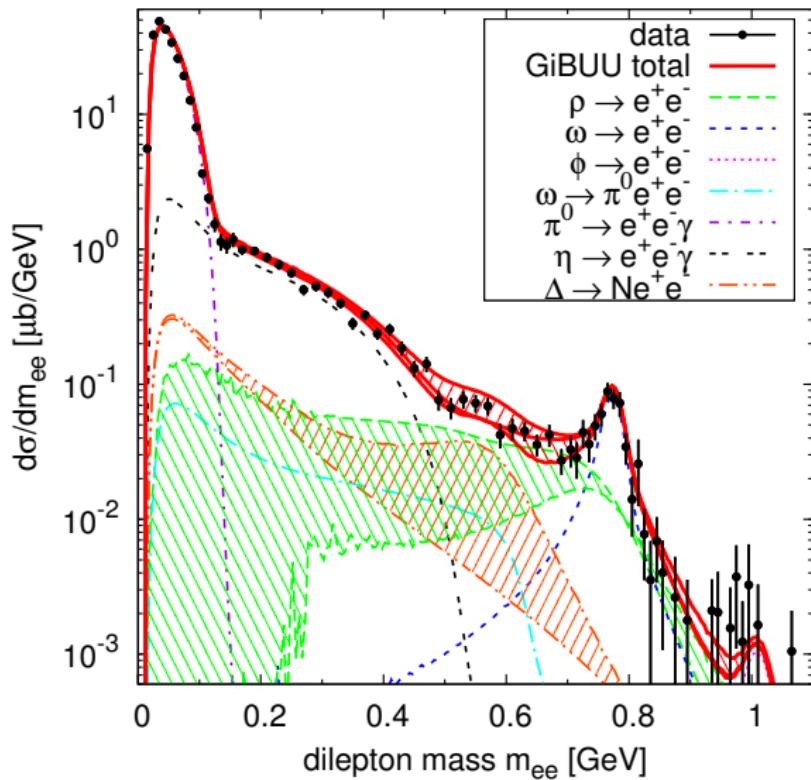
d + p at 1.25 GeV



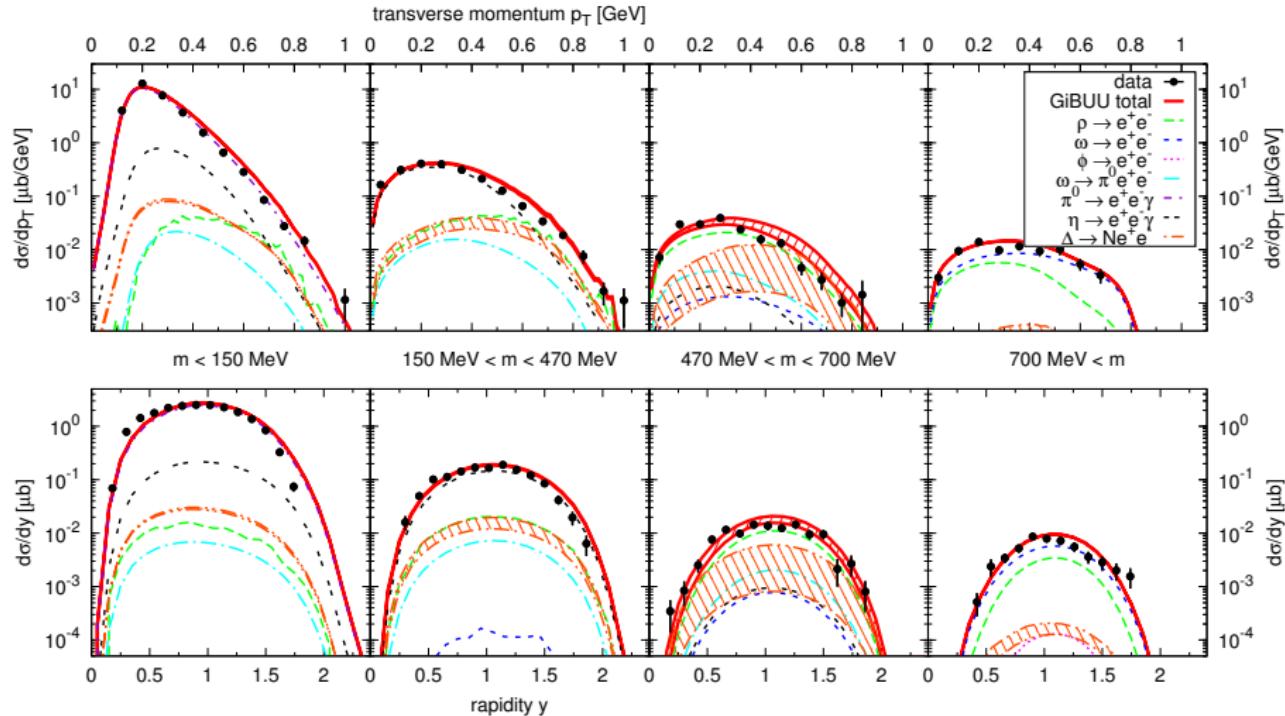
- triggered on forward protons → **quasifree np scattering**
- model uncertainties:
 - ρ production through $D_{13}(1525)$ (isospin symmetric?)
 - $S_{11}(1535)$ [enhanced in np; (from η production)]
 - d-wave function treatable as quasiclassical “distribution”?
 - bremsstrahlung contributions

GiBUU: p+p (3.5 GeV) (SIS/HADES)

p + p at 3.5 GeV

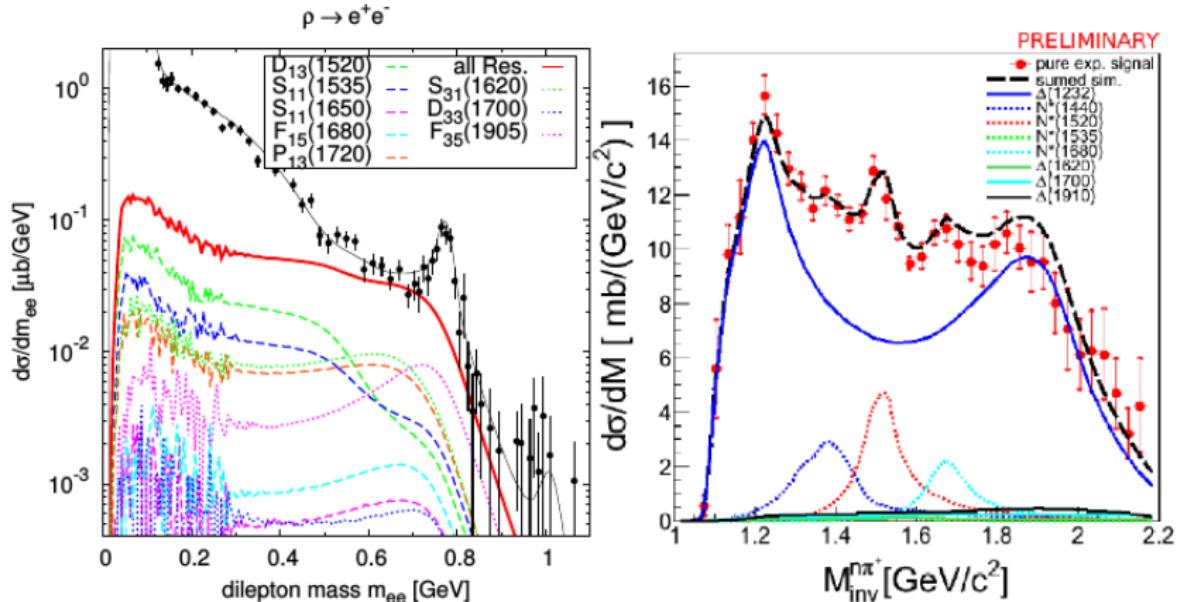


GiBUU: p+p (3.5 GeV) (SIS/HADES)



GiBUU: “ ρ meson” in pp

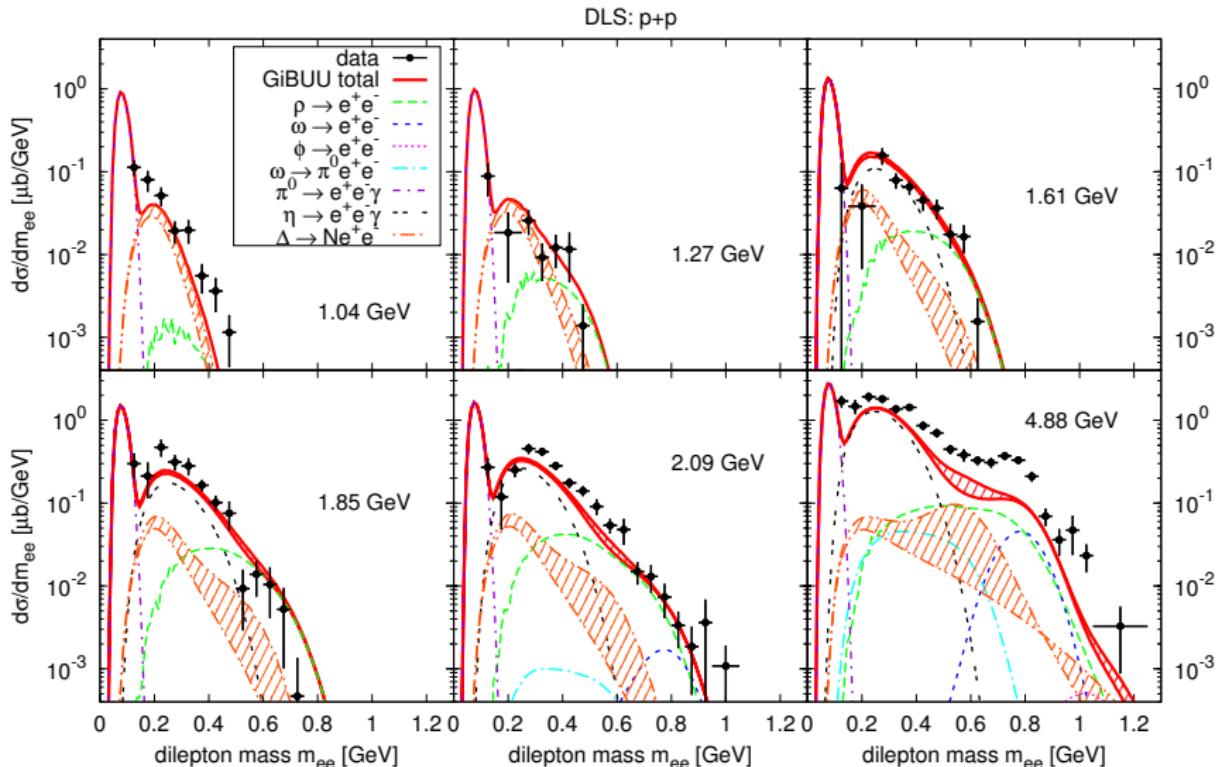
- production through hadron resonances
 $NN \rightarrow NR \rightarrow NN\rho$, $NN \rightarrow N\Delta \rightarrow NN\pi\rho$



- “ ρ ”-line shape “modified” already in elementary hadronic reactions
- due to production mechanism via resonances

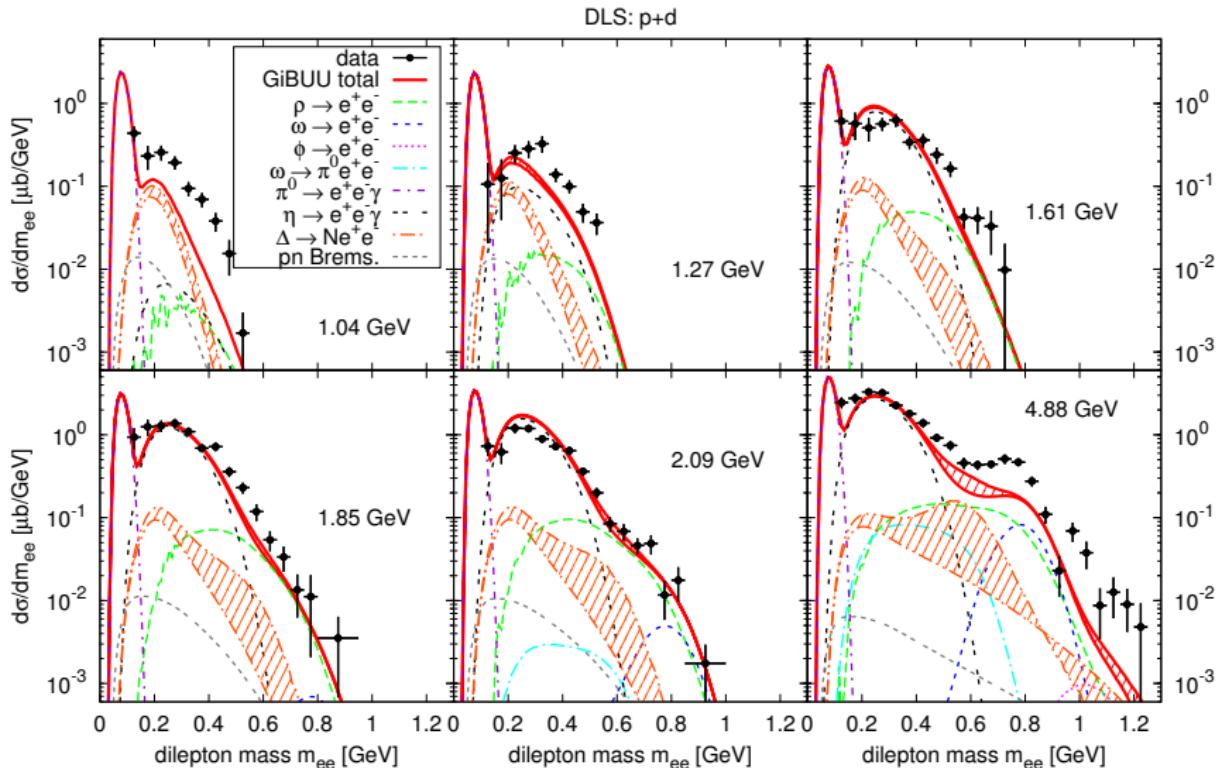
GiBUU: Comparison to old DLS data (pp)

- HADES data consistent with DLS data
- checked by comparing HADES data within DLS acceptance



GiBUU: Comparison to old DLS data (pd)

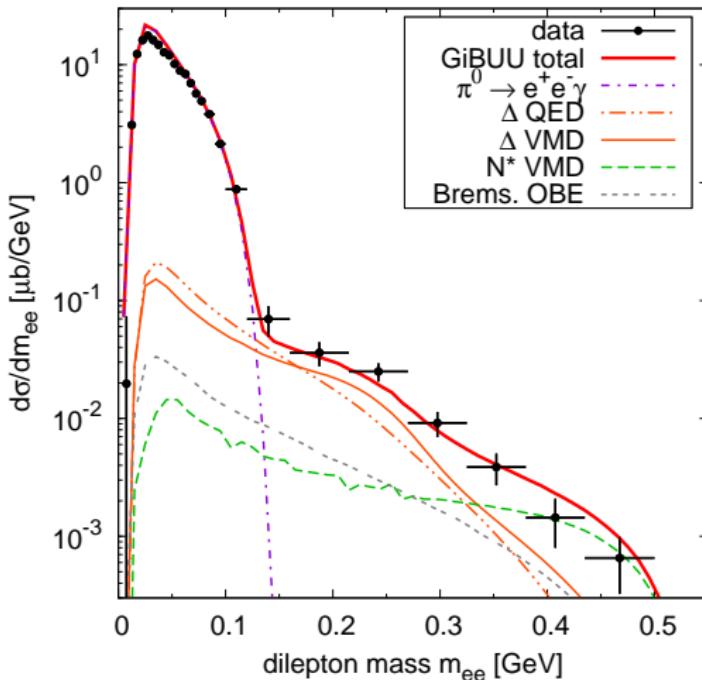
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GiBUU: Δ meson in VMD model

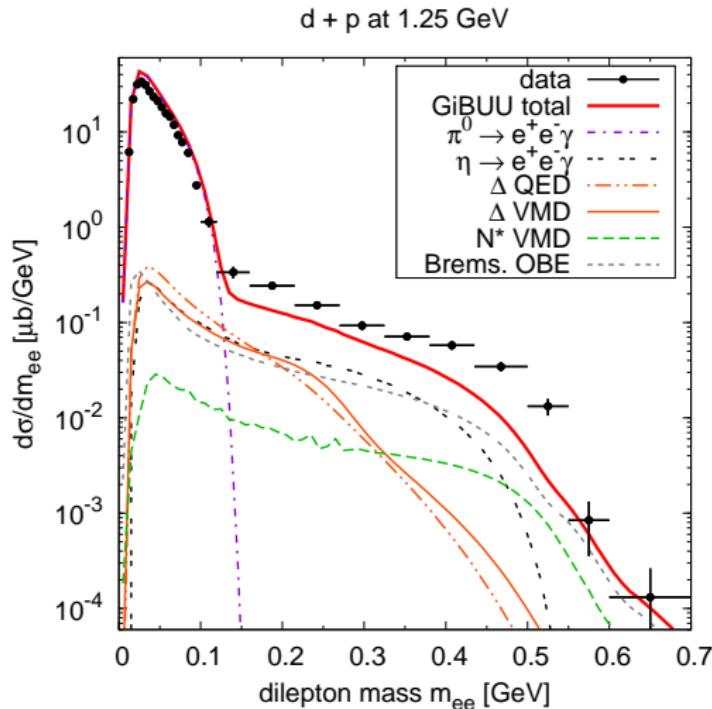
- so far: Δ -Dalitz decay treated separately from other resonances
- now: treating Δ as all other resonances via VMD model

p + p at 1.25 GeV



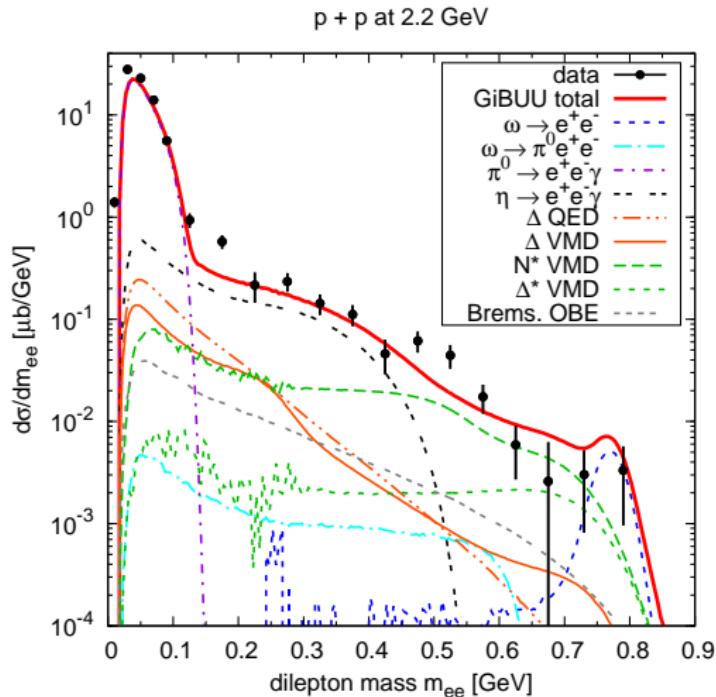
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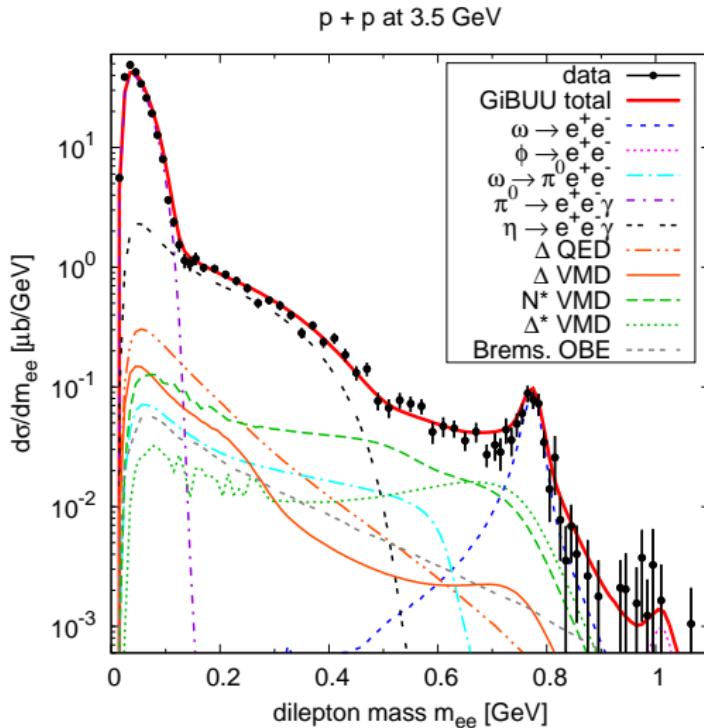
GiBUU: Δ meson in VMD model

- so far: Δ -Dalitz decay treated separately from other resonances
- now: treating Δ as all other resonances via VMD model



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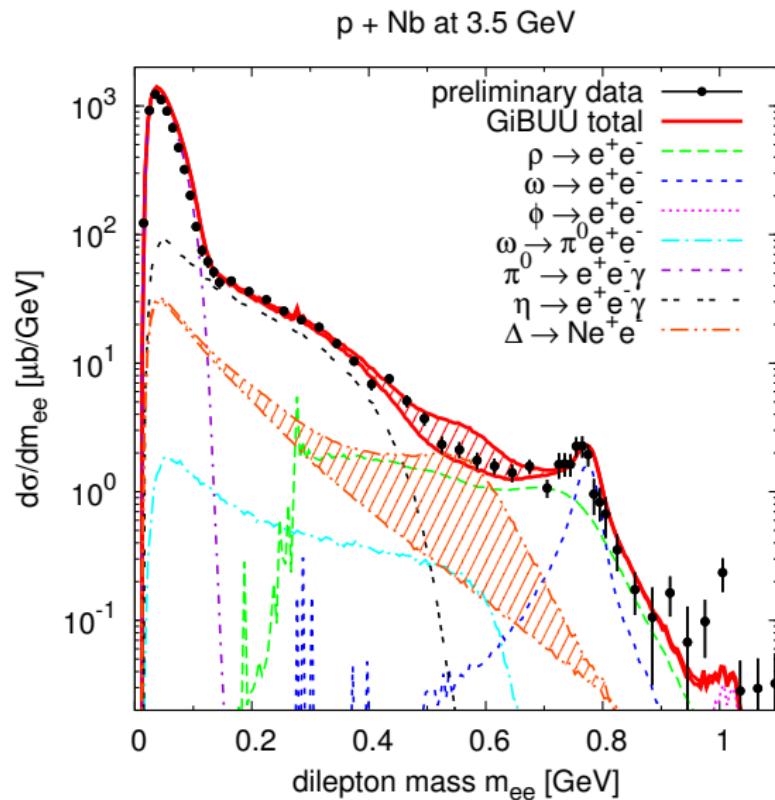
GiBUU: p+Nb (3.5 GeV) (SIS/HADES)

GiBUU:

- medium effects built in transport model
 - binding effects, Fermi smearing, Pauli blocking
 - final-state interactions
 - production from secondary collisions
- sensitivity to additional **in-medium modifications of vector mesons?**

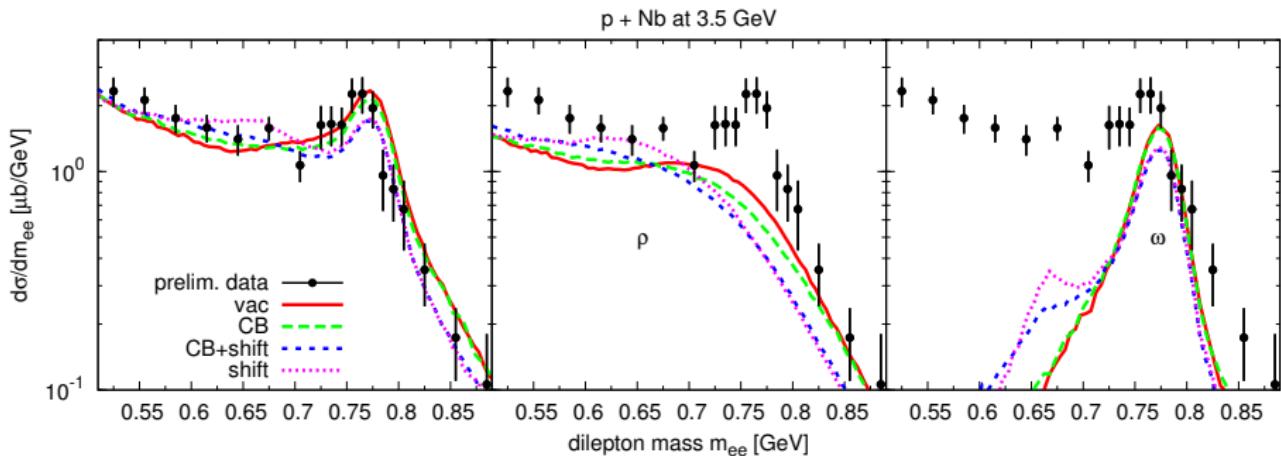
GiBUU: p+Nb (3.5 GeV) (SIS/HADES)

- with vacuum spectral functions:



GiBUU: p+Nb (3.5 GeV) (SIS/HADES)

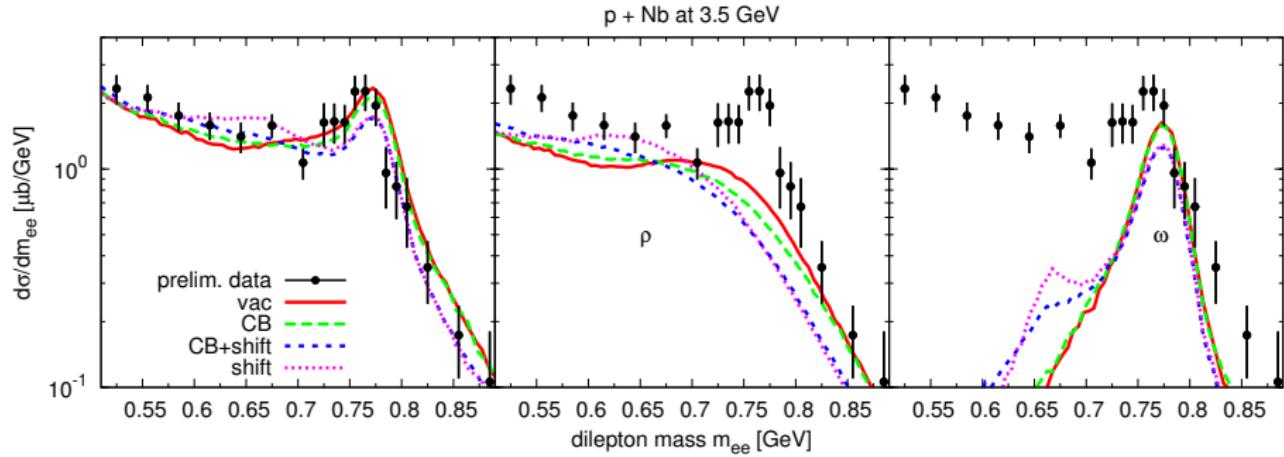
- with medium modified spectral functions:



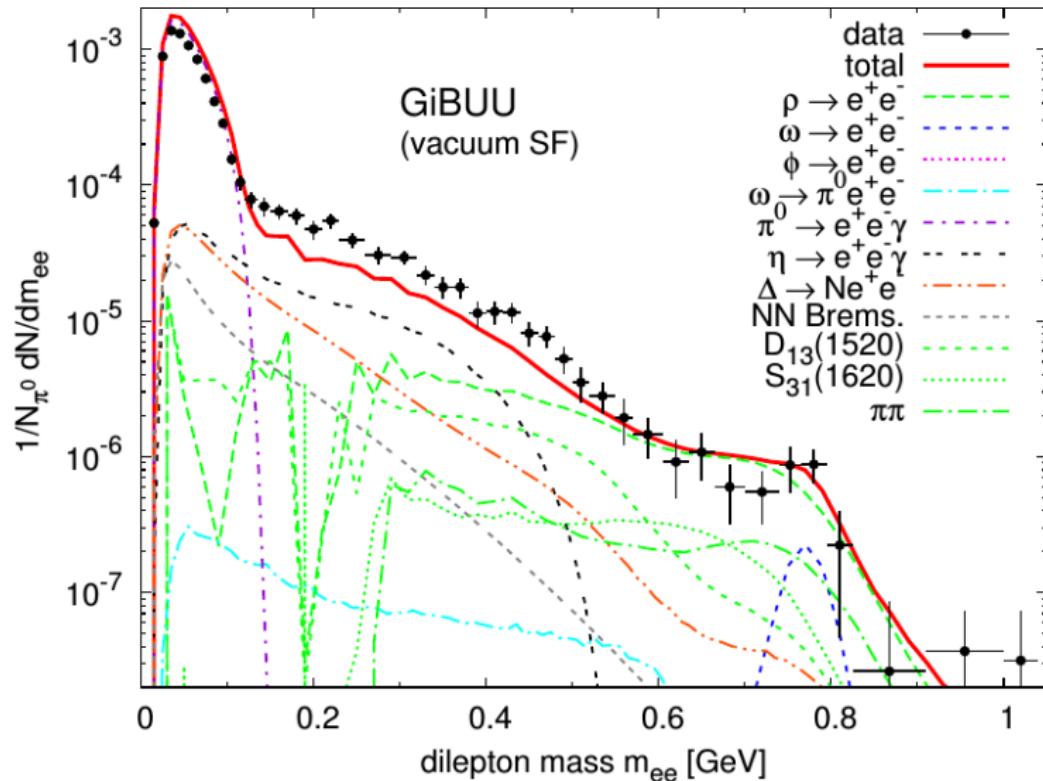
- no definite hint for medium modifications in p Nb

GiBUU: p+Nb (3.5 GeV) (SIS/HADES)

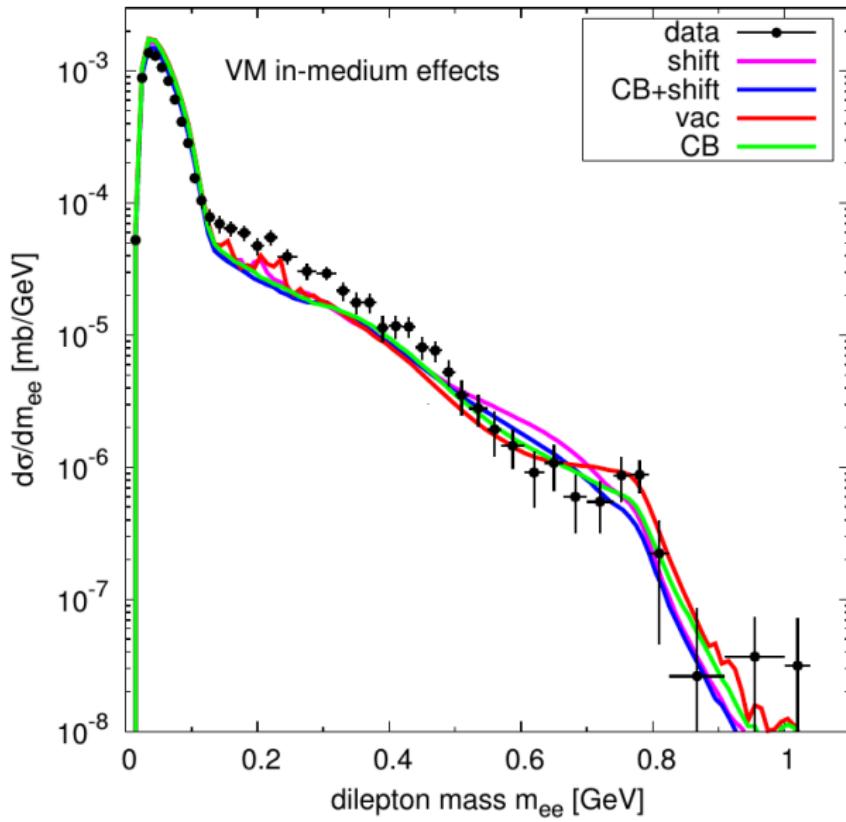
- medium effects built in transport model
 - binding effects, Fermi smearing, Pauli blocking
 - final-state interactions
 - production from secondary collisions
- sensitivity on medium effects of vector-meson spectral functions?



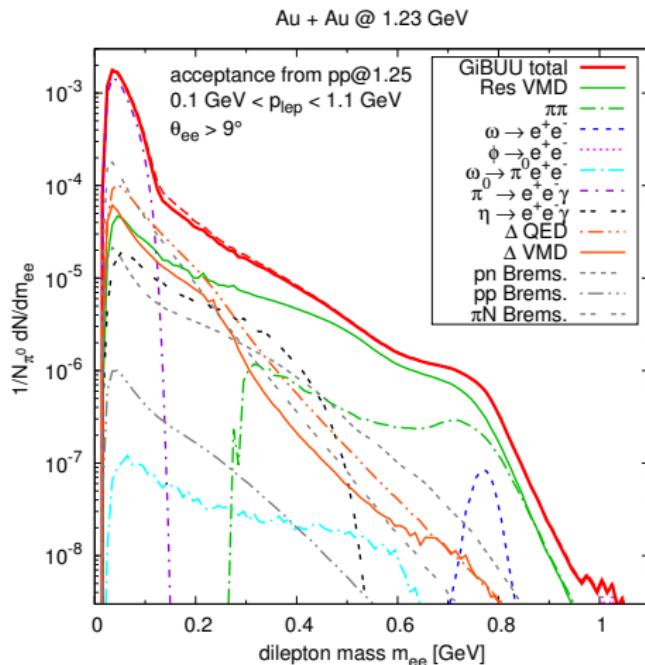
GiBUU: Ar+KCl (1.76AGeV) (SIS/HADES)



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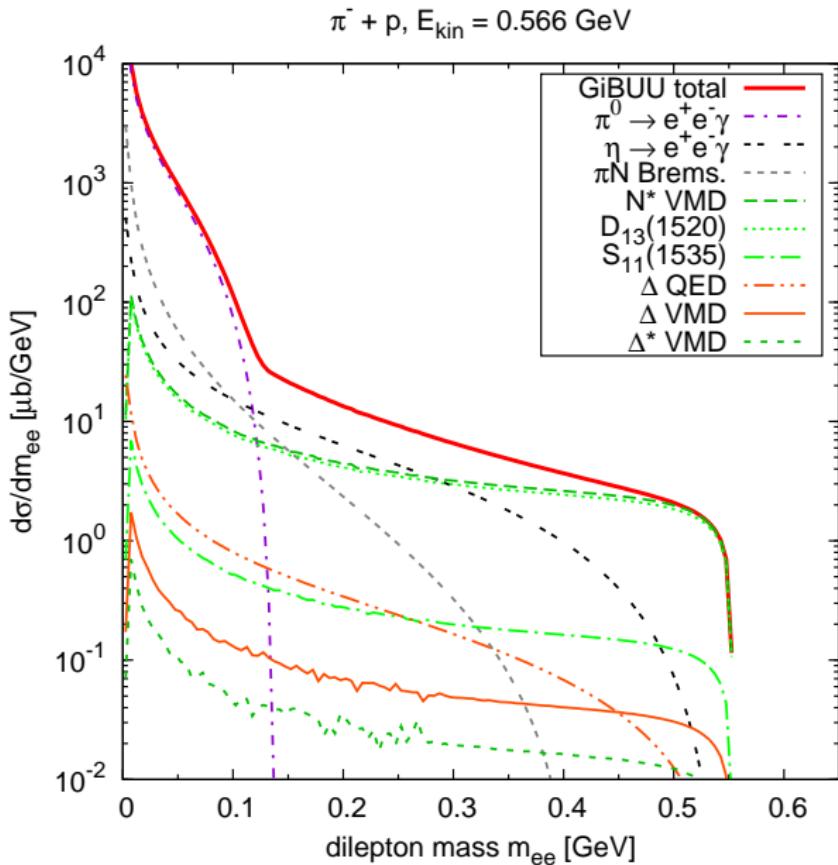


GiBUU (NEW!): Au+Au (1.23 AGeV) (SIS/HADES)

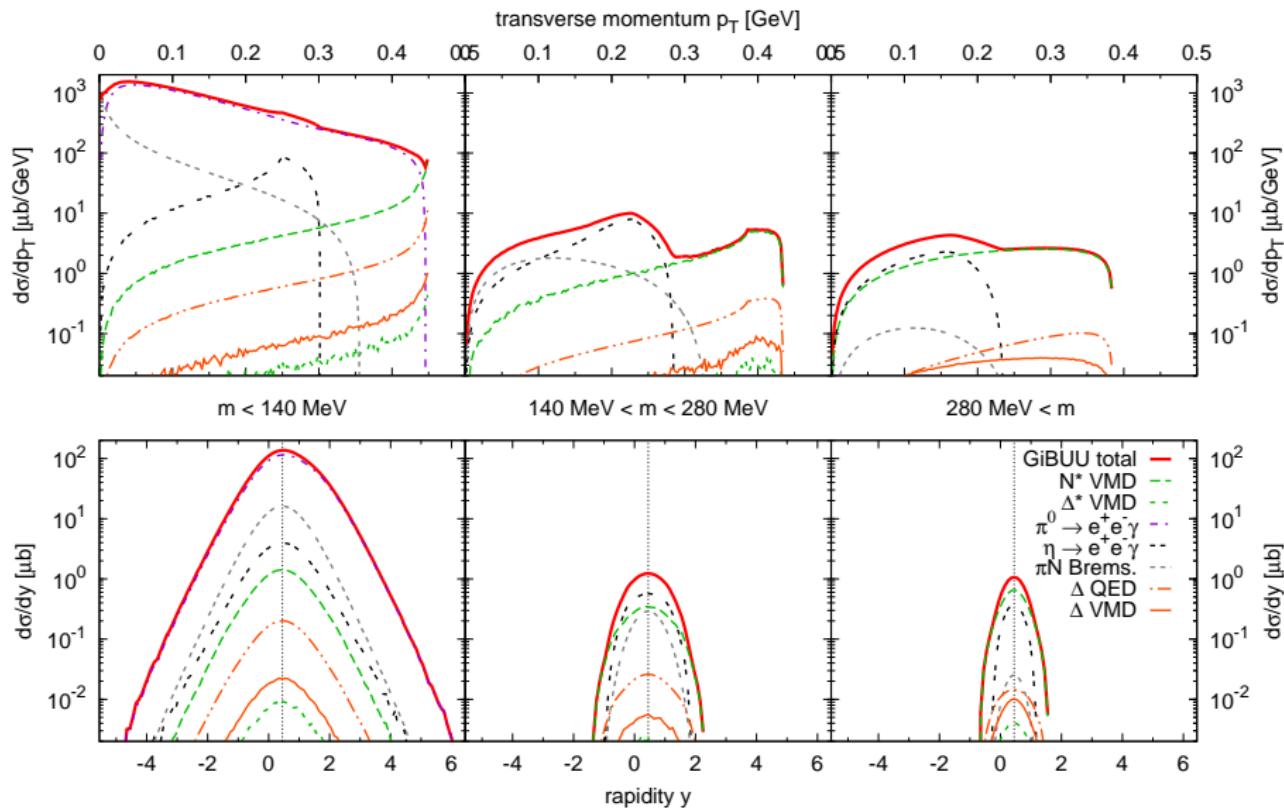


- caveat: pp/np acceptance filter with single-e cut, $p_t < 100$ MeV
- correct filter urgently needed!
- comparison to preliminary HADES data [Gal14] \Rightarrow room for medium modifications (data points not shown here on request of the HADES collaboration)

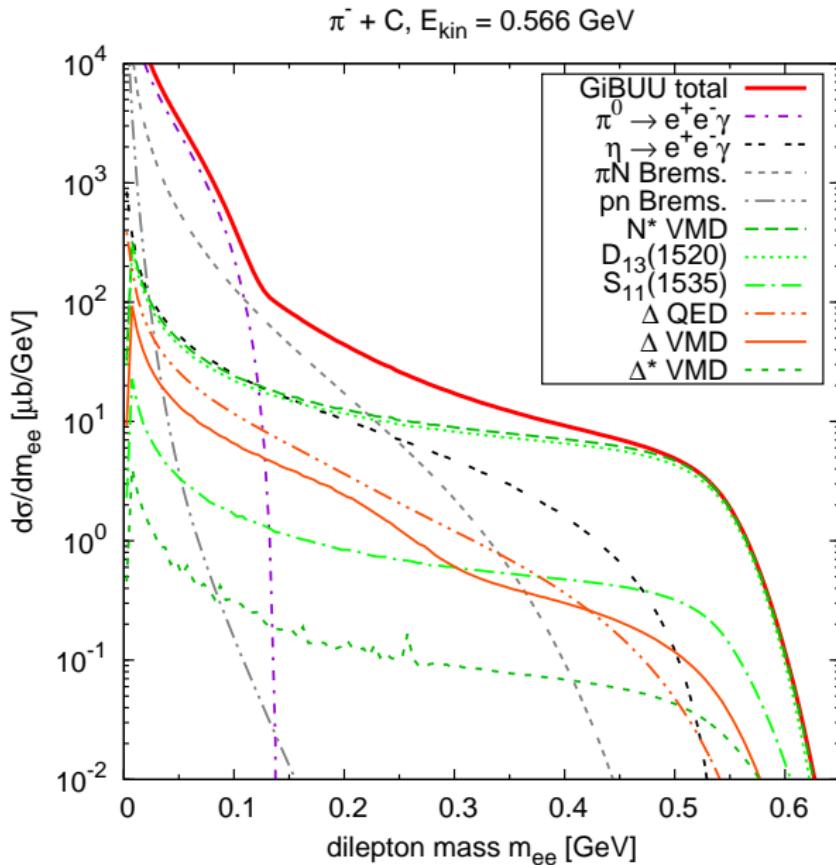
GiBUU (NEW!): $\pi^- + p$ (566 MeV) (SIS/HADES)



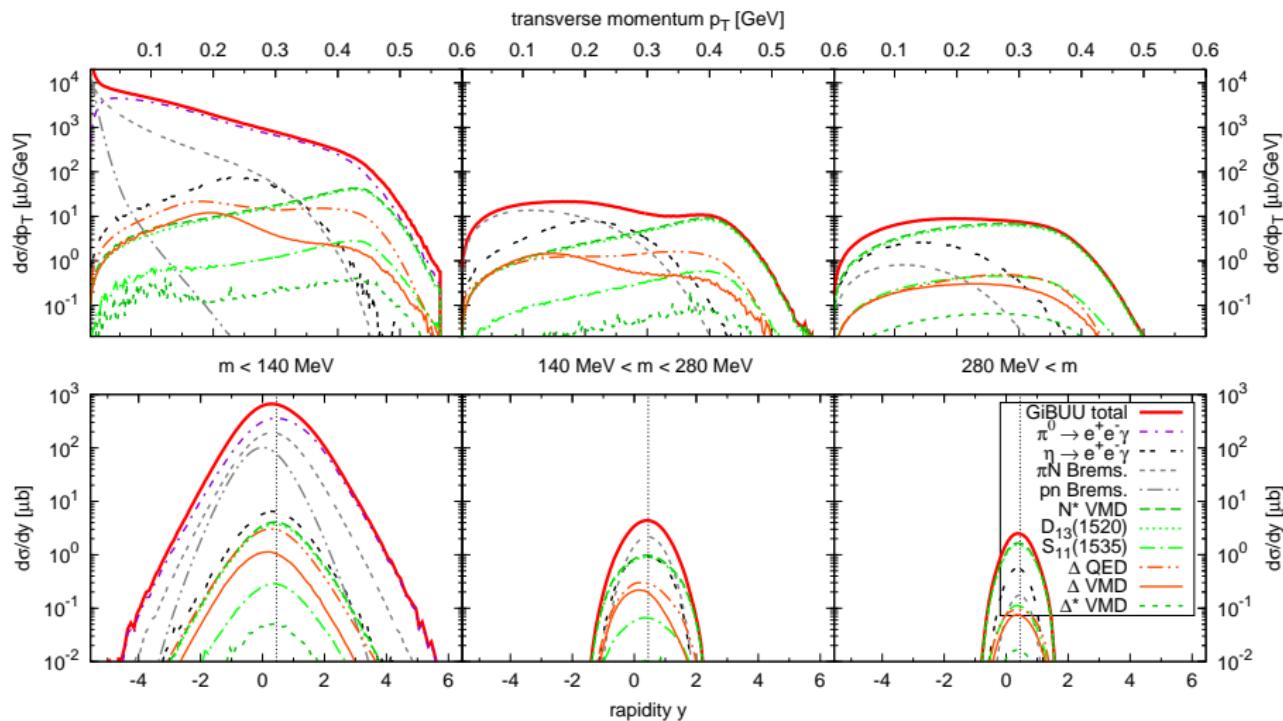
GiBUU (NEW!): $\pi + p$ (566 MeV) (SIS/HADES)



GiBUU (NEW!): $\pi^- + C$ (566 MeV) (SIS/HADES)



GiBUU (NEW!): $\pi + C$ (566 MeV) at (SIS/HADES)



Heavy-ion collisions and medium effects

“Coarse grained UrQMD” (with Stephan Endres)

Coarse-grained UrQMD (CGUrQMD)

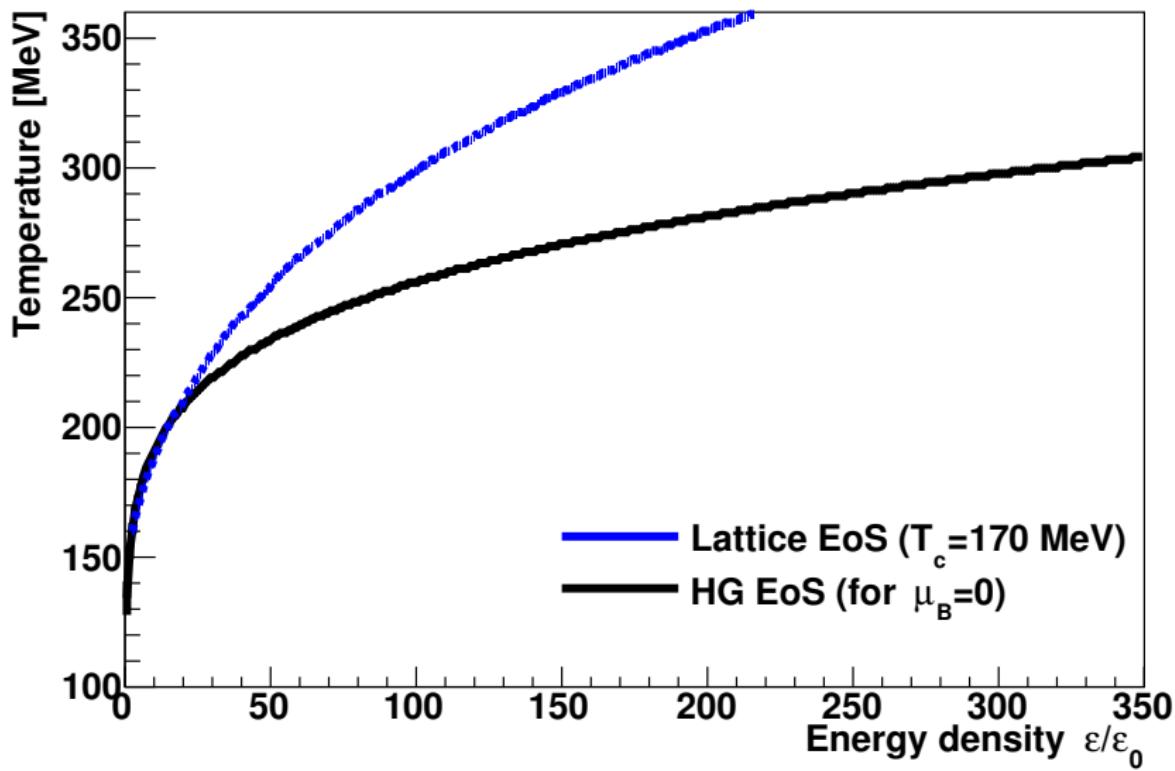
- problem with **medium modifications** of spectral functions/interactions
- only available in equilibrium many-body QFT models
- implementing “in-medium cross sections” naively: **double counting?!?**
- way out: map transport to **local-equilibrium fluid**
- Use **ensemble of UrQMD runs with an equation of state**
- fit **temperature, chemical potentials, flow-velocity field** from anisotropic energy-momentum tensor [W. Florkowski et al, NPA **904-905**, 803c (2013)]

$$T^{\mu\nu} = (\varepsilon + P_{\perp})u^{\mu}u^{\nu} - P_{\perp}g^{\mu\nu} - (P_{\parallel} - P_{\perp})V^{\mu}V^{\nu}$$

- thermal rates from **partonic/hadronic QFT become applicable**
- here: **extrapolated lattice QGP** and **Rapp-Wambach hadronic many-body theory**
- caveat: **consistency between EoS, matter content of QFT model/UrQMD!**

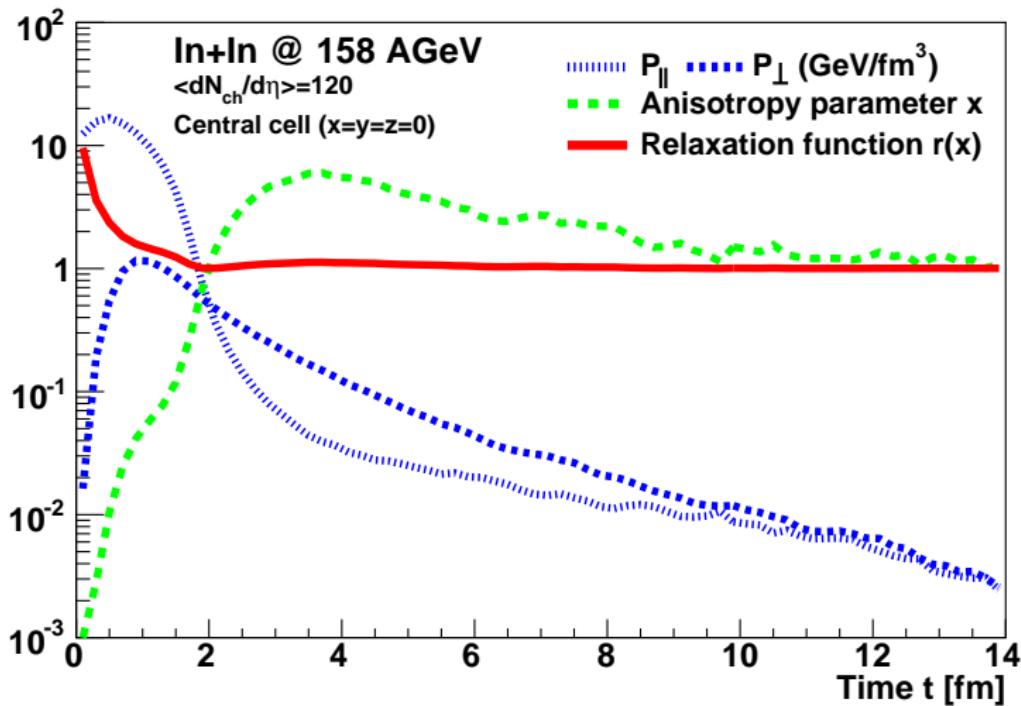
Coarse-grained UrQMD (CGUrQMD)

- $T_c = 170$ MeV; $T > T_c \Rightarrow$ lattice EoS; $T < T_c \Rightarrow$ HRG EoS



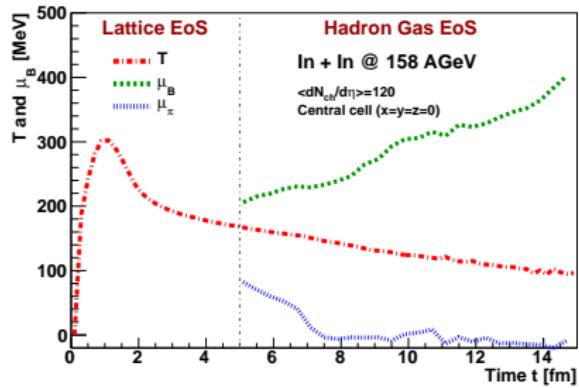
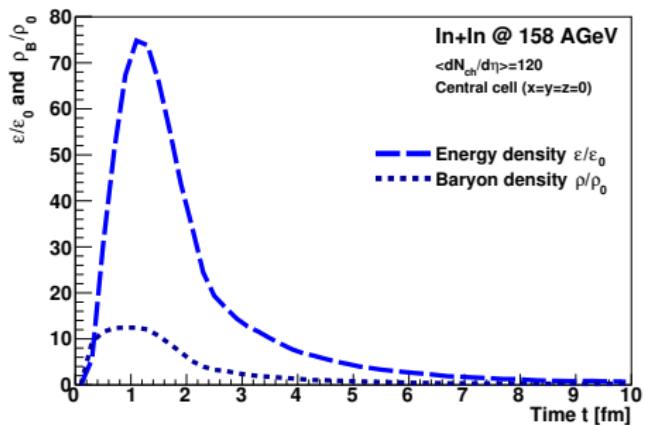
Coarse-grained UrQMD (CGUrQMD)

- pressure anisotropy (In-In collisions (NA60) at SIS)



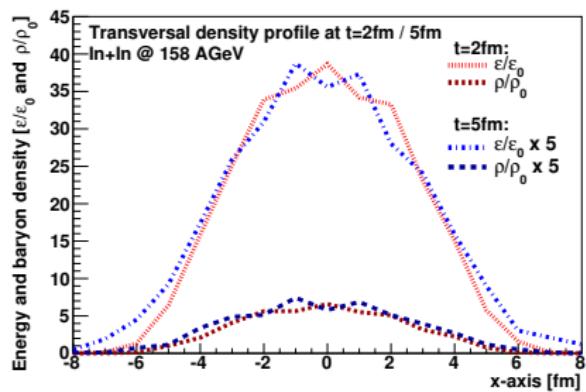
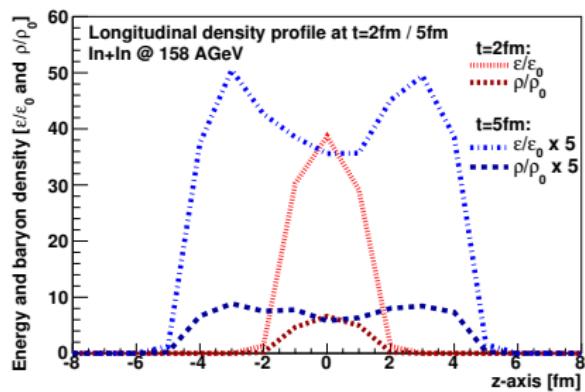
Coarse-grained UrQMD (CGUrQMD)

- energy/baryon density $\Rightarrow T, \mu_B$ (for In+In @ SPS; NA60)
- central “fluid” cell!



Coarse-grained UrQMD (CGUrQMD)

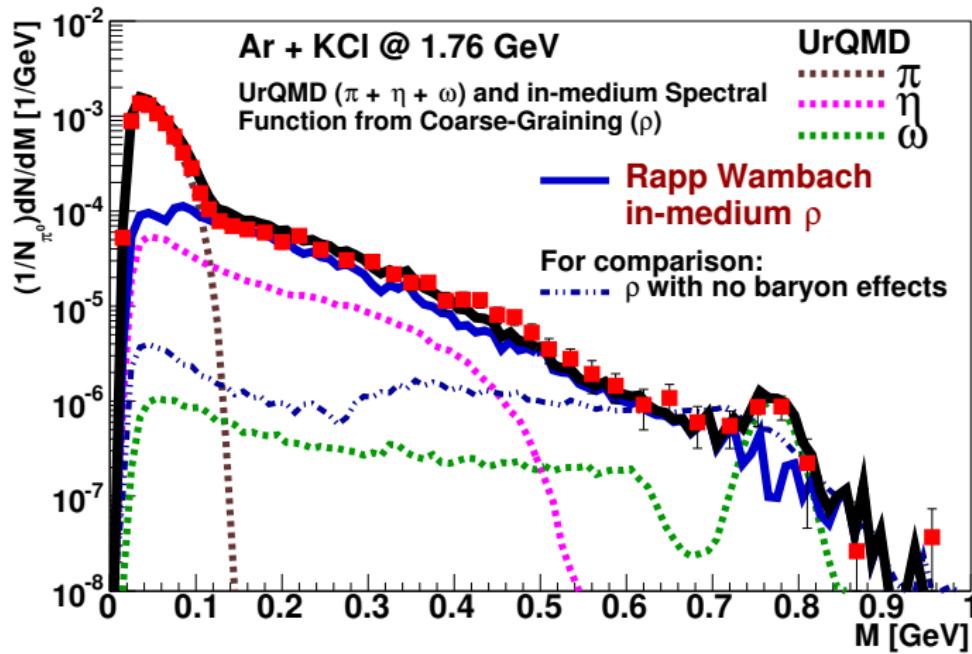
- temperature/density profiles (for In+In@SPS; NA60)



Dielectrons (SIS/HADES)

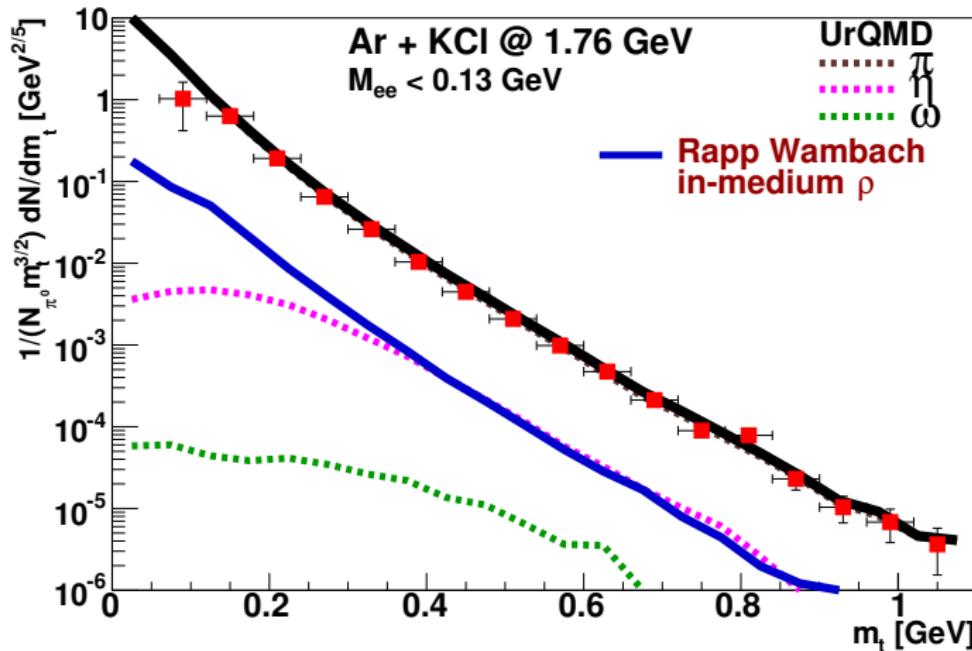
CGUrQMD: Ar+KCl (1.76 AGeV) (SIS/HADES)

- coarse-graining method works at low energies!
- UrQMD-medium evolution + RW-QFT rates



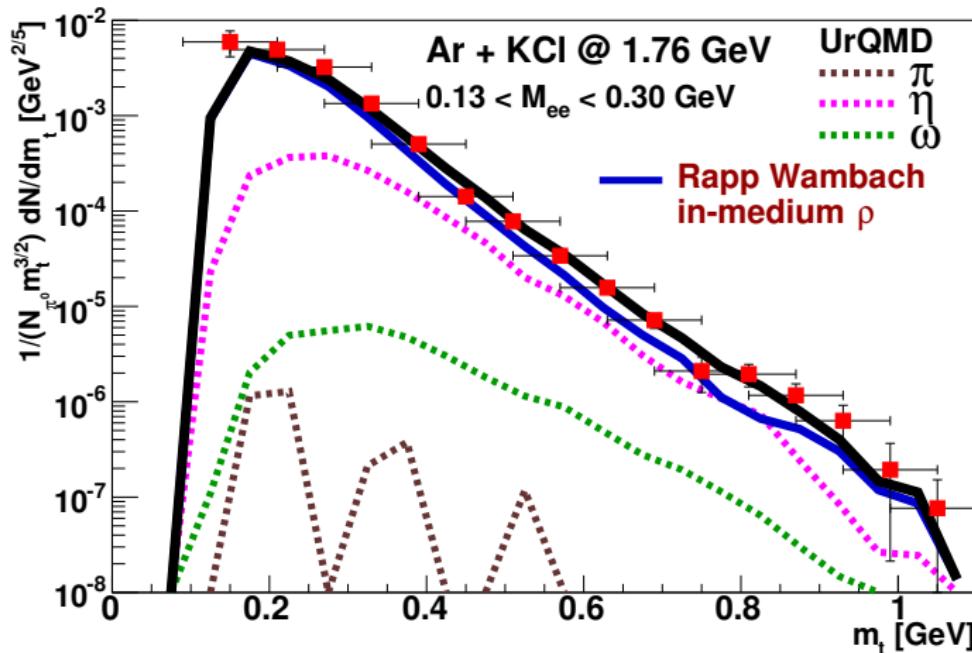
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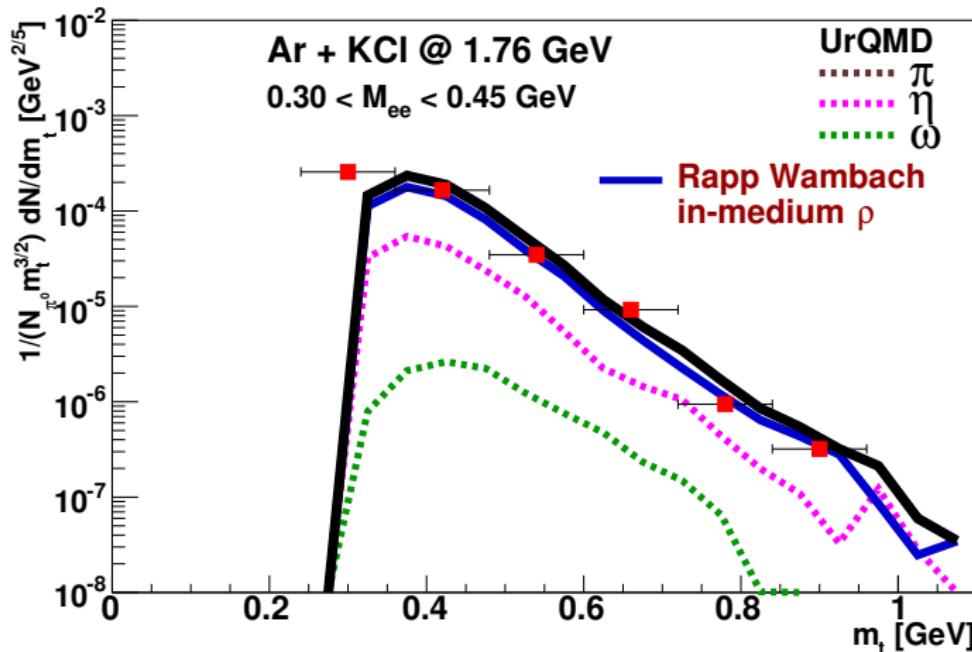
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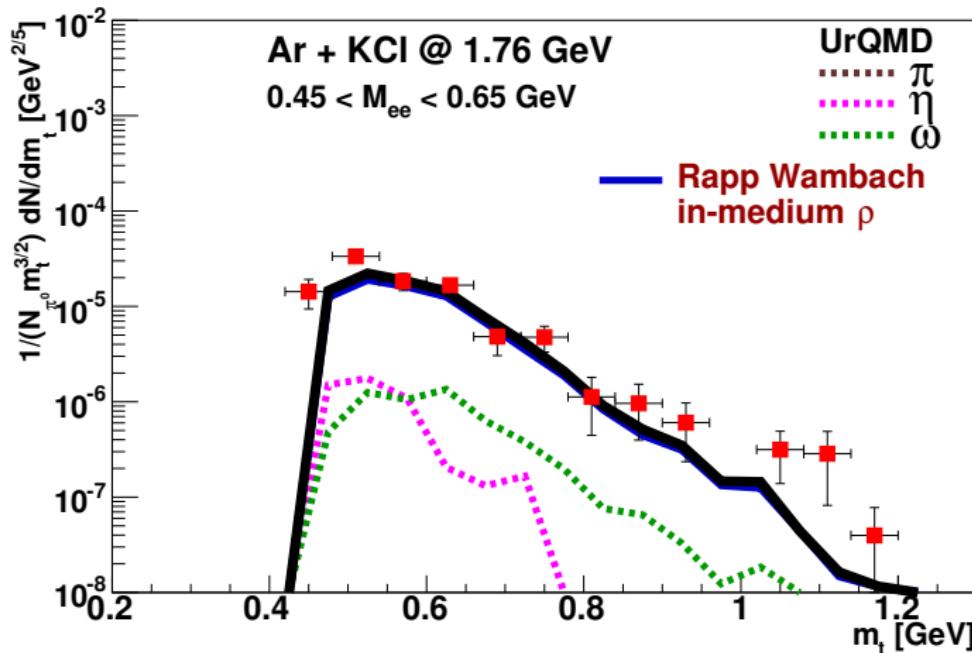
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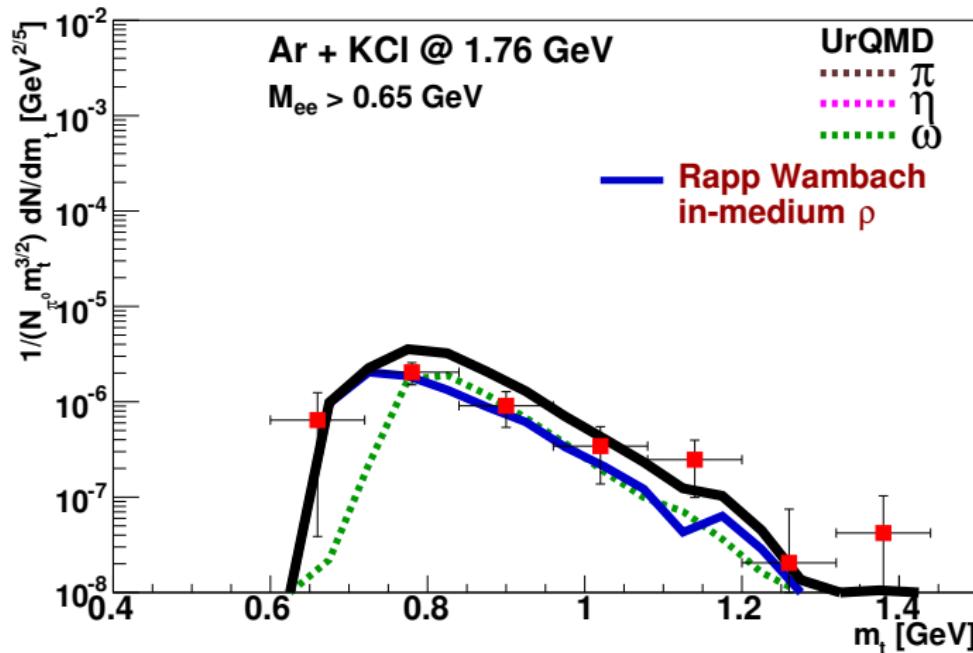
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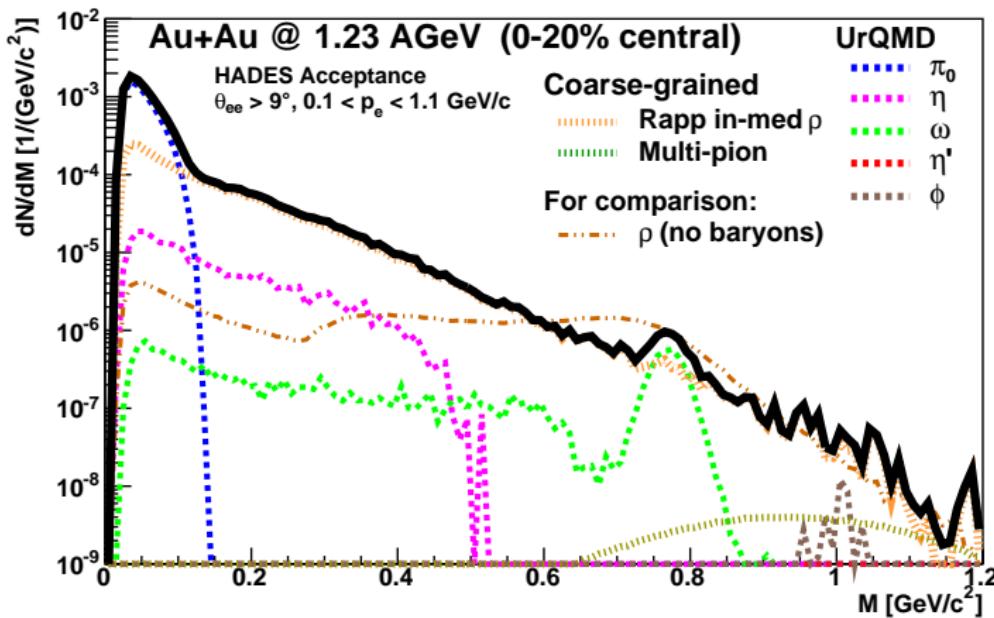


CGUrQMD: Ar+KCl (1.76 AGeV) (SIS/HADES)

- dielectron spectra from Ar + KCl(1.76AGeV) $\rightarrow e^+e^-$ (SIS/HADES)



CGUrQMD: (NEW) Au+Au (1.23 AGeV) (SIS/HADES)

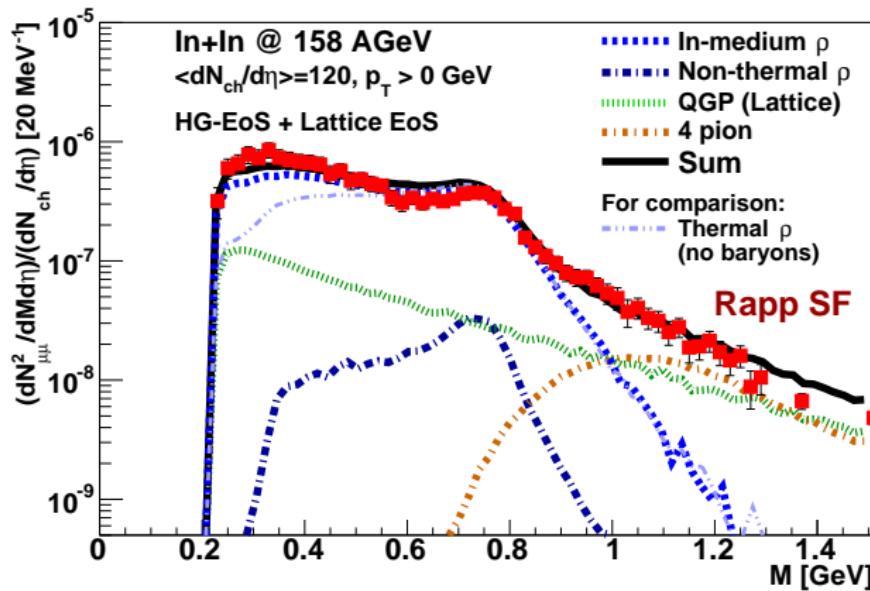


- caveat: pp/np acceptance filter with single-e cut, $p_t < 100 \text{ MeV}$
- correct filter urgently needed!
- excellent agreement with preliminary HADES data [Gal14]
(data points not shown here on request of the HADES collaboration)

Dimuons (SPS/NA60)

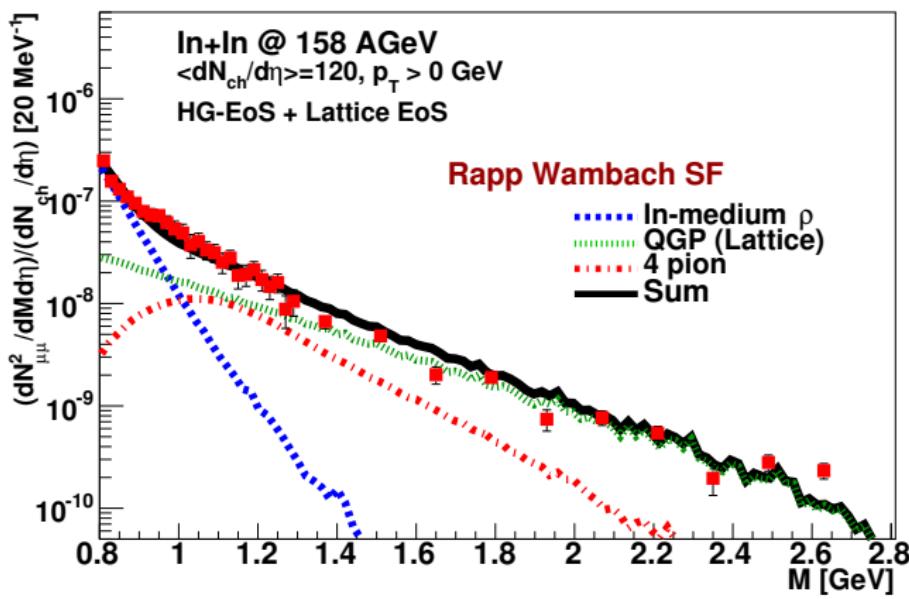
CGUrQMD: In+In (158 AGeV) (SPS/NA60)

- dimuon spectra from $\text{In} + \text{In}(158\text{AGeV}) \rightarrow \mu^+ \mu^-$ (NA60)
- min-bias data ($dN_{\text{ch}}/dy = 120$)



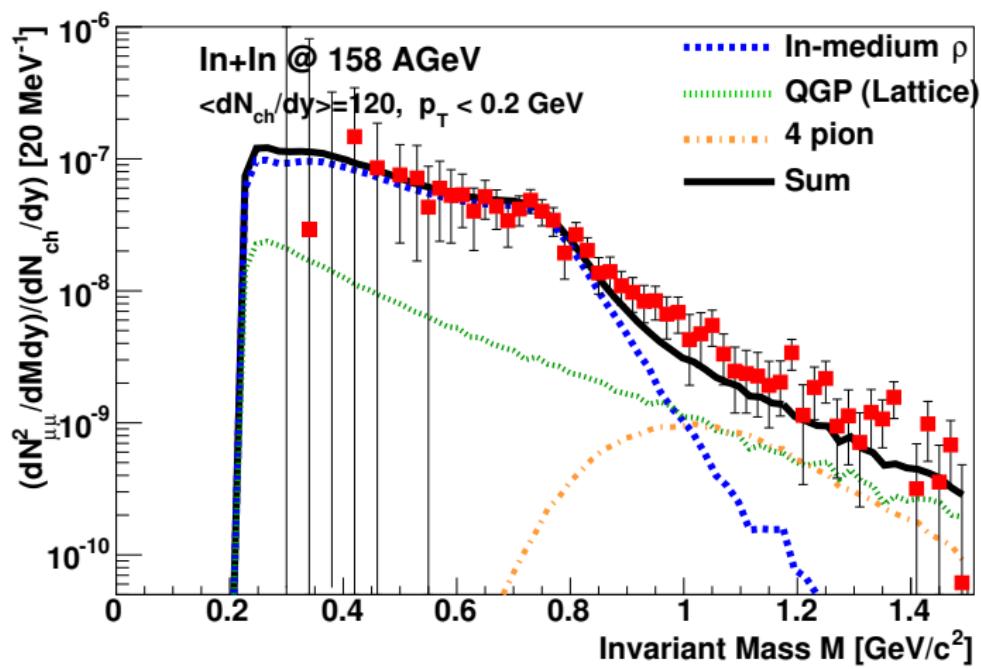
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- dimuon spectra from $\text{In} + \text{In}(158 \text{ AGeV}) \rightarrow \mu^+ \mu^-$ (NA60)
- min-bias data ($dN_{\text{ch}}/dy = 120$)
- higher IMR: provides **averaged true temperature**
(no blueshifts in the **invariant-mass** spectra!)



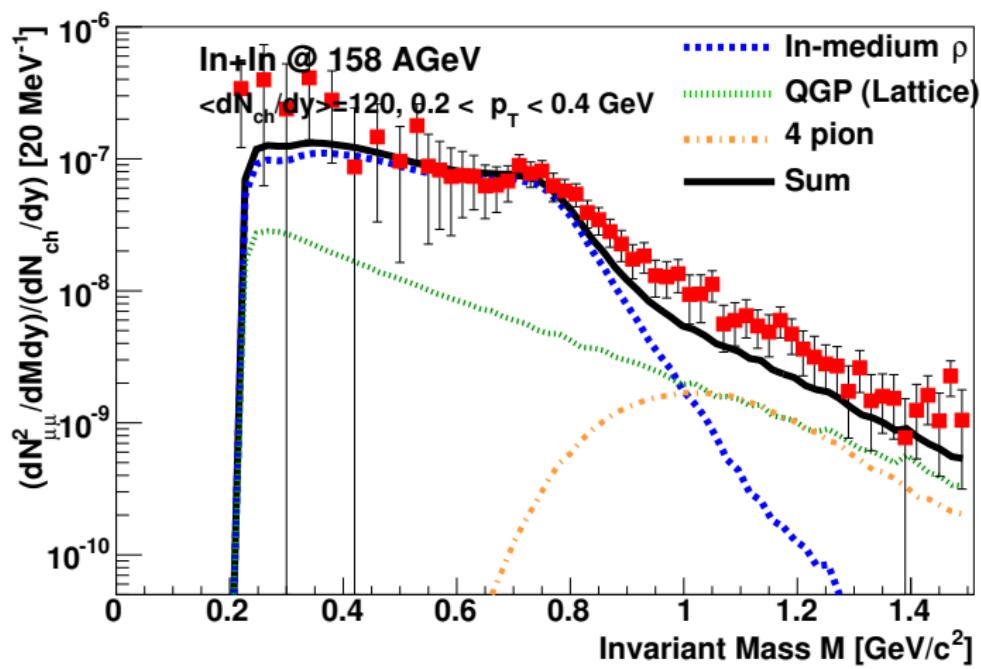
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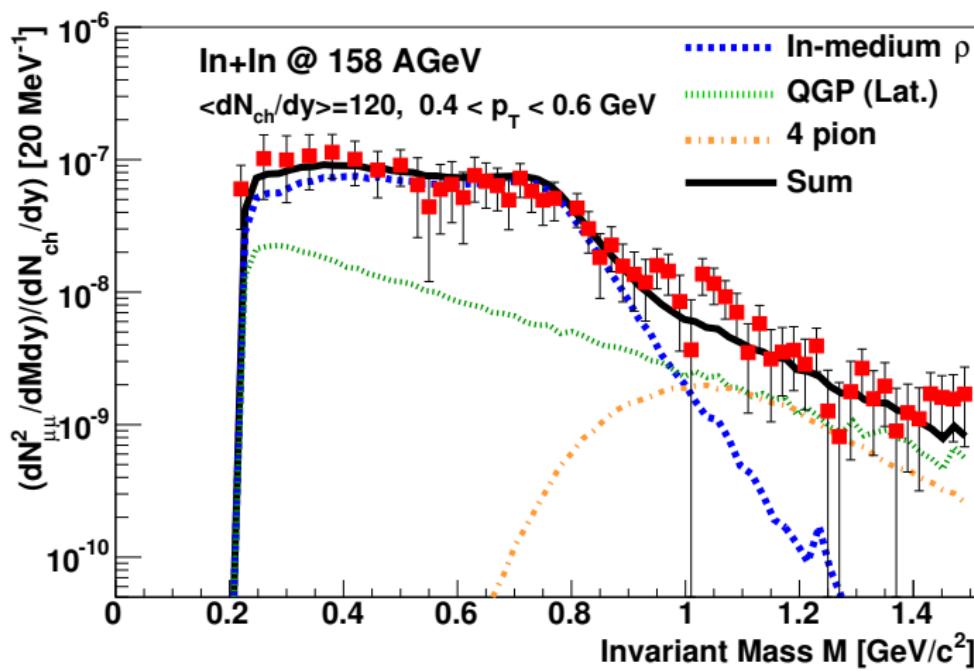
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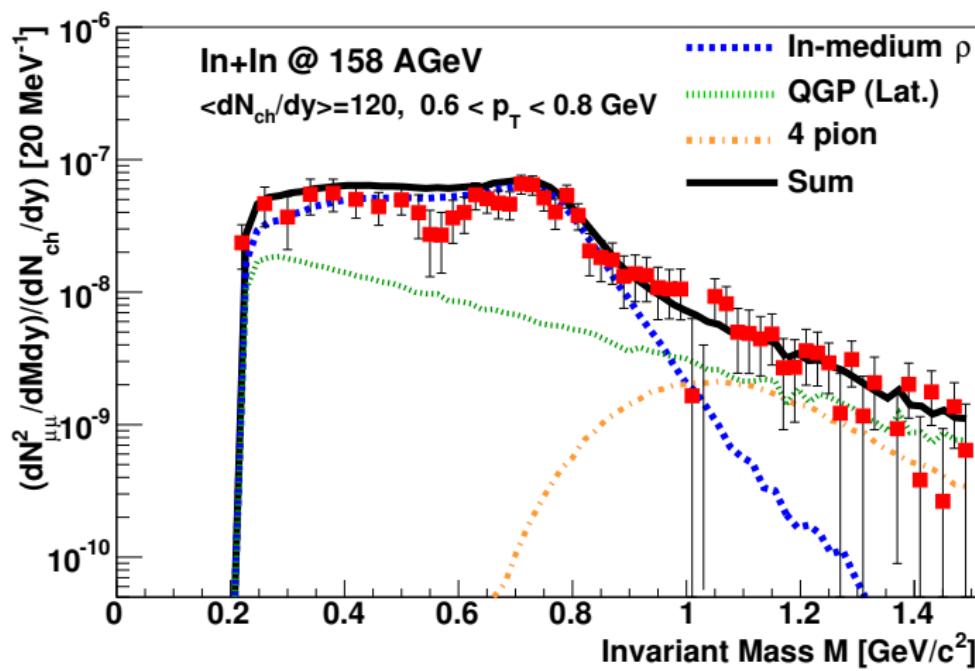
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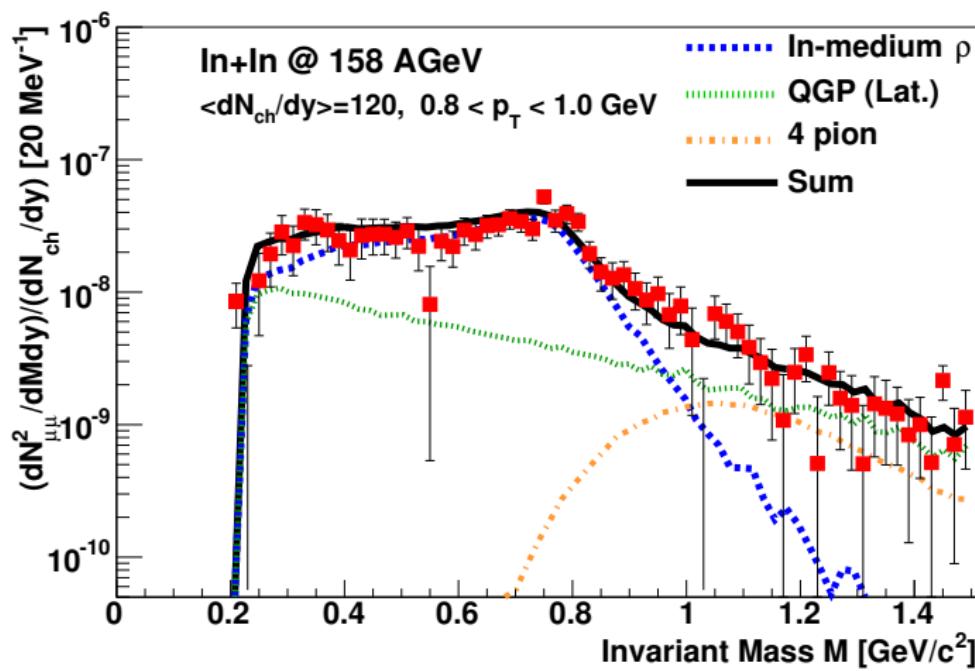
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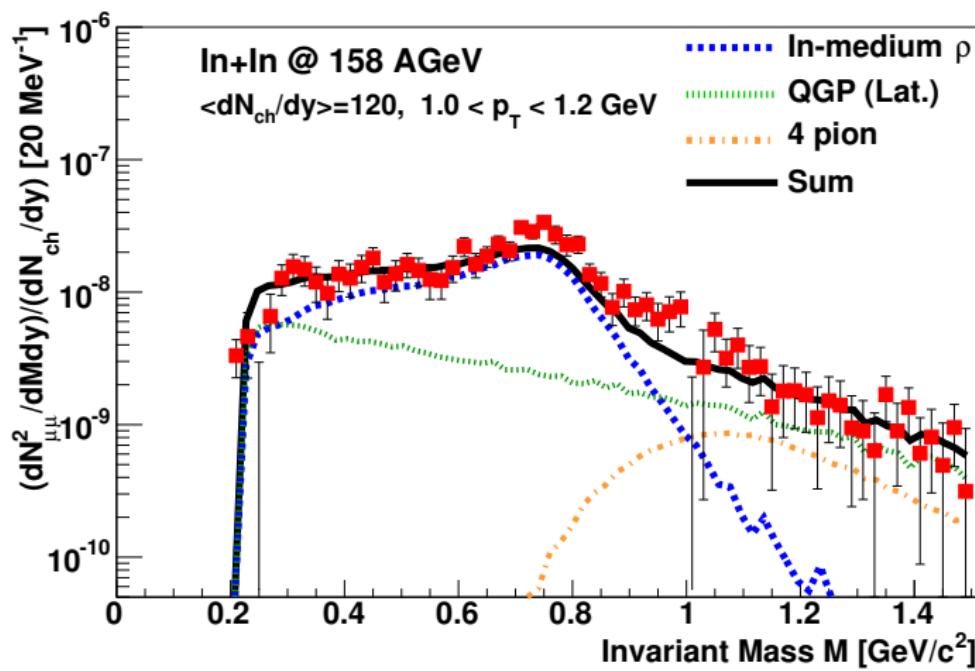
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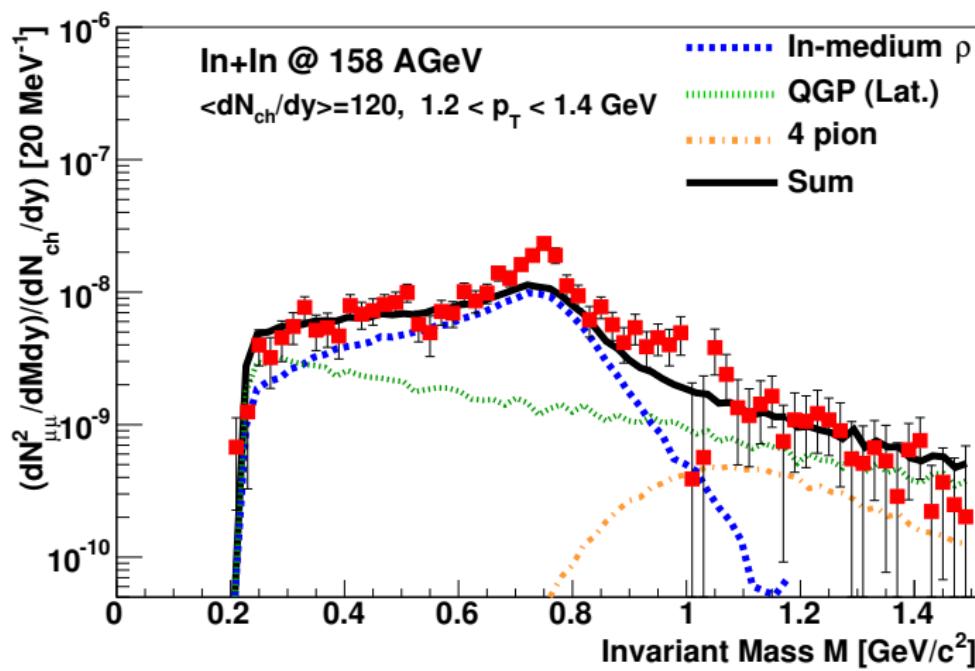
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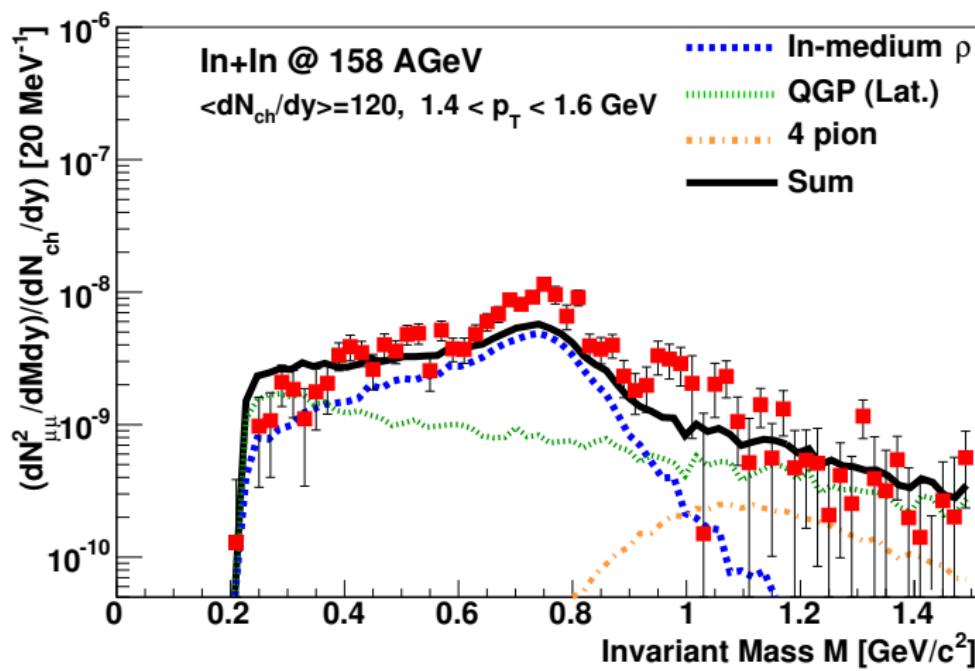
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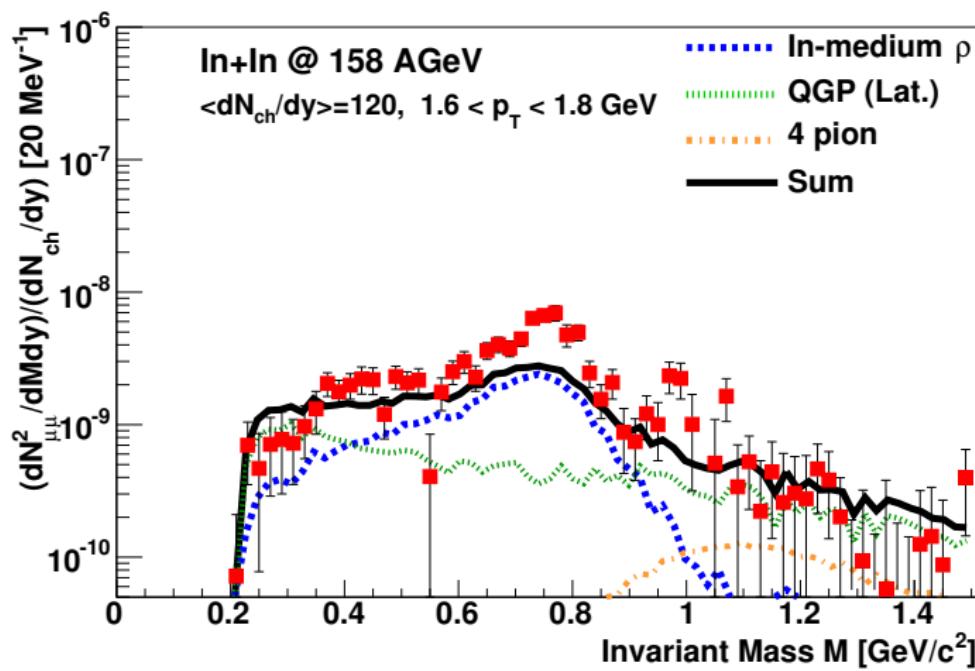
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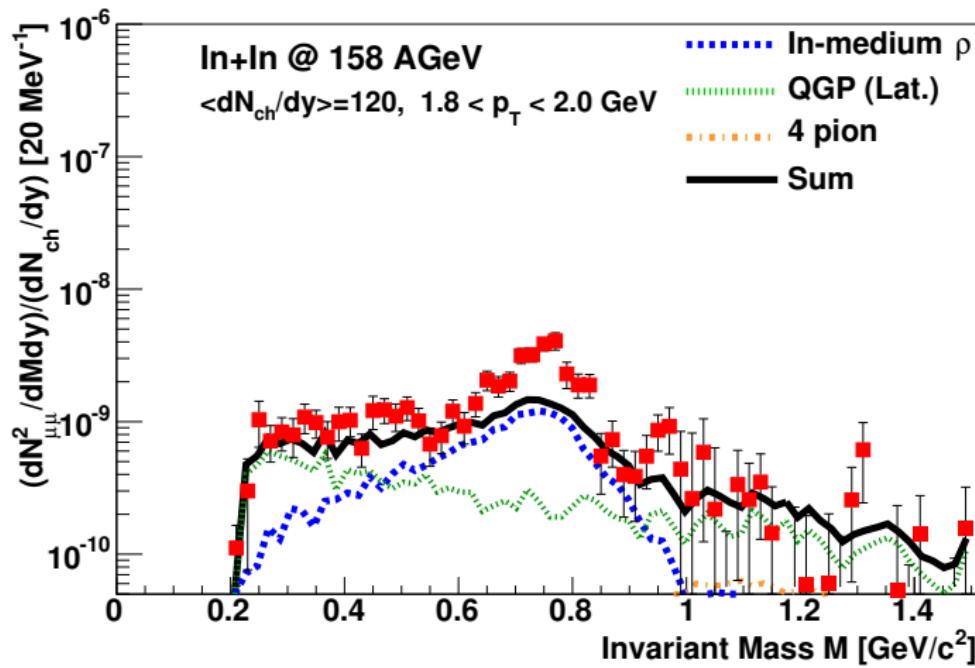
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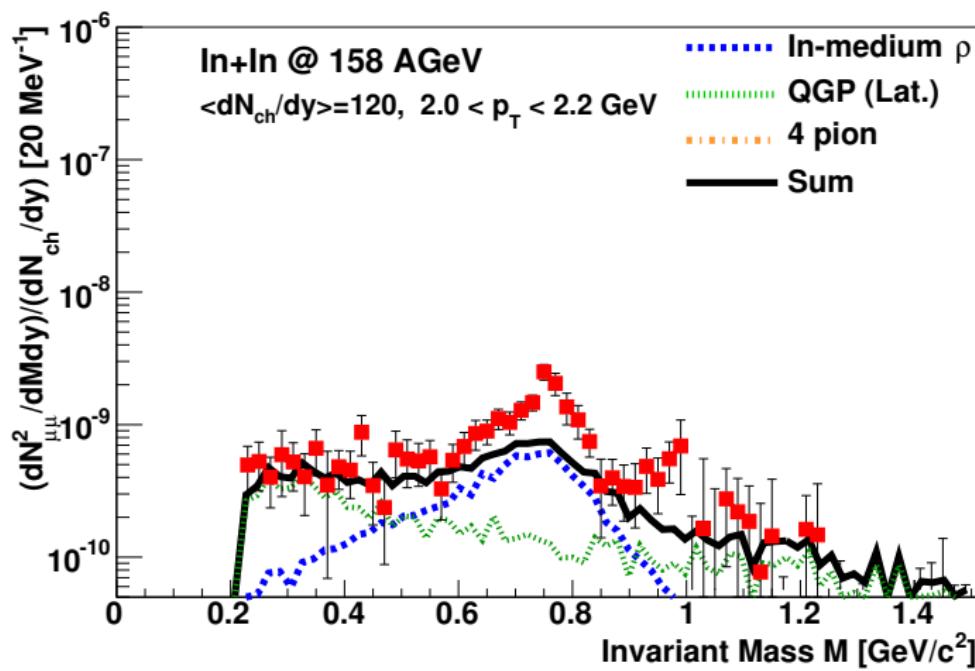
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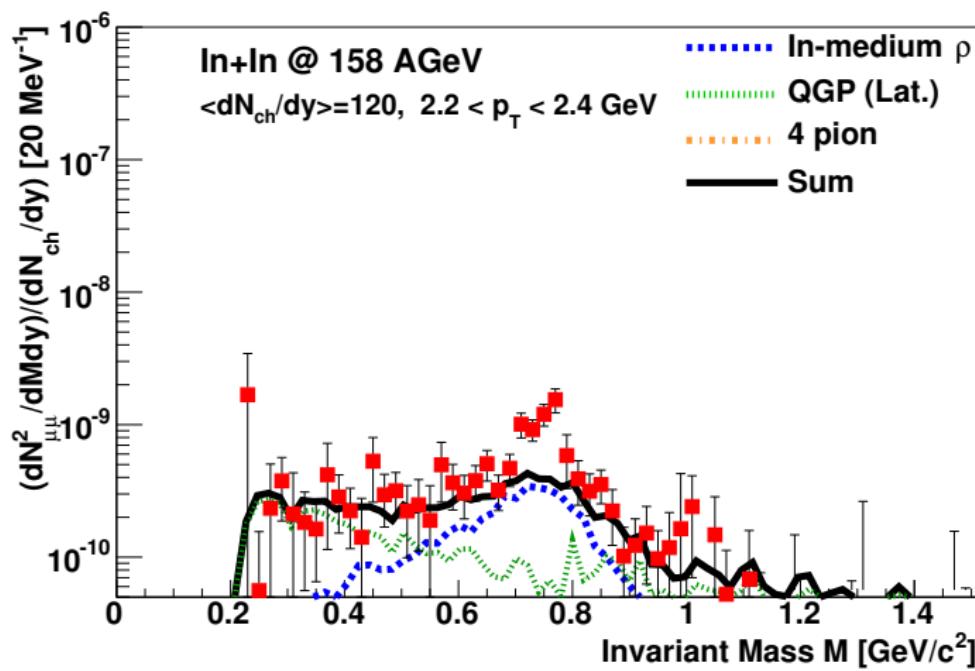
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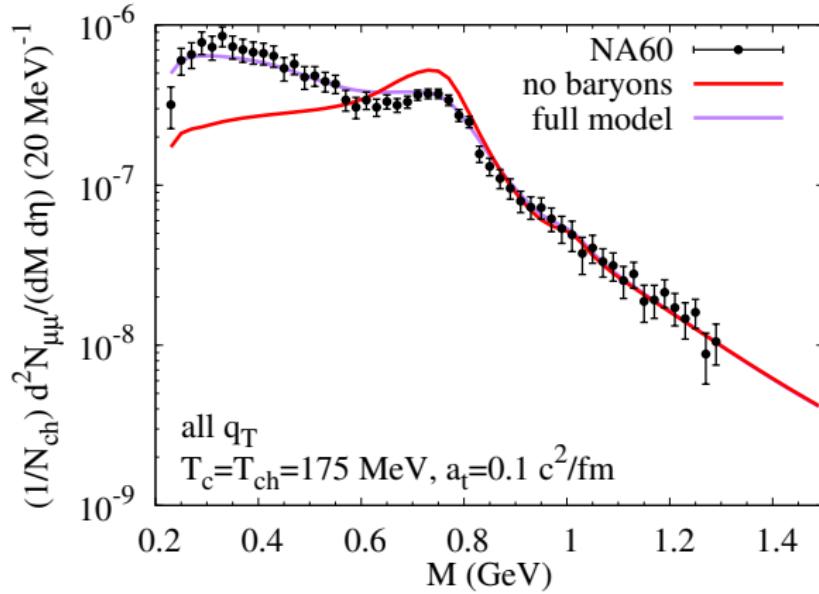
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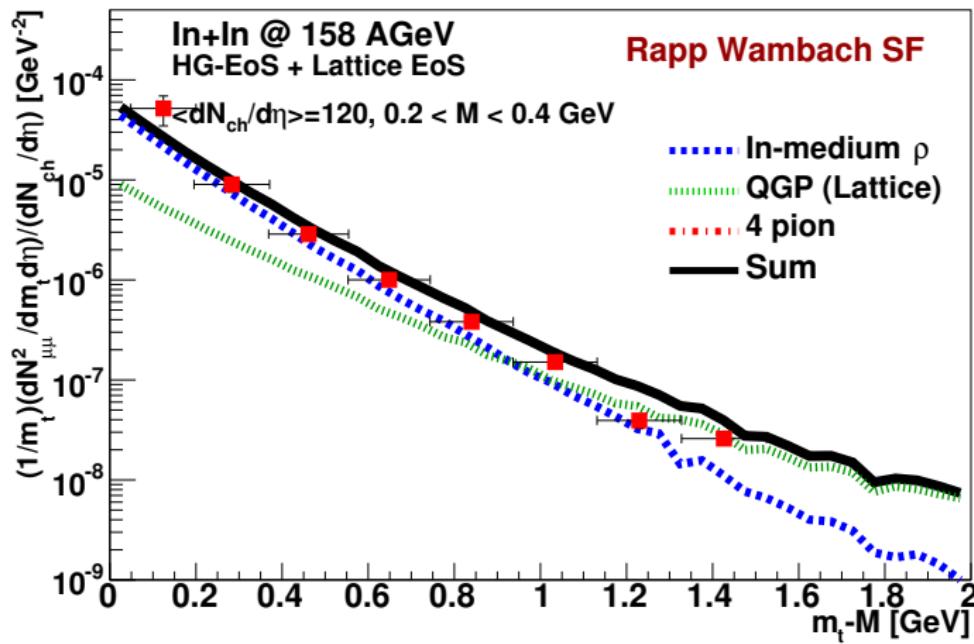
CGUrQMD: In+In (158 AGeV) (SPS/NA60)

- dimuon spectra from $\text{In} + \text{In}(158 \text{ AGeV}) \rightarrow \mu^+ \mu^-$ (NA60)
- min-bias data ($dN_{\text{ch}}/dy = 120$)
- influence of baryon interactions in spectral function
- from previous calculation with thermal-fireball parametrization (compatible with course-grained UrQMD)



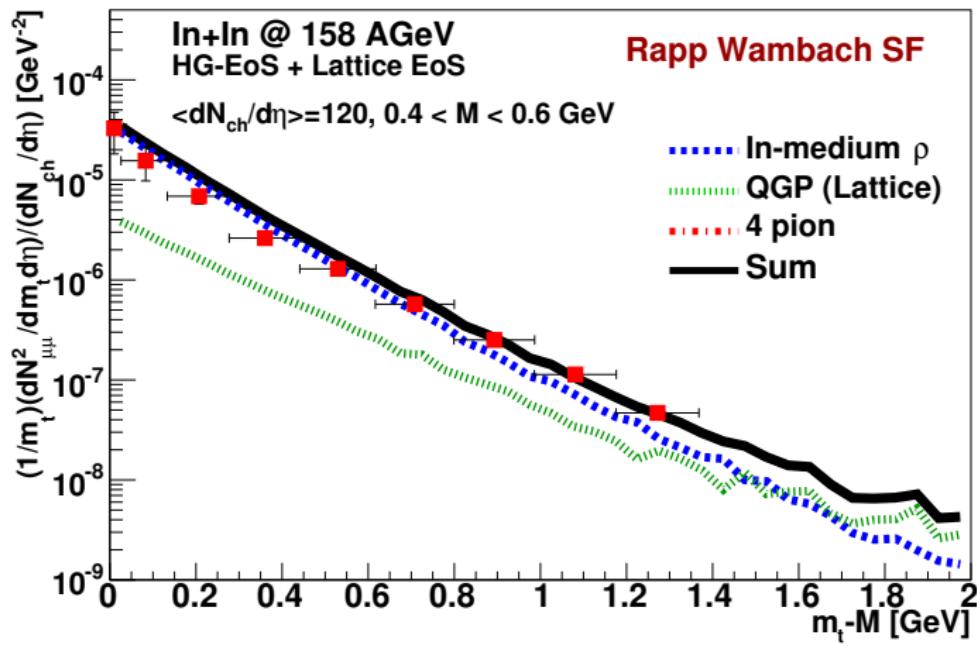
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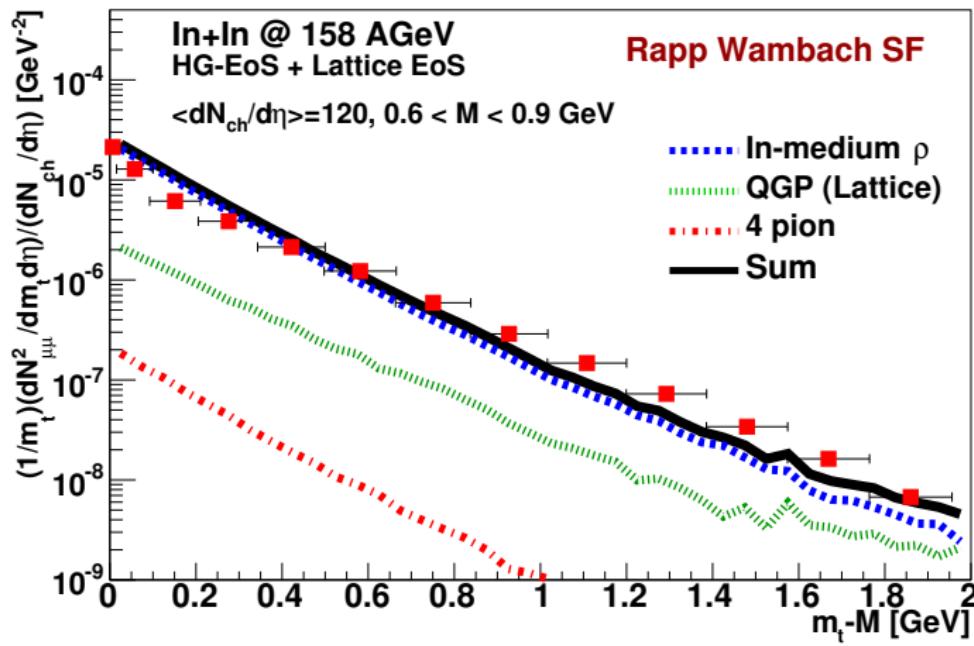
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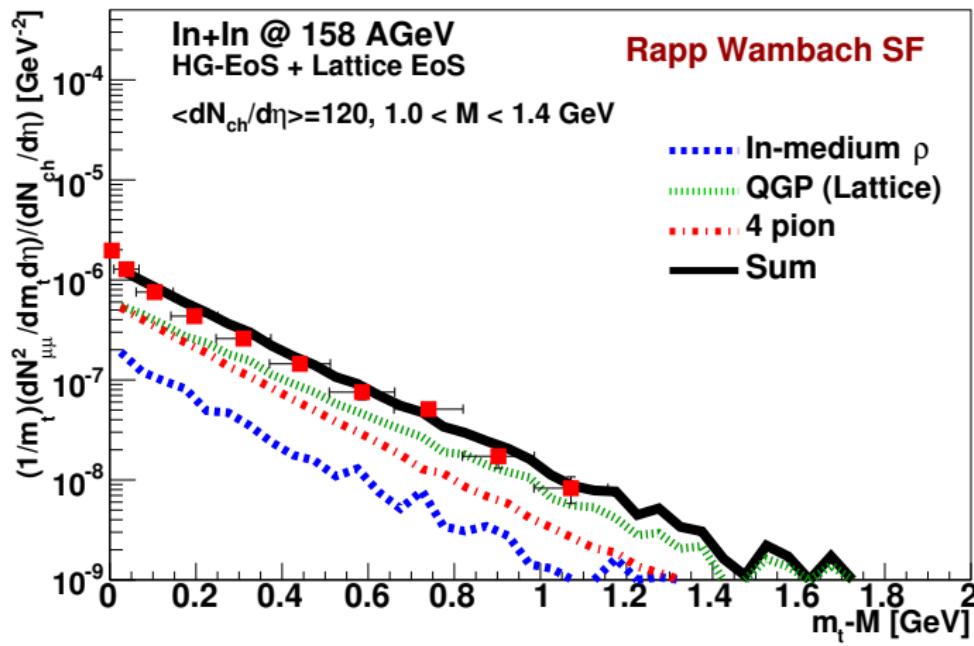
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Conclusions and Outlook

- General ideas

- em. probes \Leftrightarrow in-medium em. current-correlation function
- dual rates around T_c (compatible with χ symmetry restoration)
- medium modifications of ρ , ω , ϕ
- importance of baryon-resonance interactions

- Application to dileptons in HICs

- need realistic bulk-medium evolution
- thermal fireball, (ideal) hydrodynamics, transport
- coarse-grained transport (here: CGUrQMD)
- allows use of thermal-QFT spectral VM functions
- applicable also at low collision energies
- allows use of thermal-QFT models for em. current-correlation functions
- successful description at HADES, SPS, and RHIC (STAR)
- consistent description of M and m_T spectra!

- Outlook

- effective slope of M spectra in higher IMR ($1.5 \text{ GeV} < M < M_{J/\psi}$) provides $\langle T \rangle$
- beam-energy scan at RHIC and FAIR \Rightarrow signature of phase transition?
- signature of cross-over vs. 1st order (or even critical endpoint)?

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